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Fracture Mechanics Analysis of Centered & Offset Fastener Holes in Stiffened & Unstiffened Panels under Uniform Tension

Massachusetts Inst of Tech Cambridge

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FRACTURE MECHANICS ANALYSIS OF CENTERED AND OFFSET FASTENER HOLES IN STIFFENED AND UNSTIFFENED PANELS UNDER UNIFORM TENSION

AEROFLASTIC AND STRUCTURES RESEARCH LABORATORY DEPARTMENT OF AERONAUTICS AND ASTRONAUTICS MASSACHUSETTS INSTITUTE OF TECHNOLOGY CAMBRIDGE, MASSACHUSETTS 02189

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This report documents a finite-element analysis procedure for computation of Mode I and Mode II stress intensity factors associated with one or two sharp cracks emanating from a fastener hole in a panel under uniform tension. The fastener hole may be offset from the panel centerline, and one or both edges of the panel may be integrally stiffened. The formulation of a special assumed-stress hybrid element for the region near the fastener

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hole is presented. A detailed description of the programming covers the physical problem, modelling, program flow and options, input/output conventions, execution times, and limitations which must be observed. Results are presented for performance tests of the special element, and for some example analyses of cracked panels.

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FOREWORD

The developments documented in this report were carried out at the Aeroelastic and Structures Research Laboratory, Massachusetts Institute of Technology, Cambridge, Massachusetts 02139, under Contract No. F33615-74-C-3063 (Project 1367, Task 136703) from the U.S. Air Force Flight Dynamics Laboratory. Mr. James L. Rudd (AFFDL/FBE) served as technical monitor. The authors gratefully acknowledge the many contributions by Mrs. Susan E. French of the Aeroelastic and Structures Research Laboratory. Mrs. French was involved with the detailed programming aspects of the work throughout the project. This report is the second in a series, covering research conducted during October 1974-February 1975, and was submitted for technical review in May 1975. The other reports in this series are AFFDL-TR-75-51 (Fracture Mechanics Analysis of an Attachment Lug), Analysis of an Attachment Lug), Analysis 75-71. (Fracture Mechanics Analysis of Single and Double Rows of Fastener Holes Loaded in Bearing), and AFFDL-TR-76-12 (Numerical Computation of Stress Intensity Factors for Aircraft Structural Details by the Finite Element Method). The contractor's report number is ASRL TR 177-2.

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Section 1

INTRODUCTION

This is the second of a series of reports on the development of finite-element analysis procedures for computation of linear elastic stress intensity factors associated with cracks in common aircraft structural details. Finite-element analysis serves the important purpose of providing $\mathbf{K}_{\mathbf{I}}$ and $\mathbf{K}_{\mathbf{II}}$ solutions for situations in which the boundary geometries are too complicated to permit convenient treatment by the classical methods.

The first report in the series [1] summarized the formulation of two basic building blocks which are used in the analyses: the well-known bilinear isoparametric quadrilateral and the PCRK59 assumed-stress hybrid crack-containing elements. The former element has been widely accepted and appears in most general-purpose finite-element programs. The latter element was originally developed at ASRL in 1972 [2], and has subsequently been put through extensive performance tests to characterize its behavior as a function of shape distortions [3].

Earlier work [4, 5] has demonstrated that the assumedstress hybrid method permits accurate computation of stress intensity factors, while preserving Matrix Displacement Method conventions in the global programming environment (data input, assembly, matrix solution procedure, etc.). In the present work, the hybrid method is used again to formulate another specialpurpose element for modelling the region around a fastener hole. The new element is combined with the quadrilateral and PCRK59 to represent a skin tension panel containing an open fastener hole. The ASRL FEABL program [6] is again used for global analysis. Additional features belonging to FEABL which have not yet been formally documented are employed in the present analysis, and are outlined briefly in this report. These features pertain to the technique of substructuring by a Gauss elimination algorithm.

Section 2

NEW DEVELOPMENTS

Modularization of the finite-element model of a structure becomes as important as modularization of the basic program when the application is computation of stress intensity factors. The objective is to reduce unnecessary arithmetic operations and computer printout to a minimum. In particular, the stresses and displacements are of little interest (and of no interest at all at any distance away from the crack tip) except for verifications of accuracy during development. The substructuring technique, used for many years in airframe analysis programs*, provides the required modularity. Subroutines for substructuring were developed as add-ons to FEABL as pirt of an unrelated project** and have been used in the present work. The substructuring algorithm and the functions and conventions of the add-on subroutines are discussed briefly in this section to provide a complete picture of the panel analysis program.

The so-called "near-field" region around a fastener hole forms one such substructure module. The first attempt to model this region with conventional quadrilateral elements resulted in

^{*}For example, the Boeing ASTRA program.

^{**}Sponsored by the Xerox Corporation (Dr. T. C. Soong, technical monitor).

severe mesh distortion, numerous unwanted degrees of freedom, and solution accuracy problems. In consequence, the hybrid method was called upon, resulting in the HOLEI special-purpose element for this module. The history of these investigations is traced in Subsections 2.3 and 2.4.

2.1 Substructuring

Figure 1 illustrates the finite-element model of a square panel which contains a single fastener hole offset from the panel centerline. A detail in the lower part of the figure shows how a PCRK59 element might be inserted to represent a small crack emanating from the hole. It is evident that the complete global solution (displacements at each of the many nodes in the model) constitutes unwanted information if the analysis is to be repeated while the crack location is varied parametrically around the fastener hole.

A computationally more efficient procedure is obtained by subdividing the model into far-field and near-field substructures, as shown in Fig. 2. The broken line in Fig. 2 corresponds to the edges ABCD in Fig. 1. If the element stiffnesses, prescribed nodal forces and nodal displacements are first assembled for the far-field substructure, the resulting equation system may be partially solved. In effect, all of the information pertaining to the far field substructure is transferred to the inter-substructure boundary ABCD. This information may then be treated as a "super-element", which can be assembled with a succession

of near-field substructures containing a crack in different locations. As a result, many fewer degrees of freedom are processed in the parametric stress intensity computations.

The substructuring process may be represented formally as follows. Let the assembled equation system $K q = \hat{Q}$ for a substructure be partitioned into:

$$\begin{bmatrix}
K_{11} & K_{1B} \\
K_{81} & K_{8B}
\end{bmatrix}
\begin{bmatrix}
\mathbf{q}_{1} \\
\mathbf{q}_{B}
\end{bmatrix} = \begin{bmatrix}
\hat{\mathbf{Q}}_{1} \\
\hat{\mathbf{Q}}_{B}
\end{bmatrix}$$
(1)

where

K = stiffness coefficients

q = (unknown) nodal displacements

Q = prescribed nodal forces

and where $K_{BI} = K_{IB}^{T}$. Subscripts I and B refer to nodes and degrees of freedom which are considered respectively as "interior" (to be eliminated) and "boundary" (to be retained for subsequent assembly along the inter-substructure boundary). The interior degrees of freedom are formally eliminated by solving the first of Eqs. 1 and substituting into the second:

$$K_{11} Q_{1} + K_{18} Q_{8} = \hat{Q}_{1}$$

$$Q_{1} = K_{11}^{-1} \hat{Q}_{1} - K_{11}^{-1} K_{18} Q_{8}$$
(2)

$$\overset{\sim}{\mathbf{K}}^{g} \left(\overset{\sim}{\mathbf{K}}_{1}^{g} \overset{\sim}{\mathbf{G}}^{z} - \overset{\sim}{\mathbf{K}}_{1}^{g} \overset{\sim}{\mathbf{K}}^{g} \overset{\sim}{\mathbf{G}}^{g} \right) + \overset{\sim}{\mathbf{K}}^{g} \overset{\sim}{\mathbf{G}}^{g} = \overset{\sim}{\mathbf{G}}^{g}$$
(3)

A rearrangement of the terms in Eq. 3 leads immediately to:

$$\overset{(c)}{\kappa}_{BB} \overset{\bullet}{q}_{B} = \overset{\bullet}{Q}_{BB}^{(c)}$$
(4)

where $K_{BB}^{(c)}$, $\hat{Q}_{B}^{(c)}$ are the statically condensed stiffnesses and forces, given by:

$$\overset{\sim}{\mathbf{K}}_{BB} = \overset{\sim}{\mathbf{K}}_{BB} - \overset{\sim}{\mathbf{K}}_{BI} \overset{\sim}{\mathbf{K}}_{II} \overset{\sim}{\mathbf{K}}_{IB}$$
(5)

$$\hat{Q}_{8}^{(c)} = \hat{Q}_{8} - \mathbf{K}_{81} \mathbf{K}_{11}^{-1} \hat{Q}_{1}$$
(6)

It is apparent from Eqs. 5 and 6 that the substructuring process may be realized as a computing algorithm independent of the unknowns $g_{\rm I}$, $g_{\rm B}$. In practice, the process may be programmed to eliminate one degree of freedom (one equation) from the system at a time, so that inversion of $K_{\rm II}$ is avoided. The entire algorithm then consists of as many passes through the assembled equations as there are degrees of freedom to be eliminated, a procedure quite similar to the Gauss-Cholesky factoring methods normally used to solve the whole equation system [6].

Substructuring places an additional burden on the program user when the global software stores K as a band-matrix. It can be shown by tracing the details that the elimination algorithm inflates the stiffness matrix bandwidth if g_I and g_B are arbitrarily

interspersed. However, if $q_{\rm I}$ always appear as the first degrees of freedom in the global numbering sequence, the bandwidth of K is not affected by elimination. This restriction has been placed on the FEABL add-on subroutines, and it requires some care in the choice of global numbering sequence and substructure boundary locations on the user's part.

The foregoing derivation of the substructuring algorithm assumes that all the prescribed quantities are nodal forces \hat{Q} , while all of the displacements \hat{q} are unknowns. However, if restraints are applied to the substructure such that a subset \hat{q}_{I} of the interior degrees of freedom \hat{q}_{I} are prescribed, Eqs. 2 through 6 may still be used. The only difference is that the rows and columns of K corresponding to \hat{q}_{I} are decoupled from the equation system*, while the right hand side of Eqs. 1 is replaced by:

$$\{ \hat{\mathbf{Q}}_{\mathbf{I}} | \hat{\mathbf{Q}}_{\mathbf{B}} \} = \{ \hat{\mathbf{Q}}_{\mathbf{I}} \text{ or } \hat{\mathbf{q}}_{\mathbf{I}_{o}} | \hat{\mathbf{Q}}_{\mathbf{B}} - \mathbf{K}_{\mathbf{B}} \hat{\mathbf{q}}_{\mathbf{I}_{o}} \}$$
 (7)

2.2 Implementation of Substructuring in FEABL

Three add-on subroutines have been programmed and verified for the gradual computation tasks associated with substructuring. Subroutine STACON executes the Gauss elimination algorithm on a band-matrix which has been assembled and stored in accordance with

^{*}See Ref. 6, Subsection 3.2.5.

the existing FEABL conventions. A normal MAIN program is written to control the FEABL software up to the point at which K would be factored in a conventional analysis. However, instead of factoring the instructions:

ISGN =

CALL STACON (ISGN, NID, RNAME, INAME)

is programmed, where

The control parameter ISGN must be set to +1, -1 or 0 before STACON is called. A value of +1 aborts the run if K is not a positive-definite matrix. A value of -1 aborts the run if K is singular. A value of 0 always results in return to the MAIN program with ISGN reset according to the actual matrix condition encountered: positive-definite (+1), non-positive but nonsingular (negative integer), or singular (0). The positive-definite option is used in conventional finite-element analyses. The nonsingular option is used in special cases, e.g., Hermann's principle for which ideally incompressible elements include volumetric constraints in the assembled equation system. The option ISGN=0 may be used generally, in programs for which the user wishes to retain control for debugging or other purposes when an error condition is encountered. Subroutine STACON carries out the elimination process in place,

as shown schematically in Fig. 3. After execution, the statically condensed force vector appears in INAME(IQ+NID) to INAME(LQ) and the statically condensed stiffness coefficients appear in INAME(J) to INAME(LK), where:

$$J=IK+INAME(IKØUNT+NID)+NID+1$$
 (8)*

The shaded areas shown in Fig. 3 contain the back-substitution information \tilde{K}_{II}^{-1} \hat{Q}_{I} and \tilde{K}_{II}^{-1} \tilde{K}_{IB} , which may be used to solve for q_{I} (Eq. 2) after q_{IB} has been computed.

The statically condensed stiffnesses and forces may simply be transferred to another storage area and treated thereafter as a "super-element" if desired. A general programming sequence to execute the transfer is given in Appendix A. If this is done, the substructure may later be assembled into a complete structure with subroutine ASEMBL or subroutine ASMLTV. A list of local-to-global degree-of-freedom connections must be given for the "super-element", just as is done for any ordinary element. However, while the numbering convention for an ordinary element is fixed by the manner in which the element subroutine has been programmed, the convention for a "super-element" is determined by the user's sequence of global numbering for assembly of the substructure. For example, if the far-field substructure in Fig. 2 has been

^{*}IKØUNT is another address control parameter. See Ref. 6, subsections 2.1.3, 2.2.2 and 2.2.6.

numbered such that the boundary degrees of freedom are globally assigned in the order A+B+C+D+A, then the connections of the far-field "super-element" to the near-field portion of the model must be given in that order.

A second option available to the user is to leave the statically condensed substructure in place and to employ a second DATA vector for assembly and solution of the complete structure. Add-on subroutine ASMSUB has been programmed for this option. Subroutine ASMSUB performs a function similar to the conventional assembly routines (ASEMBL, ASMLTV), but is capable of assembling $K_{BB}^{(c)}$, $\hat{Q}_{B}^{(c)}$ directly from one DATA vector into another. Since two DATA vectors must be manipulated simultaneously, extra address control parameters are required. The beginning of the program might appear as follows:

DIMENSION RNAMEL(xxx), INAMEL(xxx), RNAMEL(yyy), INAMEL(yyy)

EQUIVALENCE (RNAME1(1), INAME1(1))

EQUIVALENCE (RNAME2(1), INAME2(1))

COMMON /SIZE/ NET, NOT

COMMON /BEGIN/ TON, IKOUNT, ILNZ, IMASTR, IQ, IK

COMMON /END/ LCON, LKOUNT, LLNZ, LMASTR, LQ, LK

COMMON /SIZESS/ NETSS, NDTSS, NIDSS

COMMON /BEGSS/ IBEG(6)

CONMON /ENDSS/ LEND(6)

Now suppose that a substructure is assembled and statically

condensed in vector (RNAME1,INAME1):

•

ISGN=1

CALL STACON(ISGN, NID, RNAME1, INAME1)

At this point, the substructure's control information must be cleared from the labelled COMMON areas to permit formation of the complete structure. The information is transferred to the extra areas:

NETSS=NET

NDTSS=NDT

NIDSS=NID

IBEG(1)=ICON

•

LEND(6)=LK

•

The program continues with a conventional generation of size, connections, assembly, etc. for the complete structure in vector (RNAME2, INAME2) until the substructure is to be assembled. At this point, the user simply programs:

CALL ASMSUB(LNUM, RNAME1, INAME1, RNAME2, INAME2)

where LNUM represents the element number assigned to the substructure, considered as a "super-element" in the complete structure.

There are some cases for which the solution q_1 may be required in a particular substructure. Subroutine QBACK has been programmed as the third add-on to execute the required back-substitution solution for q_1 . Subroutine QBACK is designed to work with ASMSUB in the multiple DATA vector environment. Suppose that the above example is continued to the point at which assembly and constraint of the structure equation system are complete. Factoring and global solution now follow:

CALL FACT(ISGN, RNAME2, INAME2)

CALL SIMULO(ENERGY, RNAME2, INAME2)

At this point, vector (RNAME2, INAME2) contains the solution \mathbf{q} for the complete structure. Part of \mathbf{q} is, in fact, the boundary displacement solution $\mathbf{q}_{\mathbf{B}}$ for the substructure. An interior solution may be obtained by continuing with:

CALL QBACK(LNUM, RNAME1, INAME1, RNAME2, INAME2)

After execution of QBACK, the substructure global solution $\{q_1,q_B\}$ appears in vector (RNAME1,INAME1). The solution will also be

printed by subroutine QBACK.

2.3 Experiment with Conventional Mesh

The first attempt to model the panel and fastener hole was made with conventional quadrilaterals and a 5-node hybrid mesh-expander element. Experience with analysis of an attachment lug detail [1] indicated that at least 24 quadrilaterals should be placed around the hole to obtain accurate solutions. One then faces the following choices for the panel:

- Mesh expansion in the near-field region to reduce the number of divisions below 24 on the near/far-field boundary (ABCD in Figs. 1 and 2).
- 2. Acceptance of 24 divisions on the near/far-field toundary and continuation of this detail into the far-field region.
- Acceptance of 24 divisions on the boundary, with some mesh expansion immediately outside the near-field region.

The first choice was judged to be unlikely to give accurate computed displacements near the hole because of the severe shape distortions which the mesh-expander elements would have caused. The second choice was deemed to be unacceptable in that too many unwanted degrees of freedom would be placed in the far-field region, making either one-stage solution or substructuring computationally inefficient. The third choice was consequently selected as the best compromise between computational efficiency and solution accuracy near the hole.

Figure 4 illustrates a typical mesh for a panel with the fastener hole centered. Extra detail is kept in the far-field

region to the right of the hole in order to permit the hole to be offset continuously toward the right edge of the panel while avoiding extreme aspect ratios in the far-field elements. Tests with this model quickly showed that the asymmetric mesh grading led to highly asymmetric behavior of the computed solutions. Figure 5 illustrates a typical example. Computed horizontal displacement of the left and right edges of the panel are shown for the case of uniform vertical tension and the fastener hole centered. The inaccuracy of the model was judged to have been caused by the combination of asymmetric mesh grading, aspect ratio effects, and shape distortions in the near-field region.

The conclusion was that conventional finite-element models could be made to work for the panel structure only with very fine detail, and therefor at an unacceptably high computing cost. Lest it be thought that too much accuracy has been demanded from the analysis, we remind the reader that more than an engineering solution is required to achieve the ultimate goal. In considering the accuracy of the K_I and K_{II} solutions, it has been shown [1, 3] that shape distortions of the PCRK59 element alone can account for as much as 3 to 5 percent error. Furthermore, direct verification of accuracy by comparison with independent methods is possible only for K_I with cracks emanating horizontally from the fastener hole. Hence, a finite-element model capable of computing highly accurate displacements near the fastener hole is required to achieve engineering accuracy in the final answer. As a result, the assumed-stress hybrid method was investigated as a possible

alternate way of handling the transition from the circular hole geometry to the cartesian geometry of the near/far-field boundary.

2.4 Creation of a Hybrid Fastener Hole Element

The energy principles on which hybrid elements are based have been reviewed previously [1]. The energy principle \mathbf{T}_1 was chosen for the present investigation, giving the general form of an element stiffness matrix as:

$$\mathbf{k} = \mathbf{G}^{\mathsf{T}} \mathbf{H}^{\mathsf{T}} \mathbf{G}$$

where

$$\mathbf{G} = t \int_{\partial A} (\mathbf{NP})^{\mathsf{T}} \mathbf{L} \, dA \tag{10}$$

$$\frac{\mathbf{H}}{\mathbf{H}} = \mathbf{t} \int_{\mathbf{A}} \mathbf{P}^{\mathsf{T}} \mathbf{S} \mathbf{P} dA \tag{11}$$

and where

A = Element area

 $\partial A = Element boundary$

L = Matrix of assumed-displacement interpolation functions defined on 3A.

N = Matrix of direction cosines for the outward normal to ∂A .

P = Matrix of assumed-stress shape functions.

S = Matrix of elastic compliance constants.

t = Element thickness (assumed to be unity without loss of generality). Two fundamental properties of hybrid elements make them useful in linear elastic plane stress and plane strain analyses:

- 1. Great flexibility in choice of element shape is permitted, since L need be defined only in terms of an arc length coordinate from node to node along ∂A, and since the shape functions P need only satisfy the continuum equilibrium equations.
- 2. Many shape functions P can be chosen to satisfy equilibrium and at the same time allow the element to closely mimic a particular local stress distribution.

Both properties have been used to advantage in the development of an element for the near-field region.

Practical application of the hybrid method requires that the analyst account for known local behavior in the formulation of his element. In the present case, one reasonably expects to see $\sin(2\theta)$ and $\cos(2\theta)$ components in the stress distribution near a fastener hole in a panel under tension, as well as terms independent of θ . Second, one should expect to see the near/far-field boundary deform in the manner shown schematically in Fig. 6. Simulation of this behavior requires that the element have at least three nodes (corners and mid-edge) along its near/far-field boundary edge. Third, the element must be kinematically stable, since it will be placed in the mesh so as to separate two conventionally modelled regions. Kinematic stability is assured if:

 $m \geqslant n-3 \tag{12}$

for plane stress and plane strain elements, where

- m = Total number of assumed-stress shape functions.
- n = Total number of nodal degrees of freedom (displacements) in the element.

Finally, at least 20 nodes should be provided along the circular inner boundary, which may serve either as the fastener hole boundary or as an interface to which quadrilaterals and PCRK59 elements may be coupled.

The kinematic stability condition results in a quick determination that modelling of the entire near-field region with a single element would be impractical. For example, assumption of the minimum number of nodes (8 along the outer, 20 along the inner boundary) results in a 56-degree of freedom element which requires m > 53 assumed-stress shape functions. It is seen from Eqs. 9 and 11 that H is an mxm matrix which must be inverted to compute the element stiffness matrix. Furthermore, H is fully populated. The single-element approach was rejected in view of the difficulty in finding 5. shape functions and the computational inefficiency associated with inversion of a 53 x 53 matrix.

A 90-degree segment of the near-field region was the first geometry for which an element development was attempted. The element shape, shown in Fig. 7, encompasses one quarter of the circular boundary and one edge of the near/far-field boundary. With 20 divisions allowed around the hole, the element possesses 6 inner nodes in addition to its 3 near/far-field boundary nodes.

The element can be subjected to rotation transformations and repeated assembly to model the entire near-field region. The kinematic stability requirement now leads to $m \ge 18 - 3 = 15$ for the minimum number of stress shape functions. However, since rotation transformations are contemplated, insensitivity to orientation enters as another practical requirement. This leads to a choice of m=16, as explained in Subsection 2.5. Tests of the 9^n -degree element highlighted a problem of inaccuracy in the integration for the H matrix (Eq. 11), which was judged to have been caused by the presence of terms in $\sin(4\theta)$ and $\cos(4\theta)$ in the stress shape functions P.

The approach finally adopted divides the near-field region into eight 45-degree elements. Figure 8 illustrates the basic element, which possesses 4 nodes along its circular boundary. The element possesses 12 degrees of freedom, and therefore $m \ge 9$ is required. To preserve orientation insensitivity, m=10 is chosen, so that all $\sin(2\theta)$ and $\cos(2\theta)$ terms are included in P. The entire near-field region is assembled by first computing k_1 for the basic element and then subjecting k_1 to a series of transformations for the seven other elements shown in Fig. 9.

2.5 Final Formulation of Hybrid Hole Element

The choice of assumed-displacement interpolation functions for the hybrid element is dictated by the need to maintain interelement compatibility along its edges. Since the hole element must be capable of coupling to a quadrilateral or a PCRK59 segment between each pair of nodes, linear interpolation must be used.

In general,

where q_1 , q_2 , ... q_{12} are defined in Fig. 8, and where

u(A) = Horizontal edge displacement.

v(4) = Vertical edge displacement.

Length of edge between a pair of nodes.

The arc coordinate A in Eq. 13 is a relative measure of distance along any edge, with the positive sense taken as counterclockwise for integration along ∂A . Note also that the nonzero terms in L appear in different positions for different edges. For example,

$$\begin{array}{c}
L_{34} =
\begin{bmatrix}
0 & 0 & 0 & 0 & 1 - 4/2 & 0 & 4/2 & 0 & 0 & 0 & 0 \\
0 & 0 & 0 & 0 & 0 & 1 - 4/2 & 0 & 4/2 & 0 & 0 & 0 & 0
\end{bmatrix}$$
(14)

for the edge between nodes 3 and 4, while

for the edge between nodes 6 and 1. In a similar manner,

$$A = 0$$
, l_{34} at nodes 3,4

 $A = 0$, l_{61} at nodes 6,1

and so forth. These changes of definition do not cause difficulties in the boundary integration (Eq. 10) because the computation is carried out numerically, one edge at a time.

Assumed-stress shape functions are selected most conveniently by direct adaptation from classical elasticity solutions in polar coordinates. Let an Airy stress function Φ (r, θ) be defined by:

$$\mathcal{T}_{rr} = \frac{1}{r} \frac{\partial \overline{\Phi}}{\partial r} + \frac{1}{r^2} \frac{\partial^2 \overline{\Phi}}{\partial \theta^2} \qquad \mathcal{T}_{\theta\theta} = \frac{\partial^2 \overline{\Phi}}{\partial r^2} \qquad \mathcal{T}_{r\theta} = \frac{1}{r^2} \frac{\partial \overline{\Phi}}{\partial \theta} - \frac{1}{r} \frac{\partial^2 \overline{\Phi}}{\partial r \partial \theta} \tag{17}$$

Then the equations of elasticity for homogeneous isotropic material reduce to:

$$\nabla^2 \nabla^2 \Phi(r, \theta) = 0 \tag{18}$$

where

$$\nabla^2 = \frac{\partial^2}{\partial r^2} + \frac{1}{r} \frac{\partial}{\partial r} + \frac{1}{r^2} \frac{\partial^2}{\partial \theta^2}$$
 (19)

By assuming as an expansion for the stress function:

$$\Phi(r,\theta) = \phi^{(0)}(r) + \sum_{n=1}^{\infty} \phi^{(n)}(r) \left[\sin(n\theta) \text{ or } \cos(n\theta) \right] \tag{20}$$

it can be shown that Eq. 18 reduces to a set of equidimensional ordinary differential equations in $\phi^{(0)}(r)$, $\phi^{(1)}(r)$,..., for

which the following solutions are obtained [7]:

$$\phi^{(0)}(r) = a_0 + b_0 \ln r + c_0 r^2 + d_0 r^2 \ln r$$
 (21)

$$\phi^{(n)}(r) = a_n r^n + b_n r^{-n} + c_n r^{2+n} + d_n r^{2-n}; n \ge 2$$
 (22)

Stress distributions corresponding to Eqs. 21 and 22 are obtained by substituting back into Eqs. 17 [7]:

$$\mathcal{T}_{rr}^{(0)} = \frac{b_{o}}{r^{2}} + 2c_{o} + d_{o} (1 + 2 \ln r)
\mathcal{T}_{\theta\theta}^{(0)} = -\frac{b_{o}}{r^{2}} + 2c_{o} + d_{o} (3 + 2 \ln r)
\mathcal{T}_{r\theta}^{(0)} = 0$$
(23)

and

$$T_{rr}^{(n)} = \left[a_n (n - n^2) r^{n-2} - b_n (n + n^2) r^{-n-2} + C_n (2 + n - n^2) r^n + d_n (2 - n - n^2) r^{-n} \right] \left[sin(n\theta) \text{ or } cos(n\theta) \right]$$

$$T_{\theta\theta}^{(n)} = \left[a_n (n^2 - n) r^{n-2} + b_n (n^2 + n) r^{-n-2} + C_n (2 + 3n + n^2) r^n + d_n (2 - 3n + n^2) r^{-n} \right] \left[sin(n\theta) \text{ or } cos(n\theta) \right]$$

$$T_{r\theta}^{(n)} = \left[a_n (n^2 - n) r^{n-2} - b_n (n^2 + n) r^{-n-2} + C_n (n^2 + n) r^n + d_n (n^2 - n) r^{-n} \right] \left[-cos(n\theta) \text{ or } sin(n\theta) \right]$$

$$(24)$$

^{*}The solution for $\phi^{(1)}$ (r) is of no interest in the present work. Terms in $\sin\theta$ and $\cos\theta$ correspond to problems in which a discontinuity has been introduced, e.g., re-welding of an annulus after a segment has been cut out.

The undetermined coefficients b_0 , c_0 , ..., d_n in Eqs. 23 and 24 play the role of assumed-stress degrees of freedom, which are eliminated when the element stiffness matrix is formed [1]. The remaining r0-dependent portions of the terms are placed in the shape function matrix P.

Shape functions have been chosen from Eqs. 23 and 24 as follows. For the θ -independent terms, logarithmic behavior is not particularly desirable; only the $\mathbf{b}_{_{\mathbf{O}}}$ and $\mathbf{c}_{_{\mathbf{O}}}$ terms have been retained. This choice is admittedly arbitrary. To complete P, enough θ -dependent terms are chosen from 2θ , 4θ , 8θ ,... behavior to satisfy kinematic stability and orientation insensitivity. The latter requirement demands, e.g., that all 20-dependent terms be retained if any are required for stability. It is apparent from Eqs. 24 that there are eight $n\theta$ -dependent terms for each n when $sin(n\theta)$ and $cos(n\theta)$ terms are included. Thus, selection of the 2θ -dependent terms provides a total of 10 shape functions, just enough to satisfy the requirements for the 45-degree element (The 90-degree element requires addition of the 40-dependent terms as well, making a total of 18 shape functions.). The shape function matrix, as finally adopted for the 45-degree element, is given by:

$$P_{(r,\theta)} = \begin{cases} -2\cos 2\theta - 6\cos 2\theta/r^4 & 0 & -4\cos 2\theta/r^2 - 2\sin 2\theta \\ 2\cos 2\theta & 6\cos 2\theta/r^4 & 12r^2\cos 2\theta & 0 & 2\sin 2\theta \\ 2\sin 2\theta - 6\sin 2\theta/r^4 & 6r^2\sin 2\theta - 2\sin 2\theta/r^1 - 2\cos 2\theta \end{cases}$$

$$-6\sin 2\theta/r^4 & 0 & -4\sin 2\theta/r^2 & 1/r^2 & 2 \\ 6\sin 2\theta/r^4 & f2r^2\sin 2\theta & 0 & -1/r^2 & 2 \\ 6\cos 2\theta/r^4 - 6r^2\cos 2\theta & 2\cos 2\theta/r^2 & 0 & 0 \end{cases}$$
(25)

The numerical integration required for computation of the H matrix (Eq. 11) is accomplished most conveniently in polar coordinates. However, computation of G (Eq.10) actually requires the cartesian surface tractions which correspond to the assumed-displacement field:

$$T = \{T_x T_y\} = N \{\sigma_{xx} \sigma_{yy} \sigma_{xy}\} = NP \beta$$
(26)

where β represents the vector of stress unknowns [1]. Hence, the following modification of Eq. 10 is required. Since

$$\mathcal{Z} = \{ \tau_{rr} \ \tau_{os} \ \tau_{ro} \} = \mathbf{P} \mathbf{B}$$
 (27)

in the present case, a Mohr circle transformation must be introduced:

and Sq. 10 is replaced by:

$$\mathbf{G} = t \int_{\mathbf{A}} (\mathbf{N} \mathbf{M} \mathbf{P})^{\mathsf{T}} \mathbf{L} \, d\mathbf{A} \tag{29}$$

where

$$\mathbf{M} = \begin{cases} \cos^2 \theta & \sin^2 \theta & -\sin 2\theta \\ \sin^2 \theta & \cos^2 \theta & \sin 2\theta \\ \frac{1}{2} \sin 2\theta & -\frac{1}{2} \sin 2\theta & \cos 2\theta \end{cases}$$
(30)

In Eq. 30, θ is the angular coordinate of the current integration station on ∂A . Thus, the price paid for convenience in choosing

 $P(r,\theta)$ is the slight amount of additional computation required to form M at each integration station, as the element boundary ∂A is swept in Eq. 29.

2.6 Transformation-Assembly Procedure

A complete set of stiffnesses for the near-field region can be obtained from a single element computation by means of a transformation-assembly sequence. Element number 1 in Figs. 8 and 9 is always assumed to be oriented with edge 61 along the positive x-axis. Eqs. 11 and 29 are integrated with Gauss-Lagrange quadrature (GLQ) formulas [8] to compute k_1 , which is then assembled into a near-field substructure in accordance with the global node numbering scheme in Fig. 9.

It is apparent that the stiffnesses for elements 3, 5 and 7 can be obtained by rotation transformation of k_1 . For example, element 3 is oriented at +90 degrees from element 1. Hence, the transformation:

$$\{q_1, q_2, \dots, q_{12}\}_{L^2} \mathbb{R} \{q_1, q_2, \dots, q_{12}\}_{G}$$
 (31)

relates the locally oriented displacements \underline{q}_{L} to the globally oriented displacements $\underline{q}_{G}\text{, where:}$

$$R = \begin{cases} \cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{cases}$$

$$\frac{\cos \theta}{-\sin \theta} & \cos \theta \end{cases}$$

$$(32)$$

$$(Super-diagonal)$$

$$\cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{cases}$$

An example for one pair of nodal displacements is illustrated in Fig. 9. Since strain energy is independent of any particular coordinate system, a global stiffness matrix for element 3 may be computed as follows:

Strain Energy =
$$\frac{1}{2} \mathbf{q}^{\mathsf{T}} \mathbf{k}_1 \mathbf{q}_1 = \frac{1}{2} \mathbf{q}^{\mathsf{T}} \mathbf{k}_3 \mathbf{q}_6$$
 (33)

Introducing Eq. 31 for g_L leads to

$$\mathbf{J}_{G}^{T} \overset{R}{\sim} \mathbf{k}_{1} \overset{R}{\sim} \mathbf{J}_{G} \overset{S}{\sim} \mathbf{J}_{G} \overset{L}{\sim} \mathbf{J}_{G}$$
(34)

for arbitrary values of $q_{\boldsymbol{G}}$. Therefore:

$$k_3 = R^{\dagger} k_1 R$$
 ; $\theta = \pi/2$ (35)

and in a similar manner,

$$k_5, k_7 = R^T k_1 R$$
; $\theta = \pi, 3\pi/2$ (36)

The sequence of rotation transformations given by Eqs. 35 and 36 assembly according to Fig. 9 is followed.

A stiffness matrix for element 2 can be obtained from k_1 by the reflection transformation illustrated in Fig. 10. If element 2 is considered relative to a reflected xy axis system, then its stiffness is identical to k_1 with the displacements oriented as indicated by the broken arrows. However, stiffness k_2 is wanted again with respect to q_G . It is evident from Fig. 10 that for this case:

$$\mathbf{1}_{L} = \mathbf{1}_{C} \mathbf{1}_{G} \tag{37}$$

where

$$\mathcal{R} = \begin{pmatrix} 1 & & & & \\ & -1 & & & \\ & & & -1 & \\ & & & & \mathcal{R}^T \\ & & & & \mathcal{R}^T \\ & & & & \mathcal{R}^T \end{pmatrix}$$
(38)

Applying the strain energy argument again then gives immediately:

$$k_{z} = A k_{z} A$$
(39)

After $\frac{1}{2}$ has been assembled, the procedure is completed with rotation transformations for:

$$k_4, k_1, k_2 = R^T k_1 R_1 ; \theta = \pi/2, \pi, 3\pi/2$$
 (40)

where R is given by Eq. 32. The transformation-assembly procedure has been programmed internally, and the final result may be thought of as a single element with 16 outer boundary nodes, 24 inner boundary nodes, and 64 total degrees of freedom. Figure 11 illustrates the numbering convention for the assembly, which will be referred to as HOLEL in subsequent discussion.

2.7 Performance Tests

Several performance tests were conducted, in addition to routine checking of inversion accuracy in the H matrix, in order to assess the capabilities of HOLEL. Although its primary function is to serve as a link between a few inner rings of quadrilaterals and a coarse far-field mesh, there is some interest in determining the solution accuracy for structures in which the inner boundary of HOLEL is stress-free. Errors are to be expected for this situation, since the assumed surface tractions N M P B generally do not vanish when P(r,0) is computed for points lying on the element boundary A. Errors of this type usually appear as overshoots in the computed stresses, given by [1]:

$$Z'(r,o) = P'(r,o) H'G Q_{L} = B'(r,o) Q_{L}$$
 (41)

where r,9 represent any point in the element domain A or on the boundary θA . Matrices $B_{1}(r,\theta)$ were computed during the formation of k_{1} for several points along a ray $\theta k_{2} = 27.5$ degrees in element 1 (Fig. 9) for the purpose of the test.

Figs. 13, 14 and 15 illustrate the results of a test series in which the dimensions of HOLEL are (see Fig. 17):

Hole Diameter $D_O = 2$ inches Edge Dimension W = 8 inches

The value W/D_O = 4 was chosen on the basis of a classical elasticity solution which indicates that far-field conditions are achieved tr/R_O = 4 for an open hole in an infinite plate [9]. The finite-element results computed from Eq. 41 are compared with the classical solution at θ = 22.5 degrees [7].

The effect of increasing the number of GLQ integration stations is studied in Fig. 13, which plots $r_{\rm dif}$. This stress component is the least sensitive to overshoot error because it does not enter into the stress-free condition on the inner circular portion of the boundary. The results show that 3 GLQ stations are too few, while acceptable accuracy is obtained with 4 or more stations. The programming of HOLEL was subsequently fixed at 5 GLQ stations based on these results. The meaning of "5 stations" is actually:

5 stations x 6 edges to compute 5 on R = 30

 5×5 stations to compute H in A = 25

Total GLQ integration stations = 55

This amount of computing is comparable to the amount required for the PCRK59 element.

Figures 14 and 15 illustrate the behavior of tr and tre, respectively. Finite-element results are shown only for 5 GLQ stations. These results demonstrate surprisingly that HOLES, is able to achieve the stress-free condition. However, some inaccuracy

can be observed at $r/R_G \cong 1.7$. The important conclusion to be drawn from this test series is that HOLEL can be used without interior elements to model a multi-fastener-hole structure for which, e.g., local stress distributions or K_T and K_{II} solutions are sought only at one fastener hole, or at some other location.

The second test series studied the performance of HOLEL as a function of the parameter W/D $_{\rm O}$, using the test problem illustrated in Fig. 12. Results for $v_{\rm H\, H}$ are plotted in Fig. 16. Some performance degradation is observed for W/D $_{\rm O}$ = 3, as the near-field stress gradients begin to appear in the far-field elements, which are incapable of following this behavior with complete accuracy. Considerable degradation is also seen for W/D $_{\rm O}$ = 8, a result which might be attributed to either the absence of far-field terms in P(r, H), or errors in computing G and H caused by shape distortion, or both. One may conclude from these results that limitations must be placed on the edge distance and centerline spacing in HOLEL models of multi-fastener structures.

The objective of the third test series was to study the accuracy of HOLEL for the case of combined interference-fit or bearing loads and panel tension. Two tests were conducted, in which additional loads were applied at the fastener hole boundary of the model shown in Fig. 12. In Fig. 17, results for $\tau_{\rm rr}$ are plotted for the case of 1 ksi panel tension combined with 1 ksi uniform pressure to represent an interference fit. A curve faired through the computed stresses extrapolates to -1.07 ksi at the fastener hole boundary, i.e., an error of about 7 percent. In

Fig. 18, results for τ_{rr} are plotted for 1 ksi panel tension combined with a bearing pressure distribution given by:

$$\gamma_{0}(\theta) = \frac{2P}{\pi R_{0}} \sin \theta ;$$

$$P = \theta_{0} \cos Ab. , \quad 0 \le \theta \le \pi$$
(42)

Eq. 42 gives

$$T_{rr} = -p(\theta) = -1.95 \text{ ksi}$$
 (43)

at θ = 22.5 degrees. In this case, a curve faired from 11 computed stresses extrapolates to the exact value at the fastener hole boundary. It is apparent from these results that HOLEL is accurate for both interference-fit and bearing loads. In the former case, the results could have been improved by computing $\tau_{\rm rr}$ at 11 locations instead of the 5 which had been used. Farfield element stresses were also checked for this test series. In the case of interference-fit, the computed values for cartesian stress in the far-field elements were $\sigma_{vv} = 1$ ksi and $\sigma_{xx} = \sigma_{vv} = 0$ (to the roundoff level of the computer), with very little disturbance. In the case of bearing, it must be recognized that the 8,000-lb. bearing lcad adds to the 16,000-lb. panel tension load (1 ksi x 16inch edge) for the far-field elements below the fastener hole. The computed stresses were in fact σ_{vv} = 1 ksi for the upper elements, $\sigma_{yy} = 1.5$ ksi for the lower elements, and $\sigma_{xx} = \sigma_{xy} = 0$, with load-transfer effects appearing in the far-field elements adjacent to HOLEL.

In the fourth test series, four rings of quadrilateral and PCRK59 elements were added to the structure model with the outer ring coupled to the circular boundary of HOLEL. Two test cases were analyzed. In the first case, the ring consisted entirely of quadrilaterals, and a cosine bearing pressure distribution (Eq. 42) was applied at the free boundary of the innermost ring. Figure 19 plots the results for $\tau_{\rm rr}$ computed at the centroids of one "slice" of four quadrilaterals, along a ray at $\theta=97.5$ degrees. The faired-curve extrapolation of these four data points agrees well with

$$T_{rr} = -\gamma p(97.5^{\circ}) = -\frac{2P}{\pi R_{o}} \sin(97.5^{\circ}) \stackrel{\sim}{=} -25.2 \text{ ksi}$$
 (44)

In the second case, one or two groups of four quadrilaterals were replaced by PCRK59 elements to simulate a fastener hole with a crack at θ = 0 or two equal-length cracks at θ = 0, π . Several cases were analyzed covering the parameter ranges:

Hole diameter/HOLEL Edge: $0.02 < D_I /W < 0.05$ HOLEL edge/HOLEL diameter: $W/D_O = 4$

Crack length/hole radius: $0.25 < a/R_{\rm I} < 1.0$ Table 1 compares the computed K_I values with independent classical solutions [10, 11]. The results demonstrate that the finite-element model is capable of providing reasonably accurate K_I solutions for quite extreme geometries (small fastener hole in a large panel).

The final test series consisted of a number of demonstration runs of the complete PANEL program, in which $\mathbf{K}_{\mathbf{I}}$ and $\mathbf{K}_{\mathbf{I}\mathbf{I}}$ solutions

were computed for another range of W/D values. These results are presented in Section 5, following the documentation of the HOLEL procedure and the PANEL program.

Section 3

HOLEL PROCEDURE

Due to the complexity of the model, HOLEL has been programmed as several interrelated subroutines. Subroutine HOLEL provides overall control of the stiffness generation-assembly-transformation procedure, calling upon subroutines QHOLEL, GMTRX, HMTRX, LMTRX, MNMTRX, PMTRX and TRIG to execute specific computational tasks. In addition, HOLEL uses some of the FEABL-2 software [6] for the assembly process.

3.1 Structure Model and Input/Output Conventions

A square near-field region with an inner circular boundary of radius R_O is modelled. The numbering conventions have been indicated in Fig. 11. Subroutine HOLEL is invoked by:

CALL HOLEL (COORD, THK, S, RI, RSS, ISS, B)

where the arguments are dimensioned and defined as follows:

- COORD(12) Vector of cartesian coordinates of the

 element corners in order X₁,Y₁,Z₁,X₂,...,

 Z₄. (In the present version, the element
 is assumed to lie in the XY plane, and the
 Z coordinates need not be given any values.)
- THK Scalar value of element thickness.
- S(3,3) Array of elastic compliance constants for
 homogeneous isotropic material, i.e.:

$$S = \frac{1}{E} \begin{bmatrix} 1 & -\nu & 0 \\ -\nu & 1 & 0 \\ 0 & 0 & 2(1+\nu) \end{bmatrix}$$
 (45)

RI - Scalar value of inner boundary radius R_O.

RSS(2097),- Floating-point and fixed-point names of a

ISS(2097) FEABL-2 DATA vector. These arguments must
be equivalenced, as well as dimensioned in
the user's MAIN program.

B(6,3,13) - A collection of B matrices for stress analysis (see Subsection 3.2).

HOLEL returns the assembled subregion stiffnesses as a variable-bandwidth-stored matrix in the DATA vector RSS,ISS. The results may be read into another storage area with the algorithm given in Appendix A, or may be assembled directly into another DATA vector with FEABL-2 subroutine ASMSUB (see Subsection 2.2). Procedure HOLEL requires no input data cards.

3.2 Required Subprograms and Other Features

Procedure HOLEL requires the following additional software for execution:

- 1. ASRL FEABL-2 subroutines ASMLTV, ORK and SETUP.
- 2. IBM Scientific Subroutine Package subroutines MFSD and SINV.

No external disk or tape files are required.

3.3 Model Generation and Program Flow

Figure 20 summarizes the program flow in Procedure MOLEL.

At entry, whatever control parameters are present in the FEABL-2
labelled COMMON areas SIZE, BEGIN and END are saved in temporary
storage. Subroutine SETUP is called to establish address control
for the RSS,ISS vector for a structure model with 64 total degrees
of freedom, consisting of the eight 12-degree-of-freedom elements
in Fig. 9. Element interconnections are then generated internally,
in accordance with the numbering conventions in Fig. 8 and Fig. 11,
and subroutine ORK is called to compute the band margin and complete
address control for the assembled stiffness matrix.

Subroutine QHOLEL is now called to compute k_1 , the stiffness matrix for element 1. This subroutine calls in turn subroutines HMTRX and GMTRX to compute H^{-1} and G, forms the stiffnesses $G^TH^{-1}G$. Subroutines HMTRX and GMTRX loop over the GLQ integration stations in the element domain A and on ∂A respectively, calling upon subroutines TRIG, PMTRX, LMTRX and MNMTRX to compute $P(r,\theta)$, L(A) and M^TN^T at each station, and accumulating the product sums (including GLQ weighting factors) for P^TSP and $(NMP)^TL$. Subroutine HMTRX calls SINV (which calls MFSD) to invert H.

After k_1 has been completed, subroutine QHOLEL forms a 6x3x13 matrix for stress analysis, consisting of six matrices $B(r,\theta)$ as given by Eq. 41, and stored in accordance with the following conventions:

$$\mathbf{B}(\mathbf{I},\mathbf{J},\mathbf{K}) = \left(\begin{array}{c} \mathbf{B}_{i} \left(r_{i}, \theta_{i} \right) & \begin{array}{c} \theta_{i} \\ r_{i} \end{array} \right)$$
 (46)

where subscript I identifies the specific B matrix, and where

$$\theta_i = \pi/\theta$$
 ; $i=1,2,\dots,6$
 $\Gamma_i = R_o$ (47)

 $\Gamma_i = \Gamma_{i-1} + 0.2$ (distance from R_o to outer boundary along θ_i); $i=2,3,\dots,6$

Thus, the B matrices refer to six locations which divide the ray $\theta = \pi/8$ into five equal segments, with B₁ located on the inner circular boundary and B₆ located on the near/far-field boundary. Polar stresses for these locations can be computed from:

$$\{\tau_{rr} \ \tau_{\theta\theta} \ \tau_{r\theta}\}_{i} = STRESS(J)_{I} = \sum_{K=1}^{12} B(I,J,K)^{*} Q(K)$$
 (48)

where

$$Q(K) = \mathbf{F}_L \tag{49}$$

An extra column (K=13) is appended to each B matrix for storage of the polar coordinates of its location.

At this point, subroutine MOLEL regains control and executes the transformation-assembly process outlined in Subsection 2.6. In the program, $\frac{k}{2}$ is formed first, and the assembly sequence is programmed as:

Assembly of k_1 and k_2 Rotation through $\pi/_2$ to k_3 and k_4 Assembly of k_3 and k_4 Rotation through π to k_5 and k_6

Assembly of k_7 and k_8

Finally, the HOLEL address control parameters are transferred to the FEABL-2 labelled COMMON areas SIZESS and BEGSS, and the user's control parameters are returned to areas SIZE, BEGIN and END. Control is now returned to the user's calling program, with HOLEL ready for assembly to the user's structure model by means of FEABL-2 subroutine ASMSUB.

3.4 Procedure Status

All of the HOLEL subroutines, together with copies of IBM subroutines MFSD and SINV, are maintained as a unit in the form of individually sequenced, 029-punched FORTRAN-IV source decks. A listing of Procedure HOLEL appears in Appendix B.

Section 4

PANEL PROGRAM

The PANEL program is an executive program which controls the assembly of several substructures into a model of a skin tension panel with a single open fastener hole. The PANEL program uses procedure HOLEL and several additional special-purpose procedures to generate the required substructures. Details of these additional procedures are discussed in Subsections 4.2 and 4.3.

4.1 Structure Model and Input Conventions

Figure 21 illustrates the structure which the PANEL program models: a rectangular panel loaded by uniform tension on its horizontal edges. The panel contains a single fastener hole centered vertically. The fastener hole may be either centered or offset horizontally. The vertical edges of the panel may be stiffened symmetrically with integral stiffeners, if desired. One or two cracks may be placed to emanate radially from the fastener hole. If two cracks are specified, they will be located 180 degrees apart, and they may be of equal or unequal length. The angular position, 0, to the first crack may be varied in 15-degree increments from 0 to 345 degrees if there is only one crack, or from 0 to 165 degrees if there are two cracks. A second version of the PANEL program is available for a structure in which only the left edge may be stiffened. The second version

is otherwise similar to the first version, and will not be discussed separately.

Four input data cards are required for the PANEL program. The input data describe the specific panel geometry and define several parameters which control the type of solution executed and the amount of information printed. Figure 22 illustrates the correct format for the input cards:

1. Panel parameters

WIDTH = Total width of the panel, W_{22} .

LENGTH = Total length of the panel.

THK = Panel thickness.

STFFCT = Stiffener factor.

PRESS = Tension loading, σ_{VV} .

RI = Radius of the fastener hole.

IOFFST = Offset indicator.

2. Crack parameters

A(1) = Length of first crack.

A(2) = Length of second crack.

IPOS(1) = Crack initial position number

IPOS(2) = Crack final position number.

3. Material properties

E = Young's modulus.

v ≈ Poisson's ratio.

4. Print control parameters

KTl = Control for optional FEABL-2 output.

KT2 = Control for optional FARFLD output.

KT3 = Control for optional RING output.

The stiffener factor is defined in terms of the panel dimensions (Fig. 21):

$$STFFCT = W_r t_r / W_p t_p \tag{50}$$

The value STFFCT = 0 corresponds to an unstiffened panel. Negative values may be used to analyze panels with edges thinner than the primary structure. The offset indicator is used to control the type of solution desired. The following options are available:

IOFFST = 0 - Centered fastener hole only.

IOFFST = 1 - Fastener hole moves right.

IOFFST = -1 - Fastener hole moves left.

For the latter two options, solutions are executed automatically beginning with the hole on center and ending with the hole as close to the edge of the panel as permitted by the finite-element model. If STFFCT \(\neq 0 \), motion of the hole is further restricted to avoid overlapping with a stiffener.

A value of 0 should be assigned to crack length A(2) if a structure with only one crack is to be analyzed. Crack sizes up to 1.27 (RI) are permitted. The crack position numbers control the angular location of the first crack as follows:

$$\theta_{initial} = (IPOS(1)-1) \Delta \theta$$

$$\theta_{final} = (IPOS(2)-1) \Delta \theta$$

$$\Delta \theta = W/12 \text{ rad.} = 15 \text{ deg.}$$

Permissible limits for the position numbers are:

 $1 \le IPOS(1) \le n_{max}$ $IPOS(1) \le IPOS(2) \le n_{max}$ (52)

where

$$n_{\text{max}} = 24 \text{ if } A(z) = 0$$

 $n_{\text{max}} = 12 \text{ if } A(z) \neq 0$ (53)

Solutions are executed automatically beginning with the first crack in position 1 and ending with the first crack in position 2. A single solution is executed if IPOS(2) = IPOS(1). A case matrix is executed if ICFFST ≠ 0 and IPOS(2) > IPOS(1).

Most of the routine information printed by the PANEL program is of no interest when production runs are executed. This information may be deleted from the output by assigning each of the control parameters KT1, KT2, KT3 values equal to the FORTRAN unit number for the line printer at the user's computing facility.* Any other value permits full output by the associated software. Pull output is recommended for initial testing of the program at a new facility. Output from FARFLD and RING should be allowed whenever a new range of panel disensions is tried.

4.2 Required Subprograms and Other Features

The PANEL program requires the following additional software for execution:

^{*}The same value used in a print instruction, e.q., WRITE (6,1000) A.B.C. The FORTRAN unit number in this case is 6.

- ASRL FEABL-2 subroutines ASMLTV, ASMSUB, BCON, FACT, ORK, QBACK, SETUP, SIMULQ, STACON and XTRACT.
- IBM Scientific Subroutine Package Subroutines MFSD and SINV.
- 3. ASRL procedures FARFLD, HOLEL and RING, with included subroutines.
- 4. ASRL elements PCRK59 and QUAD4.

No external disk or tape files are required. The program must be able to communicate with the user's facility card reader and line printer, by means of two instructions near the beginning of the program:

KR = Card reader FORTRAN unit number.

KW = Line printer FORTRAN unit number.

The program is supplied with IBM-standard values KR=5 and KW=6.

4.3 Model Generation and Program Flow

The panel structure model is created via several levels of substructuring to minimize repeated processing of unwanted degrees of freedom. Figure 23 illustrates the general hierarchy of the finite-element model. Procedures FARFLD and RING generate the two major components which are finally assembled to form the complete structure.

Procedure FARPLD creates the far-field region, consisting of upper and lower rectangular substructures generated by procedure LUG,* and a center-zone substructure generated by

^{*}Different from the attachment lug procedure reported in Ref. 1.

procedure CZONE. Procedure LUG assembles a regular mesh of QUAD4 elements and eliminates all except the upper-edge and lower-edge nodes. Procedure CZONE assembles HOLEL together with right and left portions modelled with QUAD4 elements, and eliminates all but the upper- and lower-edge nodes and the inner circular boundary nodes. Procedure FARFLD assembles the LUG and CZONE components and executes additional Gauss elimination to produce one of two major substructures:

- 1. "Panel-and-Hole", in which only the nodes along the top and bottom edges of the panel and the nodes along the inner circular boundary remain as boundary nodes in the statically condensed structure. Displacement restraints are applied at the bottom edge and nodal forces are applied at the top edge to represent uniform tension.
- 2. "The Chashire Cat": a panel-and-hole with top and bottom edges eliminated by static condensation (nothing remains but the smile).

Only the Cheshire Cat option is used by the PANEL program. Numbering conventions for the FARFLD compenents are illustrated in Figs. 24, 25 and 26.

Procedure RING creates an inner cracked ring for assembly inside the Cheshire Cat. The ring consists of two 150-degree arcs and two 30-degree segments which contain QUAD4 and PCRK59 elements. The arcs are assembled by procedure ARC4, which also

removes all interior nodes by static condensation. Procedure RING assigns the angular locations of the components to obtain the required crack positions, and determines where each PCRK59 element is to be placed in the 30-degree segments according to the crack sizes A(1), A(2). Finally, procedure RING assembles and statically condenses the cracked ring to produce one of two major substructures:

- Ring with all but inner and outer circular boundary nodes eliminated.
- 2. Ring with all but outer circular boundary nodes eliminated.

Retention of the inner boundary nodes is useful for cases in which bearing or interference-fit loads are to be applied at the fastener hole. The outer boundary nodes must be retained for coupling with the Cheshire Cat. The PANEL program uses only the second option. Numbering conventions for the RING components are illustrated in Figs. 27 through 30. Procedure RING always generates a ring with an outer/inner diameter ratio of 2.52 to maintain shape conformity for the QUAD4 elements.

Figure 31 illustrates the executive flow in the PANEL program. After the problem input data have been read and printed and some parameters have been calculated for control of the various procedures, two major loops appear. The outer loop begins with the creation of a Cheshire Cat, a step which must be repeated each time the fastener hole is offset to a new position. This is followed by address control and interconnection generation for

the final structure, which will be assembled from the Cheshire Cat (super-element 1) and the cracked ring (super-element 2). The interconnection algorithm is actually completed inside the inner loop to allow the band-margin computations (Subroutine ORK) to erase the K and g data from the previous pass. The remainder of the inner loop consists of assembly of the Cheshire Cat, generation and assembly of the cracked ring, global solution (subroutines FACT and SIMULQ), a back-substitution to obtain g_L for the cracked ring substructure and finally, extraction of the PCRK59 displacements from g_L and computation of K_I and K_{II}. The ends of the inner and outer loops are governed by incrementation of the crack angle and hole offset, respectively, and logical checks to determine whether the prescribed ranges of these parameters have been swept.

4.4 Output Conventions and Error Messages

Figure 32 illustrates a sample output from the PANEI program (version 2, left side stiffened). The output from Version 1 is similar. The heading identifies the program version and repeats the user's input data. Below the material properties data appears a table of $K_{\rm I}$ and $K_{\rm II}$ solutions for one or two cracks, together with their angular positions. The $K_{\rm I}$ and $K_{\rm II}$ values are NASA/ASTM standard stress intensities in units of psi $\sqrt{\rm in}$, assuming that the input data was specified in corresponding engineering units of psi for loading and Young's modulus and inches for dimensions. The sample output is an example of the production information obtained by exercising the three options for deletion of debugging output.

Besides the FEABL-2 software error messages [6], the following diagnostics may result from the PANEL programs. In procedure RING, the length specified for each crack is checked to insure that the crack tip does not extend beyond the average radius of the outermost ring of quadrilaterals, i.e.:

$$R_{\rm Z} + A(T) \le \frac{i}{2} (R_4 + 2.52R_{\rm Z}); \quad \mathcal{J}=1,2$$
 (54)

where R₄ is the inner radius of the outermost ring. If Eq. 54 is violated, a message is printed and program execution is terminated. This condition is somewhat conservative, since it restricts the crack tip to a position mid-way in the PCRK59 element. Eq. 54 may be replaced by:

$$R_{I} + A(I) \leq 0.3R_{4} + 0.7 \times 2.5 \times R_{I}$$
 (55)

to permit the crack tip to approach somewhat closer to the outer bourdary. In procedure CZONE, a check is made to insure that the fastener hole offset is within allowable limits. This is done by monitoring the node number of the fictitious center reference node (see Fig. 25). Excessive offset causes an error message and program termination.

4.5 Program Status

Both versions of the PANEL program have been exercised successfully for all analysis options, and are maintained as

sequenced, 029-punched FORTRAN-IV source decks. Either version requires 260 to 300 KBYTES (65,000₁₀ to 75,000₁₀ words, or 176,750₈ to 222,370₈ words) of core memory and approximately 0.8 to 1.0 CPU minute, depending upon the ranges of the hole offset and crack angle parameters. Storage and time statistics are based on runs made on an IBM S-370/168 machine, using the IBM FORTRAN-G1 and FORTRAN-H compilers. Version 1 (symmetrical edge stiffeners) is listed in Appendix C. Version 2 (left edge stiffener only) is listed in Appendix D.

Section 5

DEMONSTRATION EXAMPLES

A number of example analyses have been run to verify the PANEL program code and simultaneously to explore the accuracy of the analysis for a range of panel and crack dimensions wider than considered in the HOLEL performance tests. The solutions given here focus mainly on panels with centered fastener holes having cracks at $\theta=0$, π because there exist no independent solutions with which to compare other configurations.

Figure 33 illustrates the coarsest model possible to generate from the PANEL program: lugs consisting of two elements each and a center-zone composed only of HOLEL. Also, the dimensions chosen are such that the fastener hole is no longer small compared to the panel, and since the outer/inner diameter ratio of the cracked ring is 2.52, the HOLEL shape parameter in this case is:

$$W/D_0 = 4/2.52 \approx 1.59$$

a point well outside the range studied in the HOLEL performance tests. The butterfly plots for $K_{\rm I}$ and $K_{\rm II}$ shown in Fig. 33 illustrate an error effect caused by proximity of the displacement boundary conditions to the region of interest. In the present case, the restraints are only two elements away from the "action" (a lug QUAD4 and the HOLEL) when either crack lies below the

horizontal. The error is most pronounced for K_{II} at θ = 225, 315 degrees. The error would be more pronounced as θ + 270 degrees, except that the solution tends rapidly to zero in this region. A similar but less-pronounced effect can be observed in the plot for K_{I} . Comparison of K_{I} for θ = 0, 180 degrees with an independent solution [10, 11] provides a more welcome result. Indeed, it is quite surprising that this very crude finite-element model is able to faithfully reproduce the classical solution. The general conclusion to be drawn from this test is that only the upper half of the butterfly plot may be trusted when running models with very few elements in the FARFLD substructure.

Figures 34 and 35 illustrate two runs in which the panel and crack dimensions have been varied to explore the effect of W/n_o. Also, the aspect ratios of the elements in the LUG substructure were changed to allow more elements between the restrained bottom edge and the center-zone. The latter modification has eliminated the restraint error effect. Table 2 summarizes the comparisons of results from Figs. 33 through 35 with the independent solution, showing that reasonable accuracy has been achieved over:

The greater error for the middle case remains an unexplained anomaly.

Figure 36 illustrates the $K_{\rm I}$ and $K_{\rm II}$ solutions obtained for a panel of the same dimensions, hole radius, etc. shown in Fig. 35, but with the hole offset to the maximum amount permitted in

the model, a distance of 1.5 inches. Increases of the order of 5 to 10 percent are observed for $K_{\rm I}$, with the greatest increase at crack tips which are located nearest to the edge of the panel.

Figures 37 through 39 present results for some additional studies of the basic panel shown in Fig. 35 to illustrate the stiffening options. A stiffener factor of 0.5 was used for these analyses, i.e., the added cross section area of each stiffener was 50 percent of the panel cross section area. Figure 37 plots $K_{\overline{1}}$ and $K_{\overline{1}\overline{1}}$ solutions for a symmetrically panel. Results are shown for the fastener hole stiffened centered and offset by 1 inch. There is very little difference between the two solutions. Solutions for a panel with left-edge stiffener and a centered fastener hole are plotted in Fig. 38. The results for K_{T} and K_{TT} appear to be symmetrical. In fact, very little difference can be observed between the unstiffened, symmetrically stiffened and asymmetrically stiffened panels (compare Figs. 35, 37 and 38). Some difference is noted when the fastener hole is offset 1.5 inches to the right, away from the stiffened edge. Figure 39 presents the results for this case, which are almost identical to the results for an unstiffened panel (compare with Fig. 36). The tentative conclusion from these results is that edge stiffeners and moderate offsets do not appreciably affect K_{T} and K_{TT} for cracks at the fastener hole, at least for uniform tension loading and when the hole and crack are not extremely close

to an edge or stiffener.

Figure 40 summarizes the dimensional information for a panel model used to study a broad range of $a/R_{\rm I}$ ratios with $W/D_{\rm O}$ fixed at 1.59. Table 3 summarizes the results for a series of cases with equal-length cracks at $\theta=0,\pi$. These may be compared directly with handbook data because the dimensions of the model correspond precisely with a published curve. The results are seen to be quite reasonable over the entire range:

$$0.05 \le a/R_T \le 1.25$$

Indeed some of the error indicated in the table may be attributed to inaccuracy in reading the handbook chart. A number of other cases for a single crack at $\theta=0$ and for two unequal-length cracks are compared with the foregoing results in Table 4. Complete butterfly plots of the K_I and K_{II} data computed from these runs will appear in a later report.

Section 6

CONCLUSIONS

This report has traced the development of a parametric finite-element analysis program for computation of Mode I and Mode II stress intensity factors in stiffened and unstiffened panels with cracks emanating from centered and offset fastener holes. Early attempts to model the structure entirely with conventional elements, except for the crack-tip element and a few mesh-expander elements, proved to be unsuccessful. Test runs of these types of finite-element models quickly demonstrated that asymmetric grading of the mesh was forced by the need to accommodate an offset hole and at the same time to keep the size of the model within economic bounds. The asymmetric mesh was found to give extremely poor results for computed displacements in regions of low stress gradient, and was therefore abandoned.

The assumed-stress hybrid method was called upon once again, this time to provide a special element which could handle the transition from circular geometry near the fastener hole to the cartesian geometry natural to the rest of the panel. As finally developed, the hybrid element occupied a 45-degree sector between its inner (circular) and outer boundary. Airy stress functions from classical elasticity solutions near a hole in an infinite plate were used to provide the assumed stress field. The new

element allowed a much cleaner, more economical finite-element mesh to be designed, while at the same time providing accurate computations near the fastener hole. Performance tests have shown that the element is capable of occupying a stress-free fastener hole boundary directly, and of accepting interferencefit and cosine bearing loading on the fastener hole surface. Additional tests demonstrated that conventional quadrilateral elements could be coupled in rings inside the inner boundary of the new hybrid element, with no loss of accuracy. Some tests were also conducted with hybrid crack-containing elements replacing some of the quadrilaterals. These tests demonstrated that stress intensity factors could be computed to within a few percent of the values given by well-established independent solutions based on classical methods. In the final phase of the project, a parametric program was developed and verified for analysis of tension panels in the various configurations mentioned above. During the verification tests, the hybrid fastener hole-ring combination was subjected to a variety of dimensional and shape parameters to further extend the range of measured performance. The results of these tests have demonstrated that the panel program is capable of computing stress intensity factors to within 5 percent or better for fastener hole and crack sizes found in current airframes.

The many example results presented in this report are still a rather limited data base, when compared with the number of stress

intensity factor solutions needed for a comprehensive designer's handbook. Some additional data, which were generated in the final verification tests but not included in this report, will appear in a later report in this series. However, further verification tests are still required to broaden the range of applicability of the panel program. One concern which has not yet been answered is how close a row of fastener holes may be spaced, or how near may a fastener hole approach the edge of a panel, before the finite-element model experiences unacceptable degradation of accuracy. The data generated thus far seem to indicate that there will be a limit in this respect, and that the limit may be severe. Addition of mid-edge nodes to the edges which span between the hybrid fastener hole element's inner and outer boundaries may permit closer spacing, but will also require additional terms in the assumed stress field.

Another continuing concern is associated with the verification process itself. The combination of crack-containing and fastener hole elements gives the capability to compute $K_{\rm I}$ and $K_{\rm II}$ for so many varied configurations that the numerical analyst finds himself sailing in uncharted waters. At the present time, parametric codes like the panel program can only be calibrated against classical solutions for $K_{\rm I}$ at one or two data points, while they may compute as many as 100 data points each for $K_{\rm I}$ and $K_{\rm II}$.

REFERENCES

- Orringer, O., "Fracture Mechanics Analysis of an Attachment Lug", Aeroelastic and Structures Research Laboratory, MIT, ASPL TR 177-1, AFFUL-TR-75-51, December 1974.
- Lasry, S.J., "Derivation of Crack Element Stiffness Matrix by the Complex Variable Approach", Aeroelastic and Structures Research Laboratory, MIT, ASRL TR 170-2, AFOSR-TR-73-1602, February 1973.
- Lin, K.Y., Tong, P. and Orringer, O., "Effect of Shape and Size on Hybrid Crack-Containing Finite Elements", to be presented at ASME Pressure Vessels and Piping Conference, San Francisco, California, June 1975.
- Luk, C.H., "Assumed Stress Hybrid Pinite Element Methodology for Fracture Mechanics and Elastic-Plastic Analysis", Aercelastic and Structures Research Laboratory, MIT, ASRL TR 170-1, December 1972.
- Tong, P., Pian, T.H.H. and Lasry, S.J., Int J Num Meth Eng, Vol. 7, pp. 297-308 (1973).
- 6. Orringer, O. and French, S.E., "FRABL (Finite Element Analysis Basic Library) User's Guide", Aeroelastic and Structures Research Laboratory, MIT, ASRL TR 162-3, AFOSR-TR-72-2228, August 1972. (Supplemented by ASPL TM 162-3-1 and ASRL TM 162-3-4, February 1974.)
- Dally, J.W. and Riley, W.F., Experimental Stress Analysis, McGraw-Hill, 1964.
- Abramowitz, M. and Stegun, I.A. (ed.), Handbook of Mathematical Functions, National Bureau of Standards, U.S. Dept. of Commerce, Nature Ed., November 1970.
- 9. Timoshenko, S. and Goodier, J.N., Theory of Elasticity, McGraw-Hill, 1961.
- 10. Paris, P.C. and Sih, G.C., "Stress Analysis of Cracks", ASTM STP 381, Fracture Toughness Testing and Its Applications, 1965, pp. 30-83.
- 11. Tada, H., Paris, P.C. and Irvin, G.R., The Store Analysis of Cracks Handbook, DEL Research Corporation, Hellertown Pa., 1971.

The second of th

TABLE 1

COMPARISON OF CLASSICAL AND FINITE-ELEMENT
FRACTURE MECHANICS SOLUTIONS

Number of Cracks	Crack Size, a (in.)	Hole Radius, R _I (in.)	a/R _T	K _I (ps Exact	i√in.) FEM	% Error
2	0.04	0.08	0.5	650	630	3.0
ī	0.04	0.10	0.4	660	675	2.4
2	0.38	0.10	0.8	792	771	2.7
2	0.05	0.20	0.25	910	910	
2	0.20	0.20	1.0	1150	1170	1.9

TABLE 2

COMPARISON OF CLASSICAL AND FINITE-ELEMENT
RESULTS FROM THREE DEMONSTRATION EXAMPLES

(Fastener hole with 2 cracks)

Case	Fig.	Crack Size (in.)	Hole Rad. (in.)	a/R _I	m/d ^o Holel	K (psir)	n) s 4 Error
1	3.3	0.3	0.5	0.6	1.59	19.9 1909	0 1.0
2	34	0.125	0.25	0.5	3.17	1001 113	4 4.1
3	35	0.125	0.125	1.0	6.35	886 886	7,0

(Structure model in Fig. 40; cracks at $\theta=0,\pi$.)

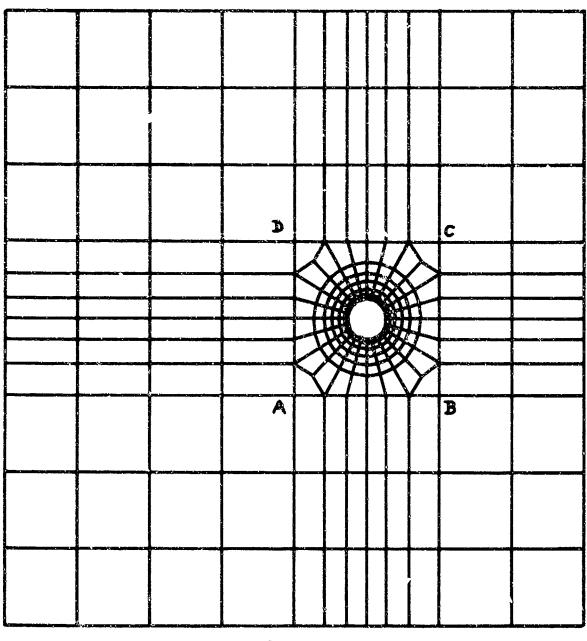
a(in.) and	K_{τ} (psi	8	
a/R _I	K _Ţ (psi Exact*	FEM	Error
0.05	1144	1160	1.4
0.1	1673	1613	3.6
0.2	2037	2051	0.7
0.4	2474	2445	1.2
0.6	2735	2715	0.7
0.8	2973	2897	2.6
1.0	3257	3099	4.9
1.2	3521	3401	3.4
1.25	3588	3500	2.5

^{*}Ref. 11, p. 19.4, curve marked h/b=2, R/b=0.25.

TABLE 4 $\label{eq:ADDITIONAL TEST OF a/R} \text{ADDITIONAL TEST OF a/R}_{\text{I}} \text{ RATIO}$

(Structure model in Fig. 40; one crack or two unequal cracks.

a(in.) θ=0	and a/R_{I}	K _I (psi	$\sqrt{\text{in.}}$) at $\theta=0$ ct (from Table 3)	% Difference
0.05	· ·	1155	1144	1.0
0.1		1600	1673	4.4
0.2		2000	2037	1.8
0.4		2302	2474	6.9
0.6		2466	2735	9.8
0.8		2522	29 73	15.2
1.0		2602	3257	20.1
1.2		2758	3521	21.7
1.25		2813	3588	21.6
0.05	1.25	1.447	1144	26.5
1.25	0.05	2824	3588	21.3



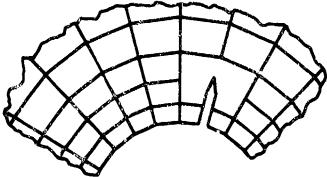


FIG. 1 CONVENTIONAL FINITE-ELEMENT MODEL OF PANEL WITH OFFSET FASTENER HOLE

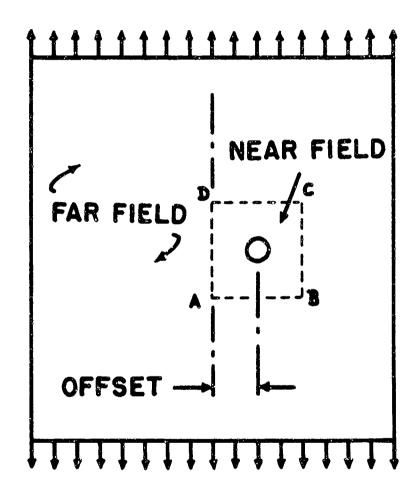


FIG. 2 SUBDIVISION OF PANEL INTO NEAR-FIELD AND FAR-FIELD REGIONS

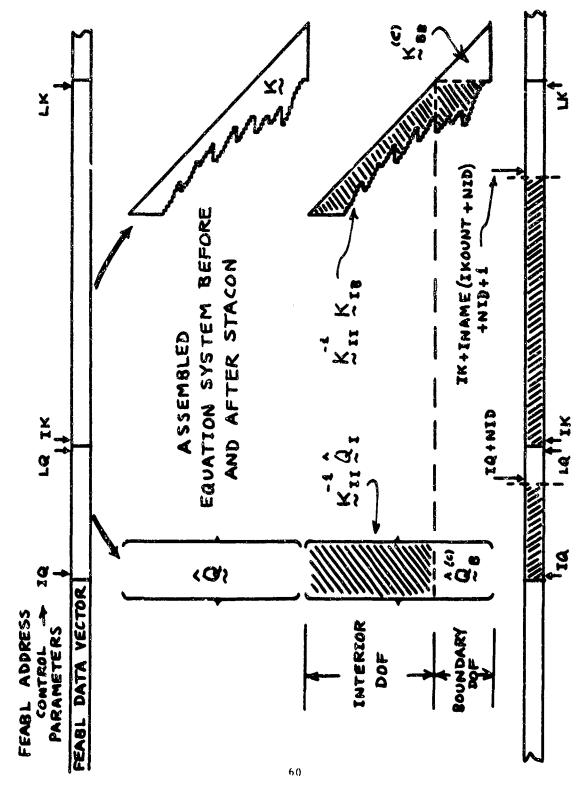
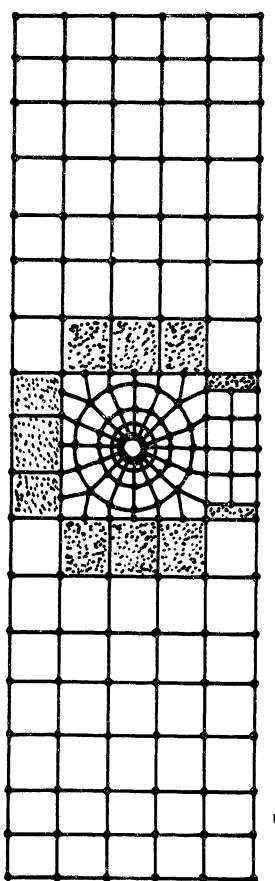


FIG. 3 ACTION OF FEABL-2 SUBROUTINE STACON ON ASSEMBLED SUBSTRUCTURE STIFFNESS MATRIX





376 Degrees of Freedom

FIG. 4 PLOT OF CONVENTIONAL FINITE-ELEMENT PANEL-AND-HOLE MODEL TESTED FOR NUMERICAL ACCURACY

UNDEFORMED VERTICAL EDGES AFTER DEFORMATION ILLUSTRATION OF FIG. 5 INACCURATE DIS-PLACEMENT SOLUTION CAUSED BY ASYMMETRIC MESH GRADING

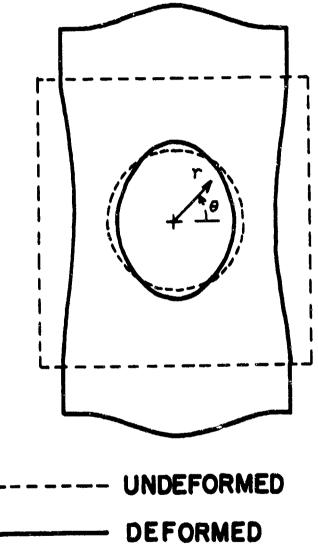
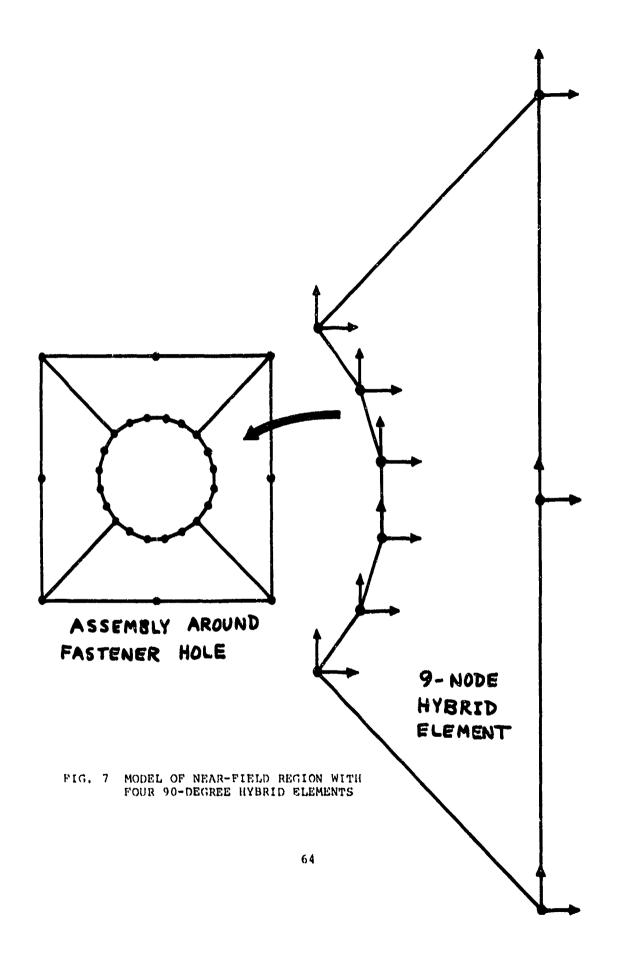
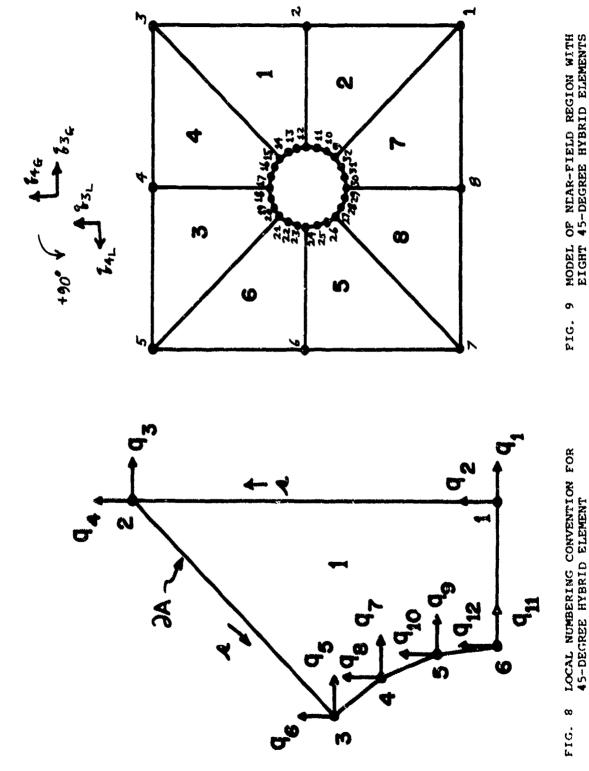


FIG. 6 EXPECTED DEFORMATION BEHAVIOR OF NEAR-FIELD REGION





LOCAL NUMBERING CONVENTION FOR 45-DEGREE HYBRID ELEMENT FIG. 8

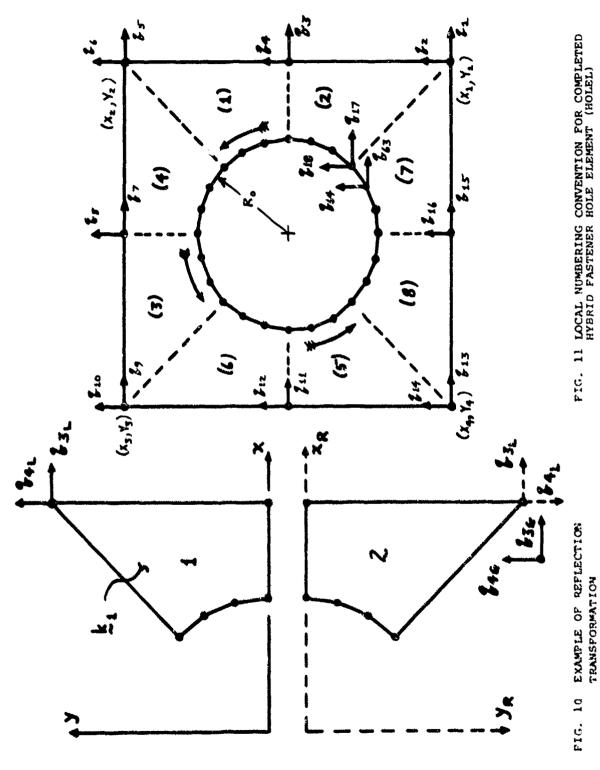


FIG. 11 LOCAL NUMBERING CONVENTION FOR COMPLETED HYBRID FASTENER HOLE ELEMENT (HOLEL)

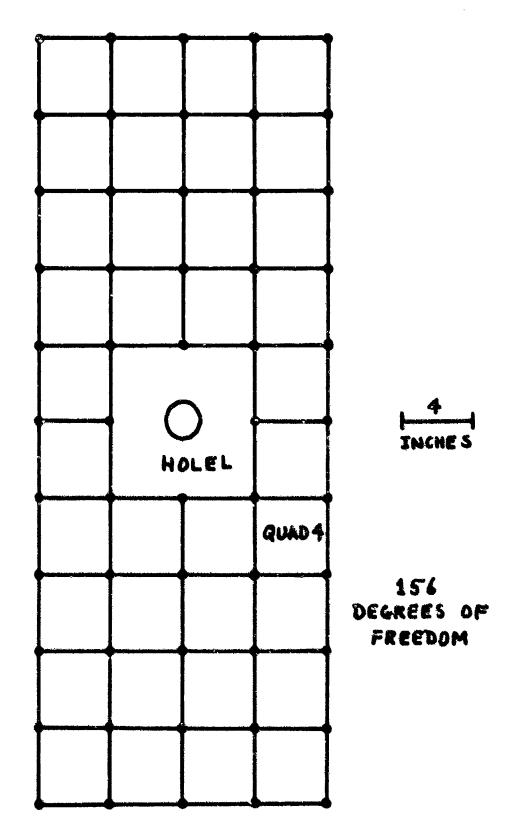
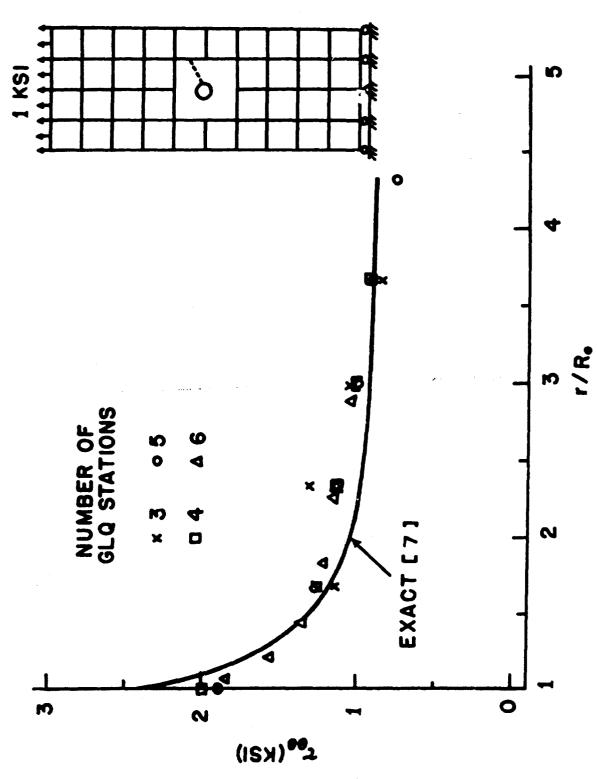


FIG. 12 FINITE-ELEMENT MODEL FOR PERFORMANCE TESTING OF HOLEL



PIG. 13 SENSITIVITY OF HOLEL TO NUMBER OF GLQ INTEGRATION STATIONS

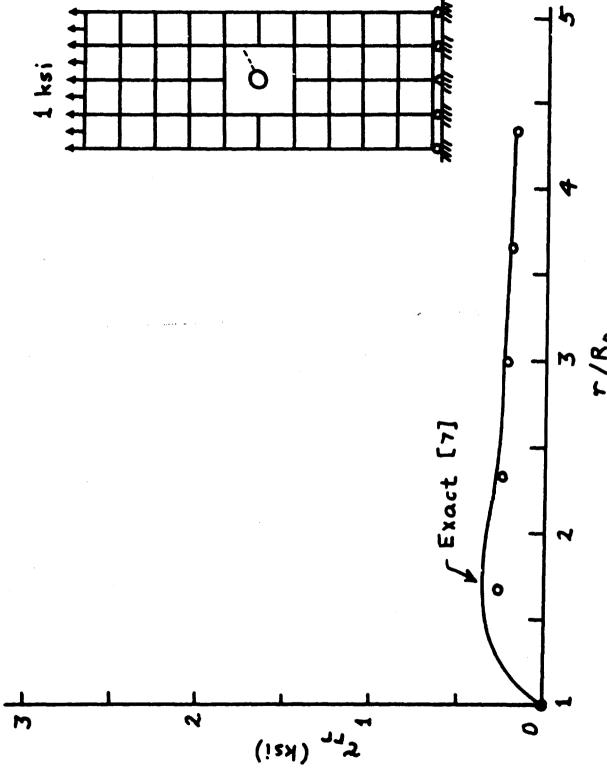
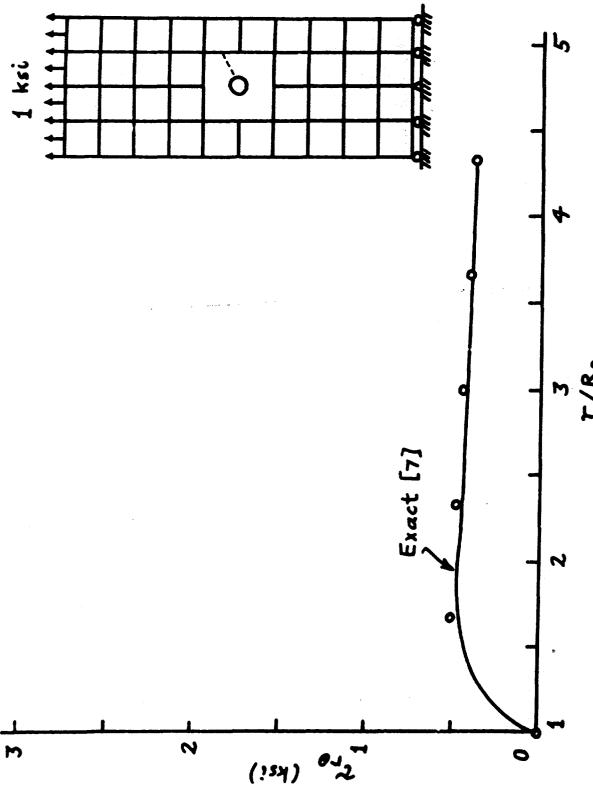


FIG. 14 BEHAVIOR OF 'INTAR STRESS-FREE EDGE

6, u



70

PIG. 15 BEHAVIOR OF $\tau_{r\theta}$ NEAR STRESS-FREE EDGE

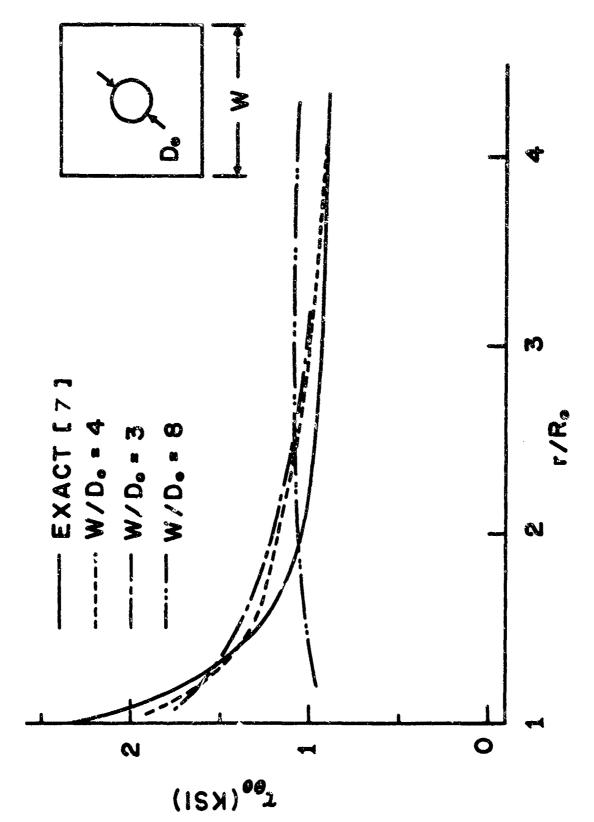


FIG. 16 SENSITIVITY OF HOLEL TO SHAPE PARAMETER W/D $_{
m O}$

2000年,1914年,1918年,1918年,1918年,1918年,1918年,1918年,1918年,1918年,1918年,1918年,1918年,1918年,1918年,1918年,1918年 1918年 1918年

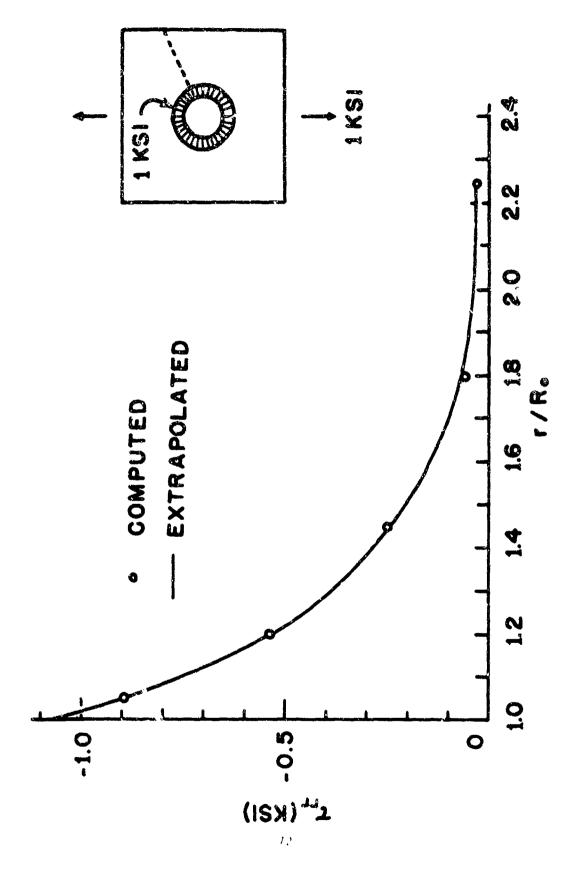


FIG. 17 ABILITY OF HOLDL TO ACCEPT AN INTERFERENCE FIT

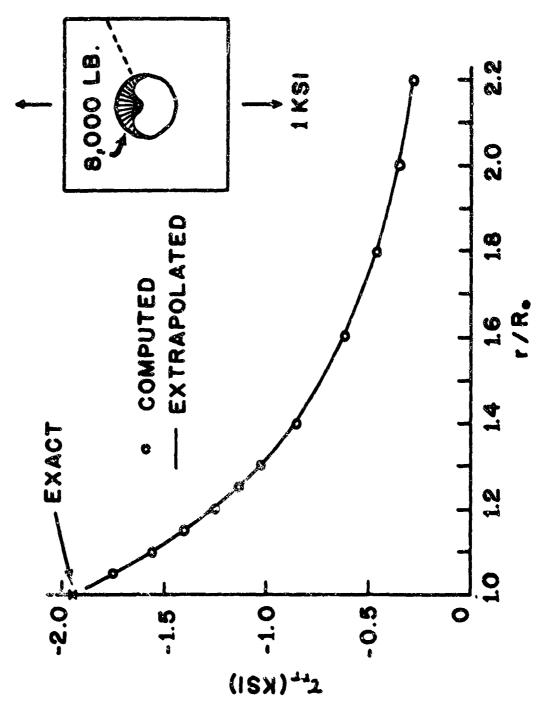


FIG. 18 ABILITY OF HOLEL TO ACCEPT A BEARING LOAD

The state of the s

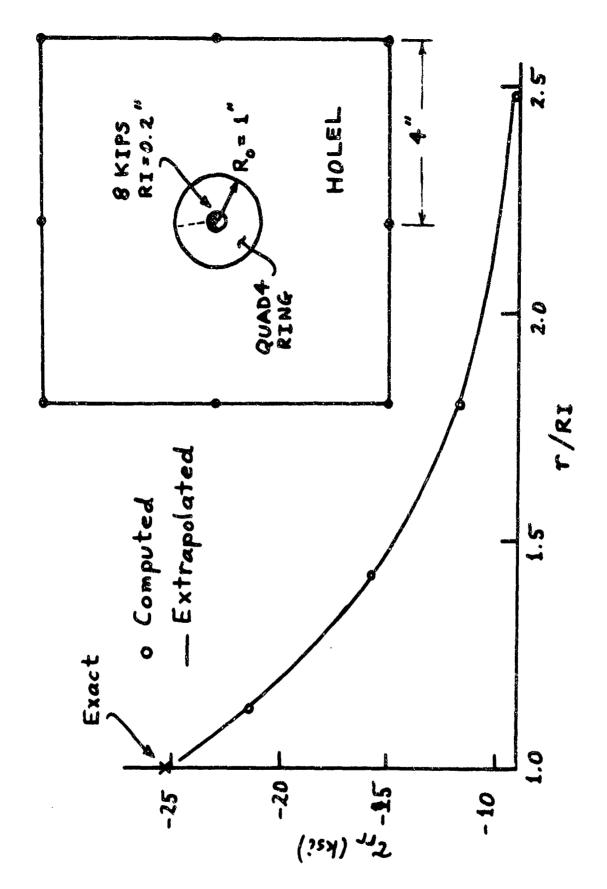
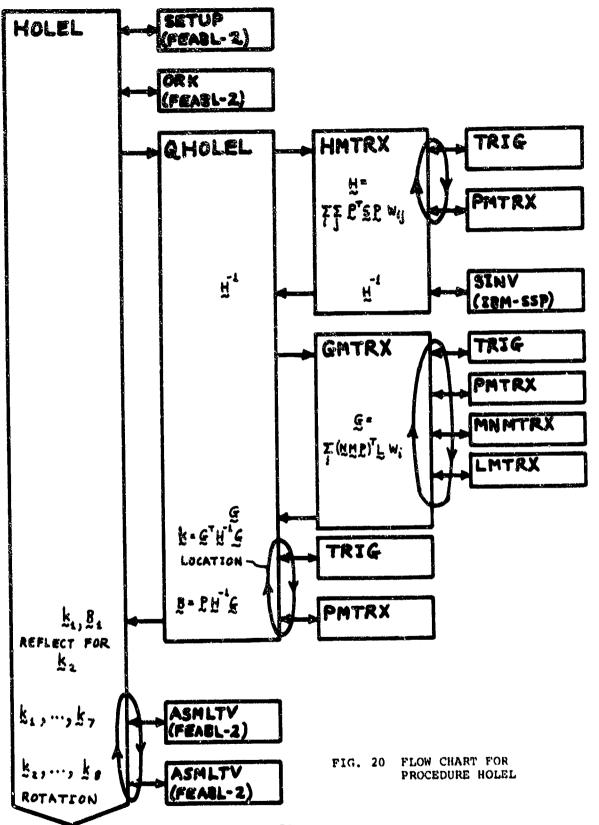


FIG. 19 TEST OF HOLEL WITH INTERIOR RING SUBJECTED TO BEARING LOAD



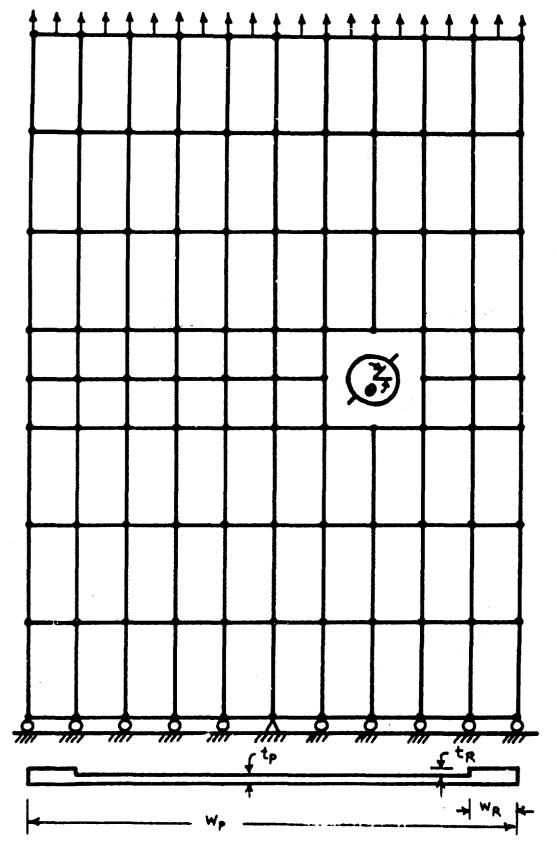


FIG. 21 PANEL PROGRAM SEPTICETIER

100 tree	PANEL PROGR.	PROFRAMS -	INPUT DATA FRENCH	INPUT DATA CONVENTIONS FRENCH	APAR 1975 SHEET I	STALK ORRENOFR
coep*	+wiprH +	LENGTH +	+ ×H.	STEFE TO HE PRESS -	**************************************	Toffst
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3 (2)	(ZE 10,3)	7				
4 - 6715	kr. 4kr.					
	de la description description de la description					
	.	PIG. 22 INPU	IT DATA CONVEN	INPUT DATA CONVENTIONS FOR PANEL PROGRAM	ž	

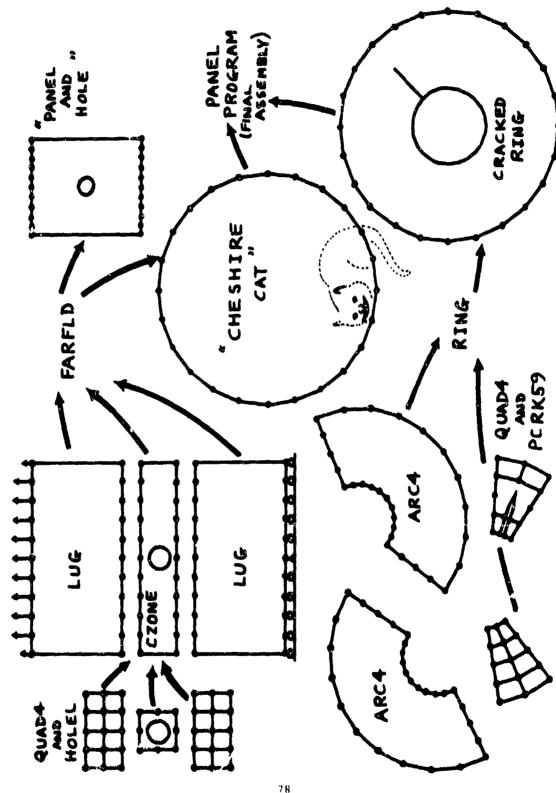
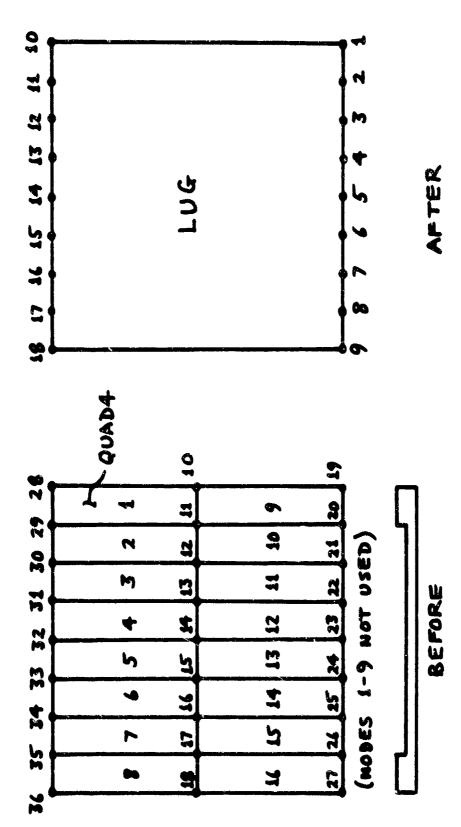


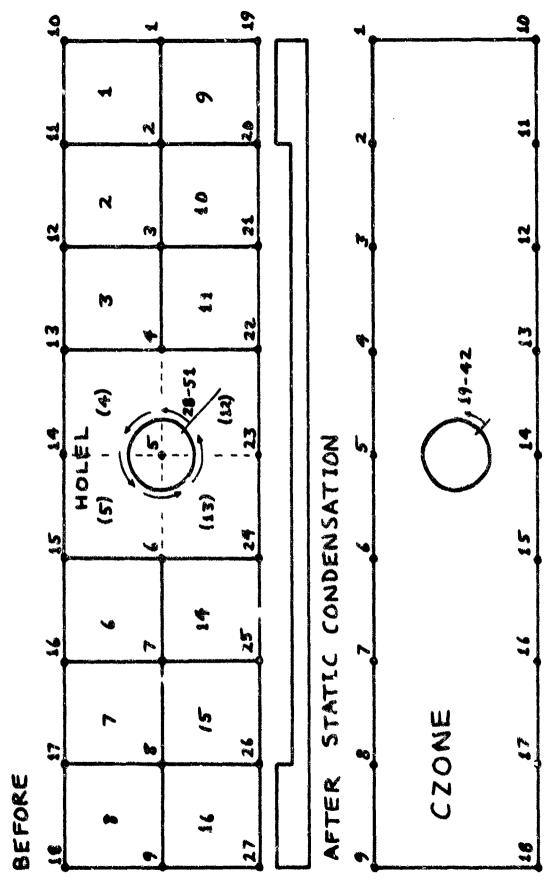
FIG. 23 HIERARCHY OF SUBSTRUCTURED COMPONENTS USED IN PAYEL PROGRAM



STATIC CONDENSATION

EXAMPLE WITH 8 ELEMENTS ACROSS PANEL

11G. 24 LUG SUBSTRUCTURE NUMBERING CONVENTIONS



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FIG. 25 CZOME STBSTPUCTUPE TUMBERING CONVEMTIONS

EXAMPLE WITH 8 ELEMENTS ACROSS PANEL

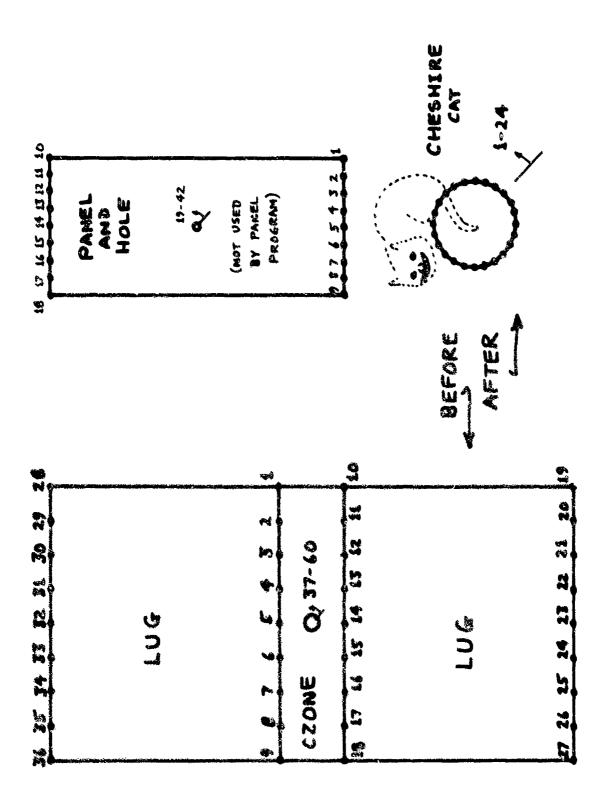
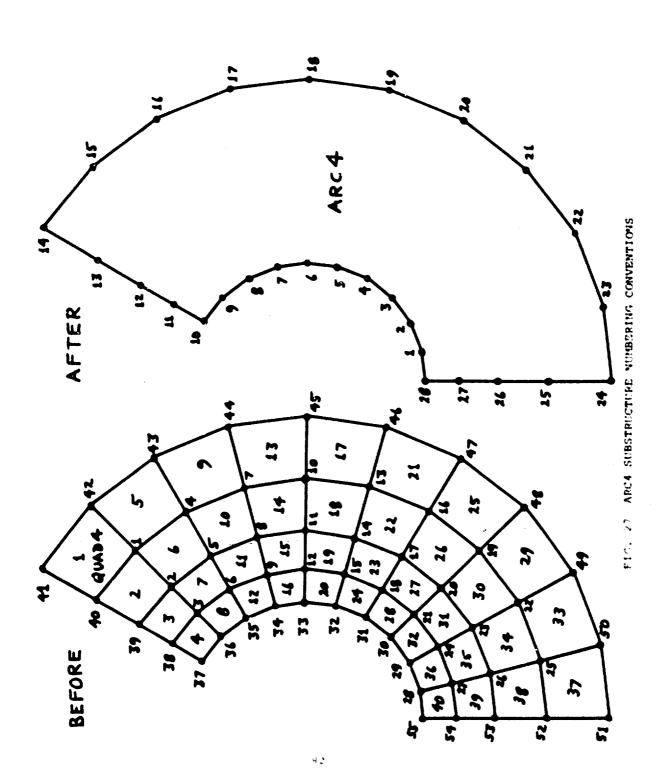
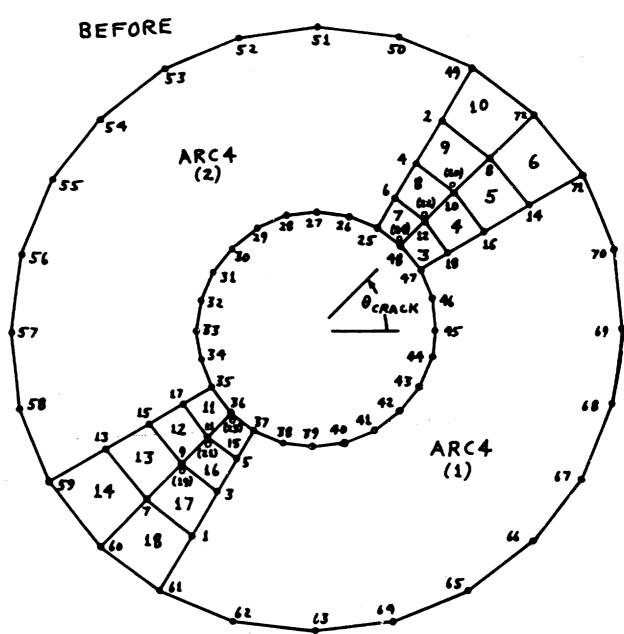


FIG. 26 FARFLD STRSTPTCTURE WURDERING CONVENTIONS





NODES (19)-(24) USED ONLY WHEN CRACK IS PRESENT PCRK59 ELEMENTS ARE 19 (CRACK 1) AND 26 (CRACK 2)

FDG. 28 RENG SUBSTRUCTURE CONVENTIONS (BEFORE CONDENSATION)

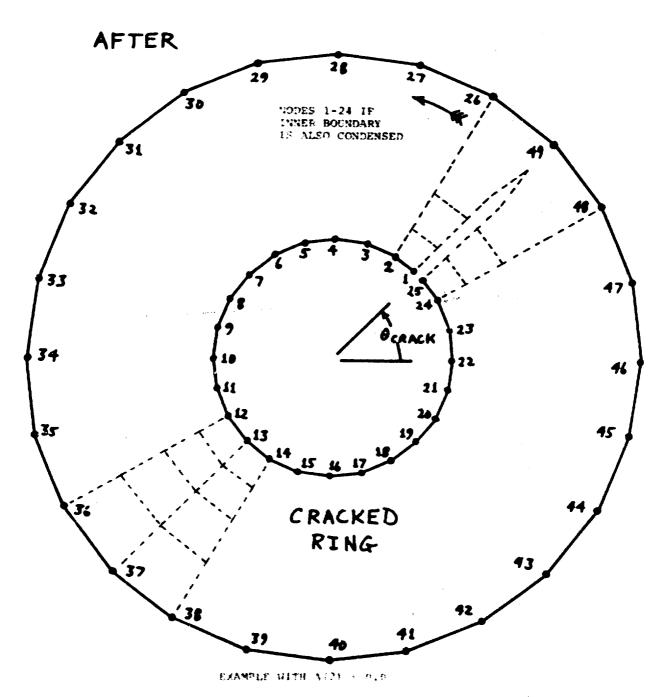


FIG. 29 FIND SUBSTRUCTURE CONTENTIONS (ONE CRACK)

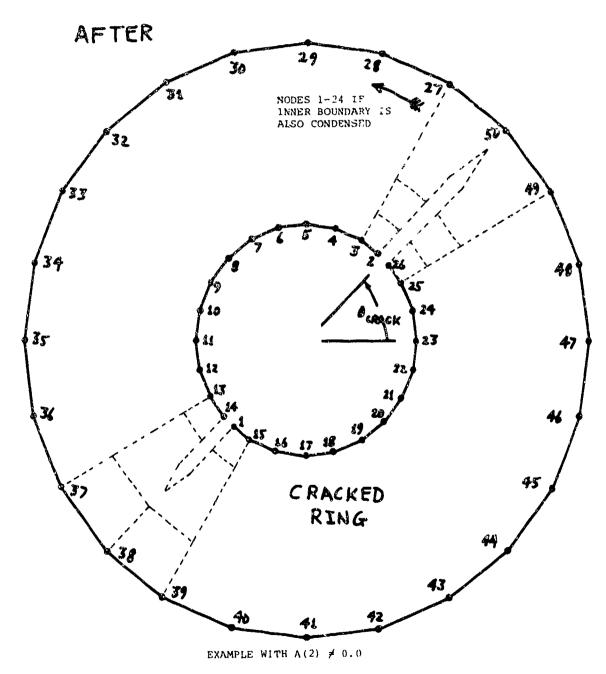


FIG. 30 RING SUBSTRUCTURE CONVENTIONS (TWO CRACKS)

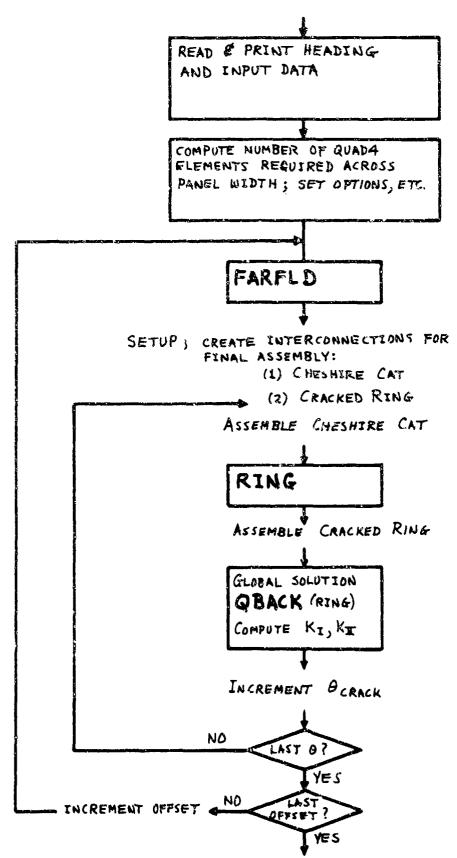


FIG. 31 EXECUTIVE FLOW CHART FOR PANEL PROGRAM

CONTRACT 81739

PROBLEM NO. 3

LEPT SIDE STIPFFRED

INPUT DATA

and one of the section of the sectio

وجالت لمجاهر تعمد

FLATE GECMETRY:

Service Service Box

PIATE WICTH= 0.4000CF+C1

PIATE LENGTH= C.100CCE+02

FLATE THICKNESS= 0.1CGCOE+01

FLATE STIFFENEN F/CTCR= 0.500

FAR FIFLD LOALING (FSI)= 0.1CCCOE+04

RACIUS OF HOLE= 0.125CCE+00

HCLE CFPSET INDICATCL= 1{=0, HOLE REMAINS CENTERED ==1, HOLE MOVED TO THE RIGHT =e1, HOLE MOVED TO THE LEFT}

CRACK DATA:

CBACK NG. 1: CRACK LENGTH= 0.125009+00

INITIAL CRACK POSITION= 1(0.0 DEGREES) FINAL CRACK POSITION= 13(180.000 DEGREES)

CRECK NC. 2: CRECK LENGTH= 0.125008+00

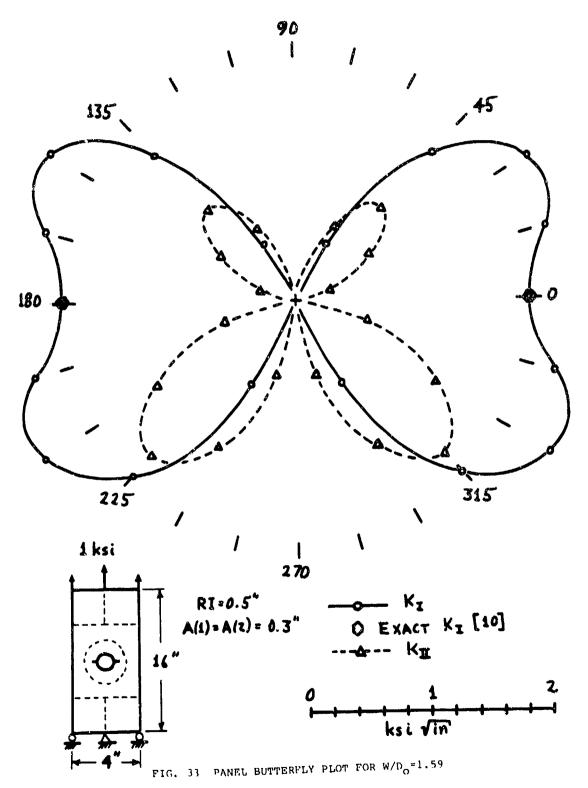
INITIAL CRACK POSITION= 1 (180.000 DEGREES)
FINAL CRACK POSITION= 13 (360.000 DEGREES)

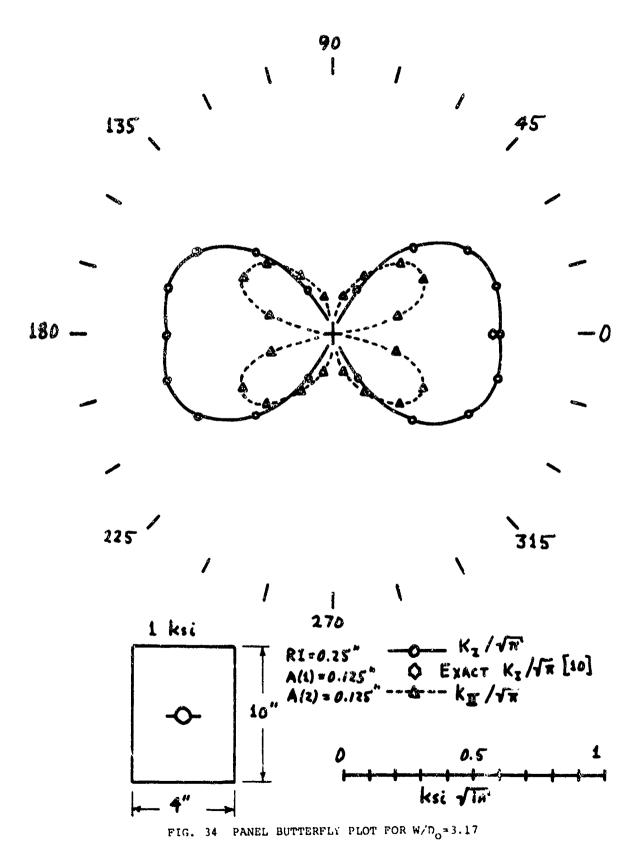
HATERIAL PROPERTIES:

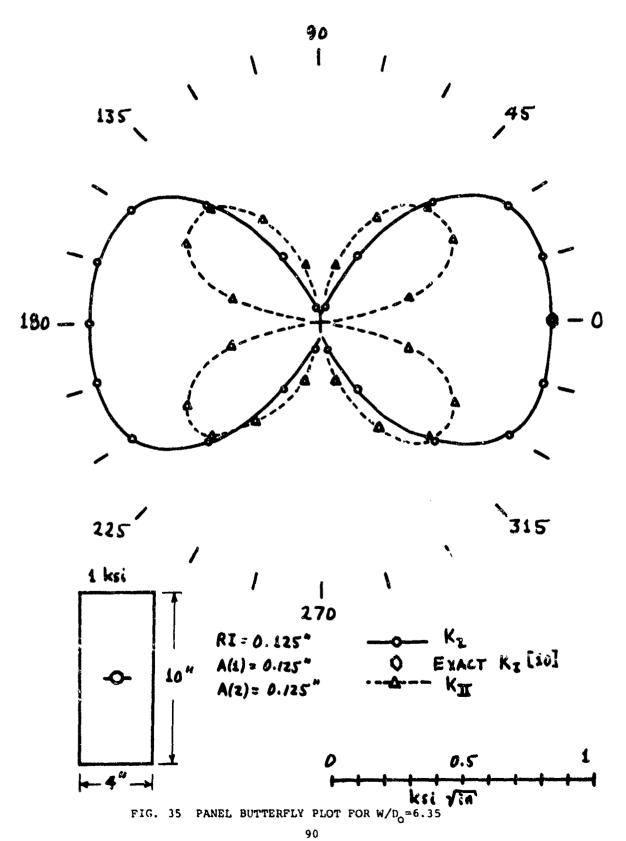
YCUNGS MCCULUS (E) = C.10000F+C8 ECISSONS FATIO= 0.30C0CE+00

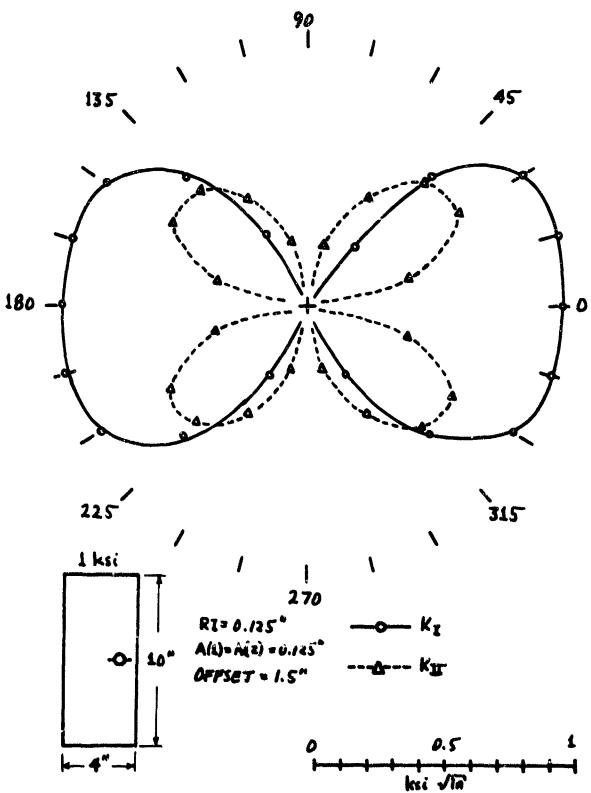
CRACK	 -	ANGLE=	C.0 180.000		0.87369F+03 0.87216F+03	 0.11424E+00 0.45826E+00
CRACK CRACK		ANGLE-	15.000 195.000		0.87397E+03 0.87177F+03	 0.35178E+03 0.35054E+03
CRACK CRACK			30.030 210.030		0.828981+03 0.826471+03	 0.58763E+03 0.58543F+03
CRACK CRACK	 	ANGLE=	45.000 225.000		0.60824E+03 0.60659E+03	 0.58508E+03 0.58246E+03
CRACK CRACK		ANGLE=	60.030 240.030	• • • •	0.27609F+03 0.27596F+03	 0.44344E+03 0.44213E+03

FIG. 32 SAMPLE OUTPUT FROM PANEL PROGRAM

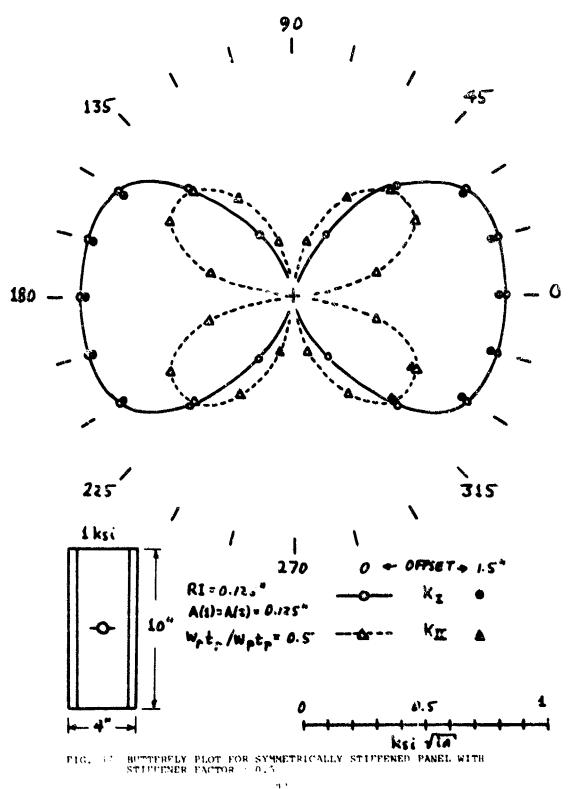


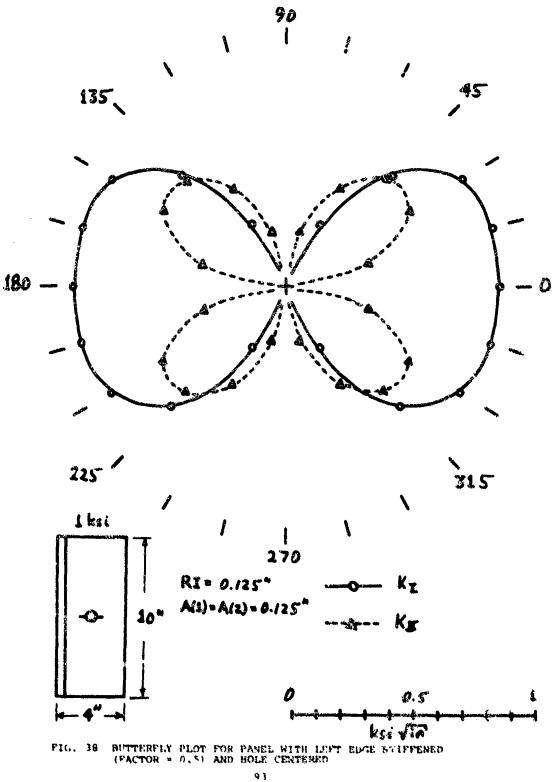


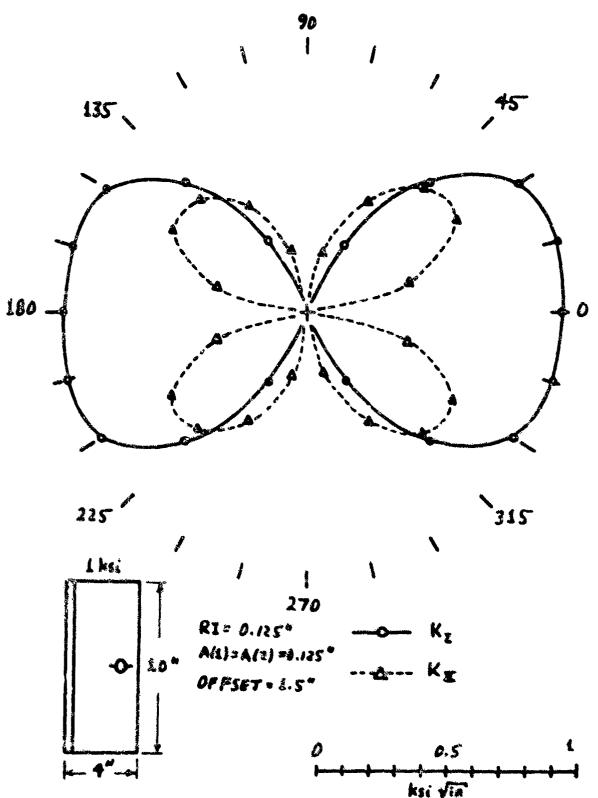




PIG. 36 BUTTERFLY PLOT FOR PANEL WITH W/D =6.35 AND FASTENER HOLE OFFSET 1.5 INCHES TO RIGHT







PIG. 19 BUTTERFLY PLOT FOR PANEL WITH LEFT EDGE STIFFENED AND HOLE OPPSET 1.5 INCHES TO RIGHT

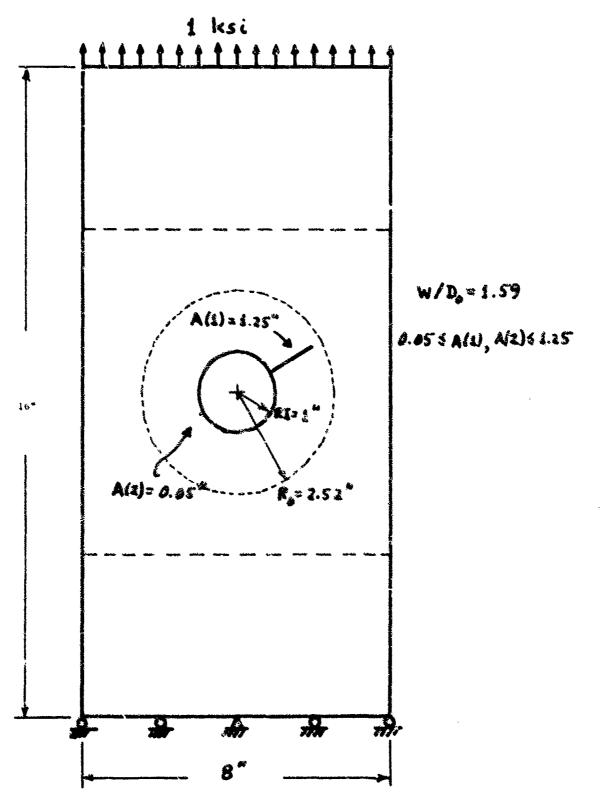


FIG. 40 PANEL DIMERSIONS FOR TEST OF SENSITIVITY TO A/RI

Appendix A

ALGORITHM FOR TRANSFERRING A SUBSTRUCTURE TO RESERVE STORAGE

Assume that a standard TEABL-2 assembly has been executed, and that the assembled structure has been statically condensed with subroutine STACON. The objective is to transfer the condensed stiffness matrix $K_{BB}^{(c)}$ and force $Q_B^{(c)}$ from the FEABL DATA vector (designated by RNAME, INAME) to reserve storage. Assume further that $K_{BB}^{(c)}$ is almost fully populated. Therefore, $K_{BB}^{(c)}$ is to be inflated to a fully populated, lower-triangle-vector-stored matrix during the transfer process. For this purpose, vectors STORK and STORQ are limensioned in the MAIN program to at least NIN+1)/2 and N words respectively, where N is the total number of boundary (uncondensed) degrees of freedom remaining. Vector STORK will receive $K_{BB}^{(c)}$, while STORO receives $Q_B^{(c)}$.

Other variables appearing in the algorithm play the following roles. IZERO is the first uncondensed degree of freedom, i.e., IZERO = NIO+1. I and J are loop indices which control progress through $K_{BB}^{(c)}$ and $G_{B}^{(c)}$ in the DATA vector: I for the lowe and I for the columns. If a row is encountered for which the band margin of $K_{BB}^{(c)}$ lies to the right of column IZEBO, then some leading zeros must be inserted in the corresponding row in STORK. LNZCOL is used to compute and compare the band margin. If is used to hold the variable-bandwidth address information required to locate

stiffnesses in the DATA vector belonging to ROW I. M, N and MN are used to trace the lower-triangle address in vector STORK.

IKOUNT, ILNZ and IQ are FEABL address control parameters located in the BEGIN labelled COMMON area. NDT is the total number of degrees of freedom in the assembled structure (boundary plus interior), available in the SIZE labelled COMMON area.

The transfer algorithm begins immediately after subroutine STACON has been executed:

IZERO = NID+1

M=0

DO 20 I=IZERO, NDT

II=INAME(IKOUNT+I-1)

M=M+1

STORQ (M) = RNAME(IQ+I-1)

N≔0

DO 10 J=IZERO,I

N=N+1

MN = (M*(M-1))/2+N

STORK (MN) = 0.0

LNZCOL=INAME(ILNZ+I-1)

IF(LNZCOL-J) 5,5,10

5 STORK (MN) = RNAME (II+J)

10 CONTINUE

20 CONTINUE

AFPENDIX B

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WOLEON13
                                                                                                                                                                 HOLE 0003
                                                                                                                                                                                                                                                                      HOLENDO7
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                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   HOLEGOZE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    HOLE 0020
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              HOLE 0025
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       HOLE 0027
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            HOLEGOZE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    HOLE 0029
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              HOLEONBE
                                                        HOLE 0001
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            HOLF 0011
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            HOLE 0 021
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 HOLEGORS
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     HOLE 0030
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                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         HOLEBO33
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          HOLEO034
                                                        SUBROUTINE HOLEL GENERATES A RECTANGULAR FINITE ELEMENT SUBSTPUCTURE
                                                                                                                                                          WITH A POUND HOLE IN ITS CENTER. THERE ARE 8 NODES ON ITS PERIMETER
                                                                                                                                                                                                                                                                                                                                                                                                                                           · 电电子电路 17 中央的 19 中央的 
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        C FINITE ELEMENT APPLICATIONS TO USAF STRUCTURAL INTECTORY PROBLEMS
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                DIMENSION RSS (2097) . ISS (2097) . ISAVE 1 (2) . ISAVE 2 (4) . ISAVE 3 (4)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 @.COGRD(12).5(3.3):V(78).ELU(12).B(6.3.13):VR(78):((12.12).
                                                                                                                                                                                                                                                                                                                       COPYRIGHT (C) 1975 MASSACHUSETTS INSTITUTE OF TECHNOLOGY
                                                                                                                                                                                                                                                                                                                                                                                   C AEROELASTIL AND STPUCTURES RESEARCH LABORATORY
SUBROUTINE HOLEL (COORD. THK. S.RI. RSS. ISS.8)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 DATA NODEL/2,1,9,10,11,12,2,3,15,14,13,12,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         MELKR (12.12) + ELK (12.12) + NODEL (5.8)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     84.3,15,16,17,18,4,5,21,20,19,18,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     CALLING PROGRAM FEARL CONTROLS
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          P6.5.21,22,23.24.6,7:27,26.25,24.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                COMMON/SIZESS/NETSS.NDTSS.NIDSS
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              88.7.27.28.29.30.8.1.9.32.31.30/
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          COMMON/IO/KR.KW.KP.KT.KTC.KTG
                                                                                                                                                                                                              C AND 24 NODES APOUND THE HOLE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          COMMON/PEGIN/IBEGIN(6)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  COMMON/SIZE/NET+NOT
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    COMMON/REGSS/186(6)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          SAVE2(I)=IBEGIN(I)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               COMPONZEND/JEND(6)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         DATA P1/3.141593/
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               SAVE3(1)=IEND(1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   DO 130 I=1.12
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         SAVEI (1) =NET
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 SAVE 1 (2) = MI)T
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       50 130 J=1.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      0 10 I=1.6
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                PI4=PI/4.0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        T(I.J)=0.0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    \Gamma(J_{\bullet}I) = 0.0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           PI2=PI/2.0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        SAVE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      0
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HOLE 0037
                             HOLE 003A
                                          HOLE GO39
                                                                                              40LE0043
                                                                                 HOLE 0042
                                                                                                           400 E 0044
                                                                                                                         JOLE0045
                                                                                                                                      HOLF 0046
                                                                                                                                                  HOLE 1047
                                                                                                                                                               HOLE 0048
                                                                                                                                                                             401E0049
                                                                                                                                                                                                                                                           HOLE 1055
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                                                                                                                                                                                                                                                                                                                                                                   HOLEOOK3
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                                                                                                                                                                                                                                                                                                                                                                                                                                      HOLE 6068
                                                                                                                                                                                                                                                                                                                                                                                                                                                   HOLE 0069
                                                         MOLE 0040
                                                                                                                                                                                          HOLE 0050
                                                                                                                                                                                                                               HOLEL: 1/10H POINTERS: AIS. / 16HHOLE0053
                                                                                                                                                                                                                                              HOLE0054
                                                                                                                                                                                                                                                                                    HOLE 0057
                                                                                                                                                                                                                                                                                                                                                                                 101 E 0 0 64
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                                                                                                                                                                                                                                                                                                                                                                                                                        HOLEGOR7
                                                                                                                                                                                                                                                                                                                                                                                                                                                                HOLE 0070
                                                                   HOLE 0041
                                                                                                                                                                                                      HOLENOS!
                                                                                                                                                                                                                    HOLEOOSS
                                                                                                                                                                                                                                                                                                                                        MOLEGO61
                                                                                                                                                                                                                                                                                                                                                      HOLEOO62
                                                                                                                                                                                                                                                                                                                                                                                                                                                                           THETAI=PI+P12
                                                                                                                                                                                                                                                                                                                                                                                                                                                 THETAI=PI2
                                                                                                                                                                                                                                                                                                                                                                                                                                                              THETAI=PI
                                                                                                                                                                                                                                                                                                                                                                                                                                                 (0°0
                                                                                                                                                                                                                                                                                                                                                                                                                                                             (0.0)
                                                                                                                                                                                                                                                                                                                                                                                                                                                GT.
                                                                                                                                                                                                                                                                                                                                                                                                                                                             GT.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                         ·LT.
                                                                                                                                                                                                                 WRITE (nk+6001) (ISS(I) + I=IMASTR+LMASTR)
                                                                                                                                                                                                                                                                                                                                                                                                                                                             COORD (2)
                                                                                                                                                                                                                                                                                                                                                                                                                                                CO0RD (2)
                                                                                                                                                                                                                                            ELEMENT 0.0.F.S./.R(1H .1215./))
                                                                                                                                                                                                                              FORMAT (30H MASTER ASSFMBLY LIST:
                          CALL SETUP (2097,9,104,RSS,1SS)
                                                                                                                                                                                                                                                                                   CETERMINE NODF/QUADRANT ASSOC.
                                                                                                                                                                                                                                                                                                                                                                                                                                               . GND.
                                                                                                                                                                                                                                                                                                                                                                                                                                                             . DND.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                          · GNV.
                                                                                                                                                                                                    FIKT1 .EQ. KW) GO TO 707
                                                                                                                                                                                                                                                                                                                                                                                                        303PD (N+1) = C00RD (N+1) - XC
                                                                                                                                                                                                                                                                                                                                                                                                                     0000 (N+2) = 000RD (N+2) - YC
                                                                                                       PNTR=IMASTR+NFT+NM1+12
                                                                                                                                                                                                                                                                      CALL ORK (2097, RSS-155)
                                                                                                                     SS(IMASTR+NM1)=IPNTR
                                                                                                                                                                                                                                                                                                                                                                                                                                                0.0
                                                                                                                                                                                                                                                                                                                                                                                                                                                             0.0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                         0.0
                                      ESTABLISH ASSEMBLY LIST
                                                                                                                                                                                                                                                                                                                                                    XC=XC+C00RD (N+1) /4.0
                                                                                                                                                                                                                                                                                                                                                                 YC=YC+C00RD (N+2) /4.0
                                                                                                                                                                          SS(IADG-1)=100F-1
                                                                                                                                                            DOF=NODEL (ToN) #2
                                                                                                                                                                                                                                                                                                                                                                                                                                                                        ·LT.
                                                                                                                                                                                                                                                                                                                                                                                                                                                • GT •
                                                                                                                                                                                                                                                                                                                                                                                                                                                             • L. T.
                                                                                                                                               [ADD=IPNTR+[#2-1
                                                     [MASTR=IBEGIN(4)
                                                                                                                                                                                        SS (IADE) = 100F
                                                                 -MASTR=YEND(4)
                                                                              00 40 N=1,NET
                                                                                                                                 DO 40 1=1.6
                                                                                                                                                                                                                                                                                                                         DO 50 1=1,4
                                                                                                                                                                                                                                                                                                                                                                                                                                               F (COORD (1)
                                                                                                                                                                                                                                                                                                                                                                              00 60 I=1.4
                                                                                                                                                                                                                                                                                                                                                                                                                                                             F(C00RD(1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                         (F(CC020(1)
                                                                                                                                                                                                                                                                                                                                                                                                                                  HETA1=0.0
                                                                                                                                                                                                                                                         CONTINUE
                                                                                                                                                                                                                                                                                                                                       E-E+I=7
                                                                                                                                                                                                                                                                                                                                                                                           6-6+I=7
                                                                                            NA LAN-
                                                                                                                                                                                                                                                                                                XC=0.0
             NDT=64
                                                                                                                                                                                                                                                                                                             VC=0.0
NET#8
                                                                                                                                                                                                                                6003
                                                                                                                                                                                                                                                         707
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	1BS (COO	HOLEN072
	GHOLEL	MOLE 1073
, .	2	HOLE 0074
)=1.0	HOLEN075
	-	HOLE 0076
	1	HOLENNYY
	1142=11-2	HOLE no 78
	=	HOLEU079
7.0	12+I+If	MOLE0080
	00 80 I=1.12	HOLEOOBI
) J=1+1	HOLEOOBZ
	$(I \circ J) = 0$	40LF0083
	K=1.	HOLEOOR4
	L=1:12	HOLEOO85
D.R.	=([.1]	40LE0086
	SFORM FL	HOLE0087
	1 =THETA	HOLEOOBR
	:-1	HOLE 0089
	NEL2=0	HOLE0090
	[=N 0]	HOLE0091
	WEL1=NEL1+2	HOLFOOGS
	:NEL 2+2	HOLE0093
	(1,2	HOLE0094
_	0	HOLE0095
	0°0=\$S	HOLE0096
	60 TO 5	HOLE0097
~	CS=(.0	HOLE0098
	SS=1.0	AULE0099
	60 TO S	HOLE0100
(*	CS=-1,0	WOLEN101
	0.0=58	40LE0102
	60 TO S	HOLE 0103
7	CS=0•0	HOLE0104
	8<=-1.0	HOLE 0105
៤	CONTINUE	HOLE 0106
		40LE:0107

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HULE 0109
HOLE0108
                            HOLE0110
                                                                     HOLE 0113
                                                                                                HOLF 0115
                                                                                                                                         40LE0118
                                                                                                                                                       HOLE 0119
                                                                                                                                                                    40LE0120
                                                                                                                                                                                                           HOLE 0123
                                                                                                                                                                                                                          40LE0124
                                                                                                                                                                                                                                       HOLF 0125
                                                                                                                                                                                                                                                     40LE0126
                                                                                                                                                                                                                                                                                MOLE 0128
                                                                                                                                                                                                                                                                                              40LE0129
                                                                                                                                                                                                                                                                                                                                                                              40LE 0 135
                                                                                                                                                                                                                                                                                                                                                                                               40LF0136
                                                                                                                                                                                                                                                                                                                                                                                                                       40LE0138
                                                                                                                                                                                                                                                                                                                                                                                                                                      40LE0139
                                           HOLFOILL
                                                        HOLE 0112
                                                                                    HOLEO114
                                                                                                               HOLEO116
                                                                                                                           HOLE 0117
                                                                                                                                                                                  40LE0121
                                                                                                                                                                                               40LE.0122
                                                                                                                                                                                                                                                                   401F0127
                                                                                                                                                                                                                                                                                                            40LE0130
                                                                                                                                                                                                                                                                                                                          HOLF 0131
                                                                                                                                                                                                                                                                                                                                      HOLEO132
                                                                                                                                                                                                                                                                                                                                                    HOLEO133
                                                                                                                                                                                                                                                                                                                                                                  40LF 0134
                                                                                                                                                                                                                                                                                                                                                                                                          40LE0137
                                                                                                                                                                                                                                                                                                                                                                                                                                                    401.E0140
                                                                                                                                                                                                                                                                                            RETURN CALLING PROGRAM FFARL CONTROLS TO THEIR ORIGINAL STORAGE
                                                                                                                                                                                                                                     VR(L) = VR(L) + T(K+1) + ELKR(K+LL) + T(LL+J)
CALL ASMLTV(NEL1+12+VR+FL0+RSS+1SS)
                                                                                                                                                                                                                         V(L)=V(L)+T(K+1)*ELK(K+LL)*T(LL+J)
                                                                                                                                                                                                                                                                 CALL ASMLTV (NFLZ.12.V.FI D.RSS.1SS)
                                                                                               T(ITM2+I+ITM2+J)=T(I+J)
                                                                                                                                                                                                                                                                                                                                                                                                         BEGIN(I)=ISAVF2(I)
                                                                                                                                                                                                                                                                                                                                                                                                                       (I) = I < AVE 3(I)
                                                                                                                                                                                                                                                                                                                                                                                           186(1)=18EGIN(1)
                                                                                                                                                                                                                                                                              THE TA=THF TA+DI?
                                         DO 90 IT=2,12,2
                                                                                                                                                                                                           DO 100 LL=1,12
            T(2,1)=-T(1,2)
                                                                                                                          DO 100 I=1,12
                                                                                                                                                                                             50 100 K=1.12
                          T(2.2)=T(1,1)
                                                                                                                                                                                                                                                                                                                                                    NET=ISAVE1(1)
                                                                                                                                                                                                                                                                                                                                                                NDT=ISAVE1(2)
                                                                                                                                                                                                                                                                                                                                                                              90 120 I=1.6
                                                                                                                                        DO 100 J=1.1
                                                                    90 I=1.2
                                                                                 90 J=1+2
1(1.2)=55
                                                      ITM2=11-2
                                                                                                                                                                                VR(L)=0.0
                                                                                                                                                                                                                                                                                                          NETSS=NET
                                                                                                                                                                                                                                                                                                                       NOTSS-NOT
                                                                                                                                                                   V(L)=0.0
                                                                                                                                                                                                                                                                                                                                    N1055=0
                                                                                                                                                                                                                                                                                                                                                                                                                                    RETURN
                                                                                                                                                     [=[+]
                                                                                                             0=1
                                                                                                                                                                                                                                       100
                                                                                                                                                                                                                                                                                                                                                                                                                       120
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\$ * *	SURROUTINE GHOLEL (THK+C+PI4+HFD+RI+ELK+ELG+R) spappeststatestatestatestatestatestatest	9HOL 0000
C SUB	SUBROUTINE CHOLFL FORMS STIFFNESS MATRIX AND B MATRIX THIS SUBROUTINE IS USED IN FORMING THE HOLE SUBSTRUCTURE OF HOLFL	040L0002
* a a c	.comennessessessessessessessessessessessesse	0H0L.0004
CAER	OFLASTIC AND STRUCTURES RESEARCH LABORATORY	900UTUHO
0000		TOHOL 0007
CFIN	ITE ELEMENT APPLICATIONS TO USAF STRUCTURAL INTEGRITY PROBLEMS	CHOLOOB
	DIMENSION S(3+3)+ELK(12+12)+HI(10+10)+B(5+3+13)+G(10+12)+HIG(10+12QHOL0009	20H0L6009
	#7.************************************	0100 000
	CALL HMIRK (DI4-HMD-RI-S-MI)	CHOLO012
	CALL GMTRX (PI4.HWD.RI.G)	QHOL 0013
	00 10 1=1+10	QHOL0014
	00 10 J=1.12	QH0L.0015
	HIG(I•J)=0.0	QH0L0016
	DO 10 K=1.10	QHOL NO 17
10	HIG(I.))=HIG(I.)+HI(I.K)=G(K.)	0H0L0018
	00 20 I=1·12	040L0019
	ELQ(I)=0.0	040L0020
	00 20 J=1+12	0H010051
	ELK(I,J)=0.0	CHOLO022
	DO 20 K=1.10	QH010023
20	ELK(I.J)#ELK(I.J)+G(K.I)+HIG(K.J)+THK	040L0024
	R≈RI	0H010025
	THETA=P14/2.0	040L0026
	CALL TRIG(THETA)	QH010027
	DR=(HWD/CS-R1)/5.0	0H010028
	9*1=1 0+ CO	0H0L0029
	CALL PMTRX(0,8)	0H0L0030
	00 36 J=1+3	QHOL0031
	00 30 K=1,12	0H0L0032
	G(I•J•K)=0•0	9
	PO 36 L=1.10	00
30	B(I•J•K)=B(I•J•K)+P(J•L)*HIG(L•K)	0H0L0035

0H0L0036 0H0L0037 0H0L0038 0H0L0039 0H0L0040

B(I+1+13)=THETA R(I+2+13)=R R(I+3+13)=0.0 R=R+DR RETURN END

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	SUBPOUTINE HMTRX (PIC.HWP.RI.S.H)	HMTROBOO
•	respectations are respected to a second seco	1000X ET
	SUBROUTINE	HMTR0003
U	YPIGHT (C) 1975 MASSACHUSFTTS INSTITUTE OF TECHNOLOGY	HMTR0005
⋖	LASTIC AND S	HMTR0006
0	· 在,我们的是一个,我们们的一个,我们的一个,我们的一个,我们们们的一个,我们的一个一个,我们的一个,我们们的一个,我们的一个,我们们的一个,我们们们的一个,	**HMTR0007
lu.	TE ELEMENT APPLICATIONS TO JSAF STRUCTURAL INTEGRITY PROBLEMS	HMTROOD
	H(10,10),HV(55),S(3,3	HMTRO009
	CINENSION 2(5) 2M+ (5)Z NOISNEWIO	TETRO010
	COMMON/TRGFNT/CS+SS+CS2+SS2+CS4+SS4	HMTROOIL
	F(Ae8eZ)=Ao7+B	4MTR0012
	1414 WZ/.236926947867875688889	HMTR0013
	•	HMTRO014
	98	HMTR0015
	•	-
		HMTRO017
	10 J=1	HMTROOIA
	(,,)	-MTR0019
10)H=(11)	HMTRO020
	THT=PIL/	LMTR0021
	STHT=OEL TE	JMTRO022
	20 ITHE	HMTR0023
	L TPIG(F)	HMTR0024
	EMMO/ABS (C	HMTR0025
	R= (R0-P)	HMTR0026
	3) =d5	HMTR0027
	50 IP=1+4	HMTROOZH
	FIDELROAVG	HMTR0029
	LL PMTOX	HMTR0030
	EFF=DELR*	HMTROOSI
	20 1=1.10	HMTR0032
	20 J=1.1	HMTR0033
	00 20 K±1.3	HMTR0034
	20 C=1.	HMTR0035

H(1.3)=H(1.3)*P(K.1)*S(K.L)*P(L.3)*CUEFF L=0 00 30 J=1.10 00 30 [=1.3] L=L+1 HV(L)=H([.1) CALL SIMV(Wv.10.1.0E-03.1NOCTP) CALL SIMV(Wv.10.1.0E-03.1NOCTP) CALL SIMV(Wv.10.1.0E-03.1NOCTP) H=1.0 H(1.3)=HV(L) H(1.3)=HV(L)
--

HMTR0036 HMTR0037 HMTR0039 HMTR0060 HMTR0061 HMTR0063 HMTR0063 HMTR0064

HMTROO47 LMTROO48 LMTROO49 LMTROO50

THE PARTY OF THE P

SUBBOUTINE GMTRX (PI4.H4n,R1.6)	GMTR0000
SUBDOUTINE GATOR GENERATER G MATOR A MATOR A	CATPOOC CATPOOC
HE SUBSOUTINE IS USED IN	GMTRn003
	0
NI SILUSIHUTSOTH SECOL (U) LTGIGAGGU	CMTR0005
AEROFLASTIC AND S	S4TA0006
	****CMTROOO7
FINITE ELEMENT API	CMTROODA
DIMENSION 7(9) . N. 7(9)	CMTR0009
OIMENSION G(10.12).P(3.10).PHINT(3.2).PL(2.12).THFTAI(2)	~
COMFON/TRGFNT/CS+SS+CS2+SS2+CS4+SS4	GMTRAO11
F (A+B+Z) #407 +9	=
DATA W27.236926947852875688A89	GMTRN013
2369269	7
69 538469	0
#.53846939041798 /.N7/5/	_
	CMTRO017
On 10 tml.10	CATROOLS
10 6(1.1)=0.0	prod
THETAI(1) = 0.0	34TR0020
TMFTA1(2) = P14	GMTR0021
C 90UNDARY 1-2	CMTR0022
400£1=1	3
NODE	GMTR0024
*0 £ 6	GMTRN025
=OEL THT	CMTR0026
ITHETAR	GMTROOZZ
F (DE	SHATKOORB CMTKOORB
PIGCTME	R002
SUZORRACO	CMTR0030
DS#RO/CS	3
PHTRX (P.	GMTR0032
ALL MUNTRY (N	R003
LMTRX (NODE 1 .NOD	TROOS
ZMaSUE	CMTROOUS

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GMTR0036
                               GMTR0038
                                             GMTR0039
                                                                                        GFTR0042
                                                                                                      GMTR0043
                                                                                                                                  CHIRDOGE
                                                                                                                                                GMTR0046
                                                                                                                                                                                           GMTRANGS
                                                                                                                                                                                                                                                                                CMTRORSS
               GMTR0037
                                                            CHTRO040
                                                                                                                     CMTR0044
                                                                                                                                                              CMTR0047
                                                                                                                                                                            GMTR0048
                                                                                                                                                                                                          CMTR0050
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                                                                         GMTR0041
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                                                                                                                                                                                                                                                                                                                                                                                     CMTRN062
                                                                                                                                                                                                                                                                                                                                                                                                   CMTRO063
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      CMTHO070
                                                                                                                                                                                                                        SMTR0051
                                                                                                                                                                                                                                                                                                                                                                      CMTROOF1
                                                                                                                                                                                                                                                                                                                                                                                                                  GMTR1064
                                                                                                                                                                                                                                                                                                                                                                                                                                                            にな】ないのも】
                                                                                                                                                                                                                                                                             LMTRX (NODE 1 . NODE 2 . THE TAT . THE TA . RO . R. . R.
                                                                                                                                                                                                                                                                                                                                                                    G(1.1) #G(1.1) +P(K.1) +FMTAT(K.L) +QL(L.1)+DQS
                                                          6(1.1) ±6(1.1) .p(K.1) *P#TNT(K.L) *RL(L.J) *DS
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  0517MT=(THETA1(2)-TMETA1(1))/2.0
6767MT=(THETA1(2)+TMETA1(1))/2.0
                                                                                                                                                                           DFLR=(P1-PO)/2.0*(-1.0)**(18+1)
                                                                                                                                                                                                                                                                MNMTAX (NODE 1 . NODE 2 . RMTMT)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    FPETAL (2) DTEETAL (3) LOTAT
                                                                                                                 NODE1=20(2-19).60(18-1)
                                                                                                                               NODE2=3+(2-18)+(18-1)
                                                                                                                                                                                                                                  R=F (DELR+4VGR+2(14))
                                                                                                   TERTARTERIAL (N-10)
                                                                                                                                             CALL TRIGITHETA)
                                                                                                                                                                                         AVGR= (RO.RI)/2.0
                                                                                                                                                                                                                                                                                                                                                                                                                                         NO SO ITHETAEL.3
                                                                        INDARY 2-3 & 6-1
                                                                                                                                                                                                                                                 PMTRX (P.R)
                                                                                                                                                             ROHMED/ABS (CS)
                                                                                                                                                                                                                    30 19×1.N7
                                                                                                                                                                                                                                                                                           (d1)2M+SQ=SQQ
                                                                                                                                                                                                                                                                                                                                                                                                             THE TAI (1) =PIG
                                                                                                                                                                                                                                                                                                                                                                                   HOLINDARY I-(I-1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                        MODELL = MODEL 1 - 1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                       10052×1000E1+1
                                                                                     00 30 18=1.2
[=1.10]
               J=1.12
                                                                                                                                                                                                       DS#48S (DELP)
                                                                                                                                                                                                                                                                                                          50 30 1×1.10
                                                                                                                                                                                                                                                                                                                         30 Jal 112
                                                                                                                                                                                                                                                                                                                                                                                               DIMINDIA/3.0
                                            20 1=1.2
                               K=1, =3
                                                                                                                                                                                                                                                                                                                                                     DO 30 Lel.2
                                                                                                                                                                                                                                                                                                                                       30 K=1+3
                                                                                                                                                                                                                                                                                                                                                                                                                            NOUE 1 = 5
             20
                             20
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Ash. Someter

GMTHN072 GMTHN073 CMTH0082 CMTRO076 GMTR0086 GMTR0087 CMTR0074 CMTR0075 CMTP0078 GMTRN079 CHIMNORS CMTR6040 CMT200A1 **180084** CALL, LMIDE NODE 1 . MORE 2 . THE TAL THE TA . WISH . R. PL. SCO. (- 1) 18. (1. X) TYTAG. (1. X) 0. (1. 1) 52 (1. 1) 5 THE TABE (DEL THT . AVGTHT . 7:1171) MANATOR INCOME LANGE AS A STATE THE TATE 11 STRETCI (2) CALL THIS (THETA) PMTHY (P.R!) The Italians DDS=08=42 (1141) 17-121 130-050 NO 40 1=1.10 נוט בנ שבויוץ AC 40 K21.5 ניט פט ובן.ץ RE TUNN CALL CALL

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COPYRIGHT (C) 1975 MASSACHISTIS INSTITUTE OF TECHNOLISY ACADESCENT LABORATORY	
PPLICATIONS TO USAF STRUCTURAL INTEGRITY	PPOBLEMS PMIRAGO
MENSION PINING	
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	CATRO
-	CMTR0
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10141-0	PMTRO
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	C3120

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JP4mJ+4
P(3-J)=P(3-J)=SS2
P(3-J)=P(3-J)=SS2
NO 60 1z1-2
P(1-J)=P(1-J)=CS2
C 14TROD:CF & MATAIX
NO 70 1=1-3
DO 70 J=1-10
P(1-J)=P(1-J)=A(1-J)
P(1-J)=P(1-J)=A(1-J)
P(1-J)=P(1-J)=A(1-J)
P(1-J)=P(1-J)=A(1-J)
P(1-J)=P(1-J)=A(1-J)
P(1-J)=P(1-J)=A(1-J)

TR169000	*TRIG0001	TRIG0002	TRIG0003	*TR160004	TRIG0005	TRIG0006	*TRIG0007	TRIGOOOB	TR160009	TR160010	TRIG0011	TRIGOOIZ	TR160013	TRIG0014	TRIG0015		TRIG0016	14160017
	****		F MOLEL	***			***	ROBL EMS										
	******	SZ	STRULIURE OF	*****	CHNOLOG	ŀ	****	INTEGRITY P										
	. 1000	FUALUATES TRIGONOMETRIC FUNCTIONS	IS USED IN FORMING THE HOLE SUBSTRUCTURE OF HOLFL	****	LITUTE OF TE	ABORATORY		STRUCTURAL	784									
	***	TRIGONOMETR	FORMING TH	***	INSTITE INST	DESFARCH -	****	IS TO USAF	COMMON / TREETING ST. CS. CS. CS. CS. CS. CS. CS. CS. CS. CS					S	J			
TOTC (THETA)	· -			**************************************	975 MASSACH	STOILCTUBES	******************************	APPLITCATION	00.00.00.TN	TA)	· · ·	0F0*00*0	C	SSC-C+OLO-SS-CS CCC-1 AFA-CCS&CCS		264.226		
CHEMPASTINE TOTAL THETA)		STAT TATTION IN C	PART DESIGN OF THE COMMENTER OF THE COMMENT OF THE	100001811中央中央中央中央中央中央中央中央中央中央中央中央中央中央中央中央中央中央	OYGHT (C)	C AFORD AND AND STOILLIERS PERFARCH I ABORATORY	いっぱいのことがあっている。このことのことがある。	C FINITE ELEMENT APPLICATIONS TO USAF STRUCTURAL INTEGRITY PROBLEMS	COMMON/TREE	COLUMN CONTRACTOR	CALPET AND HOO	CCO-1 OFFICE AND OFFICE OF	0 10 0 2 1 0 10 0 T 1 25 0	336-1-900 6-010 6-900	CHOUSE CHANG	224=2.010*(30*336	RFTURN	END
	7 4 4	9 10 0	ひに ひに ひい は しい	うせい こく	> 000 000 000 000 000 000		なななない	TATE C	7 1.7									

### C	**** \$UB	SUBROUTINE LMTRX(NODE1,NODE2,THETAI,THETA.RJ.RO.R.RL) ***********************************
AEROELASTIC AND ***********************************	₩ * *	S SUBROUTINE IS USED IN FORMING THE HOLE SUASTRUCTURE OF HOLFL LMTRAGO Barbrararararararararararararararararara
AEROELASTIC AND ********* FINITE ELEMENT & DO 10 1=1.72 DO 10 1=1.72 DOELR=RO-RI OFLR=RO-RI GO TO (1.2.3) RL (2.4) = RL (1.4)	COD	VAIGHT (C) 1975 MASSACHUSETTS INSTITUTE OF TECHNOLOGY
FINITE ELEMENT & DIMENSION PL DO 10 J=1.12 DELTHT=THETA GO TO (1.2.3) = (R-R) PL (1.3.3)	A FI	DELASTIC AND STRUCTURES RESEARCH LABORATORY
10 PENSION PL(2-12) THETAI(2) 10 1 = 1.2 10 D1 J=1.12 10 PL(1.J) = 0.0 10 PELTHTTHETAI(1) - THETAI(2) 10 PELTHTTHETAI(1) - THETAI(2) 11 PL(1.J) = (THETA-THETAI(2)) / I) ELTHT 12 PL(2.2) = RL(1.1) 13 PL(2.4) = RL(1.3) 14 PL(2.4) = RL(1.3) 15 PL(2.4) = RL(1.3) 16 PL(2.4) = RL(1.3) 17 PL(2.4) = RL(1.3) 18 PL(2.4) = RL(1.3) 19 PL(2.4) = RL(1.5) 10 PL(2.4) = RL(1.5) 11 PL(2.4) = RL(1.5) 12 PL(2.4) = RL(1.5) 13 PL(2.4) = RL(1.5) 14 PL(2.4) = RL(1.5) 15 PL(2.4) = RL(1.5) 16 PL(2.4) = RL(1.5) 17 PL(2.4) = RL(1.5) 18 PL(2.4) = RL(1.5) 19 PL(2.4) = RL(1.5) 10 PL(2.4) = RL(1.5) 11 PL(2.4) = RL(1.5) 12 PL(2.4) = RL(1.5) 13 PL(2.4) = RL(1.5) 14 PL(2.4) = RL(1.5) 15 PL(2.4) = RL(1.5) 16 PL(2.4) = RL(1.5) 17 PL(2.4) = RL(1.5) 18 PL(2.4) = RL(1.5) 18 PL(2.4) = RL(1.5)	***	society control and incations to had albicities. Interestations in the control of
0	-	DIMENSION P. (2-12) - THETAI (2)
00 10 J=1.12 PL(I.J)=0.0 DELTHI=THETA GO TO (1.2.3 RL (1.1) = (THE RL (2.2) = RL (1 RL (2.4) = RL (1 RL (2.4) = RL (1 GO TO 7 RL (1.3) = 1.0- RL (2.4) = RL (1 RL (2.4) = RL (1) = RL		[0]=1.2
0		10 J=1.1?
DELTHT=THETA GO TO (1+2-3 RL (3+2) = RL (1) RL (2+2) = RL (1) RL (2+2) = RL (1) GO TO 7 RL (2+4) = RL (1) RL (2+4) = RL (1) RL (2+6) = RL (1)		[+J)=0.0
DELTHT=THETA GO TO (1929) RL (292) = RL (11) RL (292) = RL (11) RL (193) = (R-R) RL (294) = RL (11) RL (294) = RL (11) RL (294) = RL (11) RL (296) = RL (11)		REPORT L'MTRA01
60 TO (1,2,3) RL (3,1) = (THE RL (2,2) = RL (1) 60 TO 7 RL (1,3) = 1,0- RL (2,4) = RL (1) RL (2,4) = RL (1) RL (2,6) = RL (1)		FHT=THETAI(1)-THETAI(2)
RL (3+1) = (THE RL (2+2) = RL (1) RL (3+3) = 1.0- RL (2+4) = RL (1) GO TO 7 RL (2+6) = RL (1) RL (1+5) = 1.0- RL (2+6) = RL (1) RL (2+6) = RL (1)		FO (1,2,3,4,5,6), NODF1 L.MTR301
RL (2.2) = RL (1 RL (3.4) = 1.0- RL (2.4) = RL (1 60 T0 7 = R- RL (2.4) = RL (1 RL (2.4) = RL (1 RL (2.4) = RL (1 RL (2.6) = RL (1)	امعو	[+1] = (THETA-THETAI(2)) / () ELTH7
RL (1+3) = 1.0-1 RL (2+4) = RL (1) RL (1+3) = (R-R) RL (2+6) = RL (1) RL (2+6) = RL (1) RL (1+5) = 1.0-1 RL (1+5) = 1.0-1 RL (2+6) = RL (1) RL (1+5) = (THE) RL (1+5) = (THE) RL (2+8) = RL (1) RL (2+8) = RL (1)		2.0) =RL(1.1)
PL (2,4) = RL (1) GO TO 7 RL (1,3) = (R-R) RL (2,4) = RL (1) RL (2,4) = RL (1) RL (2,6) = RL (1) RL (1,5) = (THE) RL (2,6) = RL (1) RL (2,		[+3]=1.0-RL(1.1)
60 T0 7 RL (1+3) = (R-R RL (2+4) = RL (1) RL (1+5) = 1,0-1 GO TO 7 RL (1+5) = (THE RL (2+6) = RL (1) RL (1+7) = 1,0-1 RL (2+8) = RL (1) GO TO 7 RL (1+7) = (THE RL (2+8) = RL (1) RL (1+7) = (THE RL (2+8) = RL (1) RL (2+8) = RL (1)		2-4)=RL(1-3)
RL (1,3) = (R-R PL (2,4) = RL (1) RL (1,5) = 1,0-1 GO TO 7 RL (2,6) = RL (1) RL (2,6) = RL (1) RL (2,6) = RL (1) RL (2,6) = RL (1) RL (2,8) = RL (1) GO TO 7 RL (1,7) = (THE RL (2,8) = RL (1) RL (2,8) = RL (1) RL (2,8) = RL (1) RL (2,8) = RL (1) RL (2,9) = 1,0-1 RL (2,10) = RL (1)		FO 7 LMTR002
PL (2.4) = PL (1) RL (1.5) = 1.0- RL (2.6) = PL (1) GO TO 7 RL (2.6) = PL (1) RL (2.	۸.	1,3)=(R-RI)/OEL.P
RL (1+5) = 1,0- RL (2+6) = RL (1) GO TO 7 RL (2+6) = RL (1) RL (2+8) = RL (1) GO TO 7 RL (1+7) = (THE RL (2+8) = RL (1) RL (1+7) = (THE RL (2+8) = RL (1) RL (2+8) = RL (1) RL (2+8) = RL (1) RL (2+8) = RL (1) RL (2+10) = RL (1)		2•4)=RL(1•3)
Pt (2.6) = PL (1) GO TO 7 Rt (1.5) = (THE Rt (2.6) = PL (1) Rt (2.6) = Rt (1) GO TO 7 Rt (2.8) = Rt (1) Rt (2.8) = Rt (1) Pt (1.9) = 1.0 Rt (2.10) = Rt (1) Rt (2.10) = Rt (1) Rt (2.10) = Rt (1)		1+5)=1,0-RL(1+3)
60 T0 7 RL (1+5) = (THE RL (2+6) = RL (1 RL (2+8) = RL (1 GO TO 7 RL (1+7) = (THE RL (2+8) = RL (1 RL (2+8) = RL (1		2,6)=9L(1,5)
RL (1.5) = (THE RL (2.6) = RL (1 RL (1.7) = 1.0-1 RL (2.8) = RL (1 GO TO 7 RL (1.7) = (THE RL (2.8) = RL (1 RL (1.9) = 1.0-1 RL (2.10) = RL (1 GO TO 7		ro 7
RL (2.6) = RL (1 RL (1.7) = 1.9 - 1 RL (2.8) = RL (1 GO TO 7 RL (1.7) = (THE RL (2.8) = RL (1 RL (1.9) = 1.0 - 1 RL (2.10) = RL (6	m	1,5)=(THETA-THETA!(2))/DELTHT
RL (2.8) = RL (1 GO TO 7 RL (1.7) = (THE RL (2.8) = RL (1 RL (2.9) = 1.0.1 RL (2.10) = RL (6 GO TO 7		2,6)=QL(1,5)
RL (2.8) = RL (1 GO TO 7 RL (1.7) = (THE RL (2.8) = RL (1 RL (2.9) = 1.0.1 RL (2.10) = RL (1.7)=1.0-RL(1.5)
60 TO 7 RL (1.7) = (THE RL (2.8) = RL (1 PL (1.9) = 1.0-1 PL (2.10) = RL (60 TO 7		2.48) =PL (1.7)
RL (1.7) = (THE RL (2.8) = RL (1 RL (1.9) = 1.0-1 RL (2.10) = RL (60 TO 7		FO 7 LMTR003
2,8)=RL(1 1,9)=1,0- 2,10)=RL(TO 7	ţ	1.77 = (THETA-THETAI(2))/DELTHT
+9}= .n- -10}= R . TO 7		?,8)=RL(1,7)
2+10)=RL (TO 7		1,9)=1,n-RL(1,7)
2		2+10)=RL (1+9)
		ro 7 LMTRa03

```
RL(1+5:3 (THETA-THETAI(2))/DELTHT
            RL (2,10)=RL (1,9)
RL (1,11)=1,0-RL (1,9)
RL (2,12)=RL (1,11)
GO TO 7
                                                                            RL(1.11)=(RO-R)/DELR
RL(2.12)=RL(1.11)
                                                                                                          RL (1,1)=1.0-RL (1,11)
RL (2,2)=RL (1,1)
CONTINUE
                                                                                                                                                        RETURN
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LMTR0037 LMTR0038 LMTR0039

LMTR0036

LMTR0040

LMTRO043 LMTRO044 LMTR0045

[MTR0041 LMTR0042 LMTR0046 LMTR0047

THE REPORT OF THE PROPERTY OF

1	SUBROUTINE MANTRY (NODE1 - NODE2 - RMINT)	MNMT000
	ROUTINE ANMIRY CREATES M AND N MATRICES AND FORMS THEIR PRODUCT	CHECK
	UTINE IS USED IN FORMING THE HOLE SUBSTRUCTURE OF	T000
	水水水水水水水水水水水水水水水水水水水水水水水水水水水水水水水水水水水水	THE WANT OF
	C) 1975 MASSACHUSETTS INS	MAMTOOOS
C AE	IC AND STRUCTURES RESEARCH LABORATORY	
*	· 中国的一种的一种的一种的一种的一种的一种的一种的一种的一种的一种的一种的一种的一种的	DOCLWNW***
I.	APPLICATIONS TO USAF S'	MNMT0008
	MTNT (3,2) + DN (2,3) + RM (3,3)	MNMT0009
	NT/CS+SS+CSS+S3S+CS4+S'	MNMT0010
	REAL NX NY	MNMTOOII
	CSCS=CS*CS	MNMTOO12
	\$\$S=\$\$ * \$\$	001
	\$5CS=\$S*CS	TOOI
	RM (1 • 1) = CSCS	001
	RM(2,1)=SSSS	001
	RM(3+1)=SSCS	100
	RM(1,2)=SSSS	0
	RM(2,2)=CSCS	7
	Ç	005
	C	TOOS
	$\overline{}$	005
	(V)	005
<u>ت</u> د	DARY SEGMENT	1002
	EG. 6 .AND. NODE2 .EG. 1) GO TO 4	1002
	EO. 1 .AND. NODEZ .EQ. 2) GO TO 1	7002
	EG. 2 .4MD. NODE2 .EG. 3) GO T	1002
	GE. 3 .AND. NODEZ .LE. 6) GO TO 3	T002
10	NX#1.0	00
	9	
	•	TOO
20	NX==SS	3
	=CS	T003
	2	MNM 10034
30	NX##CS	MNMT0035

MNMT0038 MNMT0039 MNMT0040 MNMT0041 MNMT0049 MNMT0050 MNMT0043 MNMT0044 MNMT0045 WNMT0046 WNMT0047 WNMT0048 MNMT0036 MNMT0037 MNMT0052 MNMT0051 PPINT (I.-J) =RMTNT (I.-J) +RM (K.I) +RN (J.K) RN(2.1)=0.0 RN(2.2)=NY RN(2.3)=NX DO 60 1=1.3 DO 60 J=1.2 RMTNT(I.J)=0.0 RN(1+1)=NX PN(1+2)=0.0 RN(1+3)=NY GO TO 50 NY=-1.0 0.0=XN RETURN NY=-SS END

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APPENDIX C

TEST MAIN - CONTRACT 81739 PROBLEMS 1 & 2	PAN0001
3	PANOOO3
IC AND STRUCTURES RESEARCH LABORATORY	PAN0004
中国中国中国的中国中国的中国中国中国的中国中国的中国中国的中国中国的中国的中国的	PANOCOS PANOCOS
	PAN0007
	PAN0008
I TIDIA LENGIA TAK SIFFCI, PRESS, RI, 10FFST	PAN0009
	PANOOLU
	PAN0011
(315) x12x17	PANOOIZ
FINITIONS OF INPUT VARIABL'Ssammannennennennennennennennennennennennenne	PAN0013
WIUTH OF PLATE:	PAN0014
HICKNES	PAN0015
FARFIELU LUADING! R	PANOU16
= UFF SET INUICATOR;	PAN0017
= LENGIH	PANG018
= FINAL POSITION OF CAACK ONE; E = YOUNGS MCDULUS	PAN0019
AU = PGISSONS RATIOSKI =	PAN0020
	PAN0021
T3 = PRINT CO	PAN0022
*********	PANGOZ3
DIMENSION RFF (10000) + IFF (10000) + REAL (800U) + INTGR (8000) + RRNG (12000)	PAN0024
I KNG (1200	PAN0025
ANGLE (2+2)	PAN0026
KEAL LENGT	PAN0027
INTEGER CNODE PRINTS	PAN6028
COMPON/10/KR+K++KP+KT1-KT2+KT3	PAN0029
VIS/NOWWO	PAN0030
S AW/NOWWO	PAN0031
COMMON/FIDAL CON-11 KOUNT - LINZ - LMASTR - LG - LK	PAN0032
COMMON/SIZES/NETSS NOTSS NIDSS	PAN0033
	PANCO34
COMMON THE PROPERTY OF THE	PAN0035
COMMON/K (ACCR (A. C.	PAN0036

EQUIVALER (TEND(1) DATA MSZI	uce (RFF(1), IFF(1)), (REAL(1), INTGR(1)), (IBEGIN(1), ICON), LCON), (ISZ(1), NET), (ISZSS(1), NETSS), (RRNG(1), IRNG(1)) F/10000/,NSZRNG/12000/,NSZMN/8000/ 3.141593/,S/1,0,3*0.0,1,0,4*0.0/,C/1.0,3*0.0,1.0,4*0.0/	PAN0037 PAN0038 PAN0039
(A)		PAN0041
DTHETA	1/12.0	PAN0043 PAN0044
#IdixBS		PAN0045
Ž	20003	PAN0046 PAN0047
SOOO FORMAT	(6E10.3+IS)	PAN0048
SOO! FORMAT	10.13.215)	PAN0049
	5002) E.GNU	PAN0050
SOOZ FORMAT	E10.3)	TANCOURT
	5003) KT1•KT2•KT3	PANCOSC DANOGS 3
5003 FORMAT	15)	
	1)=(1605(1)-1)41200	
ANGLE ()	(2) = (1) + (2) =	PANOONS
ANGLE (2	1) = ANGLE (191) + 180 = 0	PAN0057
ANGLE	Z) = ANGLE (1, Z) + 180 • U < 2.0.0 > = 1011 = 1	PANOOSE
	-66000) #IDINSENCTION # 1 739. //57X. 18HPROBLEMS NO. 1 & 2.//6	PAN0059
))	NO. I FIGTS -// 16H PLATE GEOMETRY: . // 13H PLATE WINTH= , E12.	PAN0060
m5./.144	PI ATE ENGTH= . E12.5./ . 17H PLATE HICKNESS= . E12.5. / . 24H PLA	PAN0061
WTE STIF	ENER FACTUR=.F8.3./.25H FAR FIELD LOADING (PSI)=.E12.5./.1	PANO062
BEH RAD	IS OF HOLE=,E12.5,/,23H HOLE OFFSET INDICATOR=,I3,27H(=0, H	PANGOOS PANGOOS
#OLE RE	INS CENTERED) +//+ICH CRACK DATA: +//	PAN0065
DI VXVX		PAN0066
c	. (1 . 0 . 0 . NCRK = NCRK + 1	PAN0067
	**************************************	PAN0068
'n	1.500	PAN0069
6001 FORMAT		D D D D D D D D D D D D D D D D D D D
EAL CKA	P05	PAN0072

ž) E.GNU JERIAL PROPERTIES: . // . 20H YOUNGS MODULUS	(E)=•E12.5•/	PAN0073
	#.16H POISSONS RATIO=+E12-5-///)		PAN0075
	CALCULATE S&C MATRICES:		PANOOTO
	C(Z•1) =GNU		PAN0077
	C(3+3) = (1,6-6NU)/2.6		PAN0078
	S(2+1) =-6NU		PAN0079
	S(3,3)=(1,0+6MU)*2,0		PAN0080
	SMU=E/(2.0*(1.0+6NU))		PAN0081
	ETA=(3.0-GNU)/(1.0+GNU)		PAN0082
	0		PAN0083
	00 20 1=1,3		PAN0084
	00 20 Jzj.I		PAN0085
	-		PAN0086
	(C+I)≤=(I+C)S		PAN0087
			PAN0086
20	((1,1)=((1,1)		PAN0089
ပ	DETERMINE NUMBER OF GUADRILATERALS NEEDED ACKOSS WIDTH:		PAN0090
	NELW=WIDT=/(4.0+RI)		PAN0091
ပ	INSURE THAT NELW IS EVEN VALUED:		PAN0092
	I =NELW/2		PAN0093
	2+I#I		PAN0094
	IFINELW ONE. I) NELWERELW-1		PAN0095
	Z*ZIOTX/NELZ		PAN0096
	RATIOHE/KI		PAN3097
ပ	DETERMINE STIFFENER THICKNESS:		PAN0098
(STF TIKHUIK+SIPPOT #INDIT #IND		PAN0099
	CENTER NODE REFERENCE (INPUT FOR SUBROUTINE CZONE):		PANO100
	CNODE=NEL#/2+1		PANOIOI
	Z=1IWIT		PAN0102
			PAN0103
	ENTER OF PLATE. IF		PAN0104
ပ	LL BE MOVED TO THE RIGHT	IN INCREMENTS 0	PAN0105
	FAR AS IS POSSIBLE		PAN0106
			PANOI07
	PRINT OUT PROGRAM STATISTICS TO DATE:		PAN0108

FFIRTI "EG. KW) GO TO 30 WRITE(KW+6003) NELW+W-RATIO.CNODE.STFIHK.SMU.ETA BOTHW-1(20H0PKGGRAM STATISTICS:.//.33H NUMBER OF ELEMENTS ACROSS WI BOTHW-14./.27H QUADRILATERAL DIMENSION WF.+12.5./.30H HOLE ELEMENT WOIMENSION RATIO=*F8.3*/.23H CENTER NOUE KEFERENCE=:14./.21H STIFFE WNEW THICKNESS=*E12.5.//.21H MATERIAL PARAMETERS:./.5H SMU=.E12.5./ WSH ETA+.E12.5.//.10H S MATRIX:./)	H 141 S
#KITE(K#+6004) (C(I+J)+JF1-3) #RITE(K#+6005) 6005 FORMAT(10HOC MATAIX:) 40 CONTINUE	
E=0.0 C QBIAIN FAR FIELD SUBSTMUCTURE (CHESIRE CAT): 32 CONTINUE PRNTSV=KT1 KT1=KT2 RO=(1.0+DTMETA)****R	PANO122 PANO123 PANO124 PANO124 PANO125
INDCINEU CALL FARFLD (WIDTH.LENGTH.NELW.THK.STFTMK.C.S.CNODE.RO.PRESS,INDCTR W.NSZFF.RFF.IFF.NSZMN.REAL.INTGR) JLOC=IPOS(1) KTI=PRNTSV DO 35 [=1.3	TR PANOLZ9 PANOLZ9 PANOLZ1 PANOLZZ PANOLZZ PANOLZZ
ia ia	PANOIJS PANOIJS PANOIJS PANOIJS
IPNTR#2*NCRK+146 CALL SETUP(NSZMM+1+IPNTR*REAL+INTGR) C SET UP ASSEMBLY LIST: C ELEMENT NU+ 1 IS THE FAX FIELD SUBSTRUCTURE (CHESIRE CAT) IPNTR=IMASTR+2	PANOI41 PANOI41 PANOI42 PANOI44

PAN0145	PAN0146	PAN0147	0148	0149	0150	0151	0152	0153	10154	0155	0156	0157	PAN0158	0159	0160	PAN0161	0162	0163	PAN0164	0165	PAN0166	0167	0166	0169	0110	_	0172	- 1	_ !	<u> </u>	0176	<u> </u>	<u> </u>	<u> </u>	2010
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15X+1615+/+25X+1615+/+25X+1615+/+25X+1615)
                                                                                                                                                                                                                                                                                                                                    OBTAIN CHACKED HING INTERIOR UISPLACEMENTS:
                                                                                                          COMPUTE AND ASSEMBLE CRACKED RING ELEMENTS
                                                                                                                                                                                                                                                     CALL ASMOUB (2.RHNG. IRNG. KEAL. INTGR)
                                                                                                                                                                                                                                                                                                                                                  CALL DBACK (2.8RNG. IMNG.REAL. INTGR)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            CALL ATRACT (1+18+18+EL11+RHIG+ HNG)
                             ASSEMBLE FAR FIELD SUBSTRUCTURES
                                                                                                                                                                                                                                                                                                                    SIMULO (GNU . REAL . INTOR)
                                                                                                                                                                                                                                                                                                                                                                  60 TC 120
              CALL OAK (NSZEN, REAL, INTGA)
                                                                                                                                                                                                                                                                                                   CALL FACT (1. REAL . INTGR)
                                                                                                                                         THICKAR (JLUC-1) *DIMETA
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                                                                                             (I) #190EE (I)
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100 RKIJ) =RK(J) +BCKK([.J.K) +ELQ(K)		PAN0217
165 BK(J) BEK(J) SORTAL		PANOZIY
など、ハンドとひり、スト、ハン・フェンのない。これに、「なべ、」、コー・コー・ジン・コー・コー・コー・コー・コー・コー・コー・コー・コー・コー・コー・コー・コー・		PANONNI
I 3	KI=+E12.5.FH	KII PAN0222
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* にこてのよだ		PANOZZA
Ÿ		PANG225
120 JLCC=JLOC+1		PAN0226
00 182 1#1.0		PANG227
I) = 1 SAVE (!)		PAN0226
į.		PAN0229
C INCREMENT HOLE POSITION:		PANOZBO
IF (10FFST .Eq. 0) 60 TO 130		PANOZ31
41. 300		PANO232
Ext. • a		PAN0233
CNODE #CNODE 1		PAN0234
ERITE (N#+6011) E		PAN0235
6011 FORMAT(121,538,24m INCLEMENT MOLE POSITION	JN.//.54X.13HHOLE OFFSET	# PAN0236
(///:3-7//)		PAM0237
		PANOZBE
130 CONTINUE		PANO239
STUP		PANOS40
END		PANOZ41

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SUBROUTINE LUG(WIDTM.LENGTM.MELW.THK.STFTHK.C.NSIZE.RSS.1SS) SUBROUTINE LUG GENERATES A RECTANGULAR REGION WHICH IS USED BY	SBL AND OBL Programme of the composition of the com	COSYRIGHT (C) 1975 WASSACHUSETTS INSTITUTE OF TECHNOLOGY	ABROST ASTIC AND STRUCTURES BESSARCH TABORATORY	FINITE ELEMENT "PPLICATIONS TO USAF STRUCTURAL INTEGRITY	DIMENSION PSS(1) - 155(1) - C(3,3) - FLX (36) - FLXSTF(3		REAL LENGTHAL	CONTOUR SEARCH SEARCH SEASON S	Č1	COMMON/BEGIN/ENCINES	うしまなのまった。このでは、このとなら、このとのでは、このとのでは、このとのでは、このとのでは、このとのでは、このとのでは、このとのでは、このとのでは、このとのでは、このとのでは、このとのでは、このとのでは、このとのでは、このとのでは、このでは、このでは、このでは、このでは、このでは、このでは、このでは、こ	56(6)	COMMON/STOSS/ SIS.01.8STF(3.0)	DATA TEMP/4+0.0/	00 % [x],12	S C00PD(11) #0.0	# 13X/MIGIRAL	AP#5.0	NELL RIENGTH/ (W. A.G.) + 1	TARTIST TO THE TARTE TO THE TAR		SOL + LOS +		CHEST CONTRACTOR	LELFNOTHANGL	Wat/1mg	C00000	T# (%) @6000

0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	COORDISTEL COORDISTEL COORDISTEL LMASTPENDW-2 IF (KII = 60. KW) GO TO 10 WRITE (AW-500U) WINTH-LENGTH+IMK+SIFIHK+NELW WRITE (AW-500U) WINTH-LENGTH+IMK+SIFIHK+NELW WRITE (AW-500U) WINTH-LENGTH+IMK+SIFIHK+NELW WRITE (AW-500U) WINTH-LENGTH+FEIS-S-15H LUG THICKNES-FIZ-S-LUG WRITE (AW-500U) WINTH-IMMS SERVERS SE	00000000000000000000000000000000000000
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30	LNODE1=LNODE1-1 IMASTR=IBEGIN(4) +NET LMASTR=IMASTR+NELW*8 INODE1=HDT-2*NDW+1 LNODE1=1 DO 35 I=INODE1.NDT DO 35 I=IMASTR+LMASTR FECTIVE		0072 0073 0075 0075 0076
900 900 900 900	10 60	907	0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0
6002	FORMAT(22HOMASTER ASSEMBLY LIST: 1/4,18H ELEMENT POINTERS: 1/1) IMASTR=IBEGIN(4) LMASTR=IMASTR+NET-1 ELNO=0		0000 0000 0000 0000 0000
40 6003	DO 40 I=IMASTR.LMASTR ELNO=ELNO+! WRITE(xw.6003)FLNO.ISS(I) FORMAT(13H ELEMENT NO.=*I5*13H POINTCR=:I5) IMASTR-LMASTR+I	900000000000000000000000000000000000000	2000 2000 2000 2000 2000 2000 2000 200
004	WYIECKW,5004) FORMAT(17H0ELEMENT D.O.F.S:,/) 50 59 I=1,NET LMASTR=IMASTR+7 WRITE(KW,6005)1,(ISS(J),J=IMASTR,LMASTR) FORMAT(12H ELEMENT NO.,I3,13H TWASTR-IMASTR,		20000000000000000000000000000000000000
	CALL URK(NSIZE,RSS,ISS) CALL URK(NSIZE,RSS,ISS) CALL QUAD4(COORD,THK,TEMP,C,0,ND,ANGLE,ELQ,ELK,B,1,KW) AR=STFTHK/THK		01000
70	ELKSTF(I)=ELK(I) *AR 50 80 I=1.3 50 80 J=1.9 8STF(I.J)=8(I.J) *AR		المحمد المحمد المحمد المحمد ا

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	NEINE SENE NO.	בסב	
	ELN0=0	907	
	DO 100 IROW=1.NELL	907	
		907	
		907	
	IF (NELWM) .LT. 2) 60 TO 92	507	
		ອີກສ	
	ELNO=ELNO+1	507	
06	CALL ASMLTV (ELNO.8) ELK.F.O.RSS.1SS)	e UG	
W		507	
100		90.1	
	•	90.1	
	IMASTR=IBEGIN(5)~1	507	
	DO 110 I=1+[MASTR	100	
	[2S(I)=I	507	
110	RSS(IMASTR+1)=0.0	907	
	CALL BCON (RSS+ISS)	503	
115	34	าด	
	CALL STACON(I.NIDSS.RSS.ISS)	507	0126
	D0 120 1=1.6	907	
120	186SS(1)=18E6IN(1)	567	
	NETSSENET	30.1 10.0	
	NOTSSENDT	907	
	IF(KT1 .EO. KW) GO TO 130	550	
	≱61116 (★3•6006)	907	
6006	FO	907	
0	CONTINUE	<u>ອ</u> ຄ າ	
	RETURN	196	
	END	50.J	0136

	SUBROUTINE CZONE(WIDTH+NELW)THK+STFTHK+C+S+CNOD5+RI+NSIZE+RCZONF+ CZM 00	000
*	3) NNU市市市的市场的企业中的企业中的企业中的企业企业企业企业的企业企业的企业企业企业企业企业企业企	> •
	GENERATES THE CENTRAL STRIP THAT CONTAINS THE HOLE CZN O	0
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r	0 NZO	20
	0 NZU	2
	0 NZO	8
	0 PZU 5	2
	CZN O	2
6008	SUBROUTINE CZONE **CZN 0	2
	.14,35H IS OUT OF RACZN O	20
	NGE OF E WIDTH (NELW).,/.44H CNODE MUST BE GPEATER THAN I AND LESSCZN 0	6
	THAN . 14.//.53H **** EXECUTION TERMINATED IN SUBROUTINE CZONE **CZN 0	33
	6 NZO	5
•	CZN	(C)
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                                                                                                                                                                                                                                                                         MH PLATE WINTH=, E12, 5, /, 33H NUMBER OF ELEMENTS ACROSS WINTH= . I4 . /, 1C2N
                                                                                                                                                                                                                                                        FORMAT(1H1.59X.11HENTRY CZONE.///.23H SUBROUTINE INPUT DATA:.//.13CZW
                                                                                                                                                                                                                                                                                         87H PLATE THICKNESS=.E12.5./.21H STIFFENEH THICKNESS=.F12.5./.28H HCZN
                                                                                                                                                                                                                                                                                                         MOLE CENTER NODE REFERENCE= 13./ 27H HOLE ELEMENT INPUT RADIUS= FIREZ
                                                                                                                                                                                                                                                                                                                                            WRITE(KW.60nl) NDW.NIDSS.(NOTASM(I).I=1.4).(IELSTF(I).I=1.4).(COOPCZN
                                                                                                                                                                                                                                                                                                                                                                          6001 FORMATI29HOSUBPOUTINE CZONE STATISTICS: , 1/1, 30H NUMBER OF NONES ACRCZN
                                                                                                                                                                                                                                                                                                                                                                                            80SS WIDTH=,14,7,75H NUMBER OF INTERNAL D.O.F.S TO BE CONDENSED OUTCZN
                                                                                                                                                                                                                                                                                                                                                                                                             GLOBAL STIFFNESS MATRIX=+14+/-30H FLEMENTS NOT TO BE ASSEMBLEDCZN
                                                                                                                                                                                                                                                                                                                                                                                                                             9: +415 - / +26H ELEMENTS TO BE STIFFENED: +415 - / +21H ELEMENT COOPDINATECZN
                                                                                                                                                                                                                                       WRITE(KW.6000) WIDTH.NELW.THK.STFTHK.CNODE.RI
                                                                                                                                                                                                                                                                                                                                                                                                                                                               CALL SETUPINSIZE, 2. LMASTR. RCZONE, 1CZONE)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     (CZONE (IMASTR+ELNO) = IPNTR
                                                                                                                                                                                                                       [F(KT] .EQ. KW) GO TO 10
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   IPNTR=IMASTP+NET+ELN0*8
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 IF (IROW .EO. 2) INODE=1
                                 NOTASM (3) = CNODE - 1 +NELW
                                                  NOTASM (4) = CNODE+NELW
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    DO 20 I=INODE, LNODE
                                                                                                                                                                                                      LMASTR= (NET-1) #9+65
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 LNODE=INODE+NELW-1
NOTASM (1) =CNGDE-1
                                                                                                                    [ELSTF (4) =2*NELW
                                                                                    [ELSTF(2)=NELW+]
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              [MASTR=IBEGIN(4)
                 NOTASM (2) = CNODE
                                                                                                  IELSTF (3) =NELW
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  DO 30 IROW=1.2
                                                                                                                                                                                                                                                                                                                                                             (D(I) • I=1 • 12)
                                                                     IELSTF(1)=1
                                                                                                                                                                                       COORD (10) =W
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                [NOOE=NOM+]
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     ELNO=FLNO+1
                                                                                                                                                     COORD (2) #3
                                                                                                                                    C00PD(1)=W
                                                                                                                                                                       C00RD (5) #W
                                                                                                                                                                                                                                                                                                                                                                                                                                              MS: 12F8,3)
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	TCZGNE (1PNTR+1)=1+2	0
	ICCONE (IFMIK) = ICCONE (IFMIK+I) = I	0 (
•	A LI NI LIT	3 (
20	ICZONE (IPNTR+3) = ICZONE (TPNTR+2) +1	00
	LNODE=ND#	00
	IF(IROW .Eq. 2) [NGDE=3*NDW	0
		00
	ICZONE (IPNTR+5) =LNODE*2	00
) = ICZONE (IPNTR+5)	00
	ICZONE (IPNTR+6) = ICZONE (IPNTR+4) -2	00
) = ICZONE (IPNTR+6)	00
	IPNTR=IPNTR-8	00
30	LNODE=LNODE-1	00
	IDOF (1) =CNODE-1+2*NDW	00
	IDOF (2) = CNODE-1	00
	I DOF (3) = CNODE = 1 + NDW	00
	IDOF (4) =CNODE+NDW	00
	100F(5)=CNODE+1+NDW	00
	100F(6)=CNODE+1	00
	IDOF (7) = CNODE + 1 + 2 * NDW	00
	IDOF (8) =CNODF +2*NDW	00
	IPNTR=IMASTR+NET+16*NELW	00
	ICZONE(IMASTR+NET-1)=IPNTR	00
	INODE=1	00
	00 40 1=1•8	00
	NODE) = I	00
	NODE-	00
40	INODE=INODE+2	00
	IPNTR=IPNTR+16	0
	INODE=2*(3*NDW+1)-1	01
	LNODE=INODE+47	0
	00 50 I=INODE+LNODE	01
Ċ	CZONE	0
λC	•	70
	IF(KII *EQ* KW) GO TO 80. BRITE(KW*6602)	CZN 0106
		4

6007	FORMAT(22HAMASTER ASSEMBLY LIST: "/". IRM FLEMENT BOINTERS: "/	0.0
)))		010
	LMASTR=IMASTR+NET-1]
	ELNO=0	011
	DO 60 I=IMASTR-LMASTR	0
	ELNO=ELNO+1	011
0	WRITE(KW.6003) ELNO.1C2ONE(I)	011
0	FORMAT(13H ELEMENT NO.=+15+13H POINTER=+15)	CZN 0115
	IMASTR=[MASTR+]	011
	FRITE (XX+6004)	011
6004	FORMAT(17H0ELEMENT 0.0.F.S: 1)	011
	IPNTP=NET-1	011
	DO 70 I=1.jpwTP	012
		(VI
	NE () . J= IMAS	012
6005	FORMAT(12H E! FMENT NO. 15,13H D.O.F.S: 415)	012
0	IMASTR=IMASTR+9	012
	LMASTR=IENn(4)	012
	IMASTR=LMASTR-63	012
	E(J) . J=IMASTR.LMAS	012
6006	FORMAT(22HNHOLE ELEMENT D.O.F.S:./.R(1H ,21X,815,/))	012
0	102	012
	CALL QUAD4 (COORD , THK . TEMP , C . 0 . ND . ANGLE . ELQ . ELK . B .] . KW)	013
		013
	DO 96 I=1.36	013
06	FLKSTF(I)=FLK(I)*RATIO	~
	00 100 1=1,3	013
	no 100 J≈1•9	013
100	BSTF(I,J)=8(I,J)*RATIO	013
	IPNTR=NET-1	013
	DO 140 N=1.IPNTR	013
		013
	IF(N .EQ. NOTASM(I)) GO TO 140	014
110	CONTINUE	14
	•	014
	IF(N .EQ. IELSTF(I)) GO TO 130	014

120	CONTINUE	0
	CALL ASMLTV(N,8,ELK,ELQ,RCZONE,ICZONE)	C
	0 140	0
130	CALL ASMLTV (N, 8, ELKSTF, ELQ, RCZONE, ICZONE)	0
140	CONTINUE	0
	50 1	C
150	(1)	0
	0(1)=2.	0
	D(4)=C0	C
	012:=00	C
	0(8)=00	C
	TREK	C
	X	C
	ĭ	0
	IMASTR	C
	ASMSUB	0
	NE (1) =C	0
	NE (2) =]	C
	TR=18EG	C
	1=1 09	C
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160	NE ()) =0	C
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84 PLATE WINTH=.F12,5./.14H PLATE LENGTH=.E12.5./.33H NUMBFR OF ELEFFD
                                                                                                                FFD
               MMENTS ACROSS WIDTH=.15./.17H PLATE THICKNESS=,E12.5./.21H STIFFENEFFD
                               BP THICKNESS=+E12.5+/.33H HOLE CENTER NODE REFERENCE CODE=+15./.27HFFD
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                                               & HOLE ELEMENT INPUT RANTUS=,E12.5./.Z6H APPLIEN TENSION PRESSURE=,FFD 4612.5./.31H STATIC CONDENSATION INDICATOR=,14.37H (INDICATOR=0:FFD
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                                                                                FCHESIRE CAT PROBLEM: 1.39x . 73H INDICATOR . I PLATE WITH END NODES ANFED
                                                                                                                               FORMAT (234nSUBROUTINE STATISTICS: . //. 12H LUG LENGTH=. F.12.5. /. 13HHOFFD
                                                                                                                                            BLE OFFSET=.F12.5./.75H NUMMER OF INTERNAL D.O.F.S TO BE CONDENSED FFD
                                                                                                                                                                                                                                                                044
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                                                                                                                                                               BOUT OF GLOHAL STIFFNFSS MATRIX= 15,//)
                                                                                                #D WITH HOLE-NO LOADS OR B.C. APPLIED))
                                                                                                                                                                              SETUP (NSI 7E . NCON . LMASTR . PSS . 155)
                                                                                                                                                                                                                                                                                              IF ( N .EQ. 2) IOOF [= (2-NOW-1) +2-1
                                                                                                                                                                                                                                                                                                              IF ( N .EQ. 2) TOOF 2= (NOW+1) *2-1
                                                                                                               WPITE (KW. 5001) LNGTH.F. NIDSS
                                                                                                                                                                                                                                                                PNTREIMASTO+NET+ (N-1) +4+NOH
                                                                                                                                                                                                                                                                               [55 ([HASTR+N-])=[PNTR
                                                                                                                                                                                                                                                                                                                               LMASTP=100F1+2+NDW-1
                                                                                                                                                                                                                                                                                                                                              DO 20 I=IDOF1.LMASTR
                                                                                                                                                                                                                                                                                                                                                                                                               DO 30 I=IDOFZ-LMASTR
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              30 40 I=IBOF1.LMASTR
                                                                                                                                                                                                                                                                                                                                                                                              MASTR=100F2+2+NOW-1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                SS(IMASTR+2)=IPNTR
                                                                                                                                                                                                                                1-(1-MUN-2=2=(30)01
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 DOF 2 = (NOW - 1) -2-1
                                                                                                                                                                                                [MASTR=IBEGIN(4)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                | DESTRETENTE . I
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                                                                                                                                                                                                                                                                                                                                                                                                                                                | PNTR= | PNTR + |
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                                                                                                                                                                                                                                                                                                                                                              (SS (IPNTR)=1
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                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 MANUFALA BANDE
                                                                                                                                                                                                                                               DO 30 N=1.2
                                                                                                                                                                                                               10051=1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                DOF 1=1
                                                                                                                                                                                CALL
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	DOF 2=100F1+47	٥	
	0 60	0	
	3S (1P)	0	
9	PNTR=	0	
	F (K11	0	
	DOF1=19EGIN(0	
	DOF2=100F1+2	0	
	AITE(KW.5002) (ISS(I), I=100F1.100F2)	FFD 0083	
200S	DAMATIZZHOMASTER ASSEMRLY LIST:./.	0	
	0 70 N=1.2	0	
	DOF 1 = 1 REG 1 N (0	
	00F2=1	0	
	AITE(KK-6003) N	0	
	DRMAT(13HOLUG ELEMENT , 12,9H D.O.F	0	
70	#11E(KW+6004) (ISS(I)+I=	0	
	DREAT	0	
	00F1=1	0	
	JOF 2=1	0	
	FIFE (KW-6000)	0	
5003	DRMATIZSHOCZONE ELEMENT D.O.F.S:./	0	
	AITE(KW*6004) (155(1).1×	0	
80	ALL ORKINSIZE . RS	0	
	10SV=h	0	
	06 0	0	
00	SAVE 1 (0	
	0 100 I=1.6	0	
	SAVE2(1)=18E	0	
100	SAVE3(1) = IEN	0	
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110	[SZ(1)=]SAVF1(1)	_	
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                                                                                           CALL CZONE (#1014.NELW.THK.STFTHK.C.S.CNODE.R1.NSZWRK.RWORK.TWORK.
                                                                                                                                                                                                                   IF (INDCTR .FU. 0) GO TO 190
ATE #ITH END NOGES AND HOLE-NO R.C. OR APPLIED LOADS
                                                                                                                                                                                                CALL ASMSUR(3.PMORX.14784.RSS.1SS)
                               CALL ASMSINGRANDORX - IMORX - RSS-155)
                                                                                                                                                                                                                                                  $100011.NEOSS.485.185
                                                                                                                                                                                                                                                                                                                                  DO 200 1=100F1.100F2.2
19EGIN(1)=15AVEZ(1)
                                                                        ISAVEZ(1) = IREGIN(1)
                                                                                                                                            IBECIN(I) = I < AVE ? (I)
                                                                                                                                                                 (1)$S581=(1)5$59#I
                                                                                                                                                                                      152525111=1525251
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                                                                                                                                                                                                                                                                                          2. (1. MUN-2) = 1 4001
                                                                                                                                                                                                                                                                                                                                                      RSS (L MASTR+1) =0.0
          [END(1) = [ SAVE 3(1)
                                                                                ISAVE 3(1) = [ELAD(1)
                                                                                                                                                                                                                                                                    CHESIBE CAT PROBLEM
                                                                                                                         (1) t30481=(1) 251
                                                   15AVE1(1) = 197(1)
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                                                                                                                                                                                                                                                                                                                                            [55([MASTR)=[
                                                            9-1=1 051 00
                                          Sel 140 141.2
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                     00 130 N=1.2
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                                                                                                                      485 (LM45TD+100F1+2) #855 (LM4STR+100F1+2) +F
                                                                                                                                 855 (1 mastr - 170f 2 - 21 = RSS (1 mastr - 100f 2 - 2) of
                                                                                                                                             ASSILMASTR - 100F? 1-8855/LMASTR + 100F?
                                                                                                            1 # B S S ( | M & S T B + 1 D O F )
                                                                                                                                                                                                                                                                     FORMAT (120.54x.) LACKIT FARFLD.///
                                                                                     RSS (LMASTR+1+2) sRSS (LMASTR+1+2)+F
                                                                                                0.5/22740.Ke
                                                                           PSS (LMASTR+1) RBSS (LMASTR+1) +F
                                                                                                                                                                              STACON (1.N10SS.4SS.1SS)
                                                                                                                                                                                                                                               IFT KT1 .FO. KW 1 GO TO 230
1-2+(3/MON+1+MON+2) #1 JOG
                                                                00 210 Te100F1.100F2.2
                                                     まもびびがたいの・レスス/ジ・0
                    RSS (LMASTR+IDOF) 1=0.0
                                                                                                                                                       CALL BCONIRGS. 1551
                                                                                                                                                                                                                                   (1) MIDJUIT (1) SSUBI
                                                                                                            RSS (LMASTR+100F)
          ISS (IMASTR) = INOF!
                                                                                                                                                                                                   15755(1) = 157(1)
                                                                                                アカーのサゲーエ系・レエス)
                                                                                                                                                                                                                                                          WATTE (KW. 6006)
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                                100Flx6.vDx.2
                                          2-#UN-8=2 1001
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SUBROUTINE ARCA(RIMMED.THETAI.DIMI.C.TMK.ELKI.RSS.ISS.ISI7E.IMEGINARC40000	ARC40000
	48C40002
C SUBROUTINE ARCA SUPPLIES THE 150 DFFARE ARC SUBSTRUCTURE USED IN	ARC40003
	ABC40004
C AEROELASTIC AND STRUCTUPES DESEARCH LABORATOHY	APC40006
C COPYRIGHT (C) 1975 MASSACHURETTS INSTITUTE OF TECHNOLOGY	APC4007
· () () () () () () () () () () () () ()	APC40008
C FINITE ELEMENT APPLICATIONS TO USAF STRUCTURAL INTEGRITY PROBLEMS	ARC&0009
・ 1911年によりには、1911年により、1911年により、1911年には、1911年によりには、191	ARC40010
#NODE (4) . COOMD& (19) . [SAVE 1(2) . [SAVE 2(6) . [SAVE 3(4)	ARC40012
6) • [EXPO (4) • NIG (4) • SNG (5) F. (4)	ARC40013
CLEENSION F. G.A. a. (3.4)	ARC40014
OATA EOCHD4/12*0.0/.18*04/406.0/	48C40015
COSECUL/LO/LO.KX.FG.KHI.KHW.KHW	48C46016
COMMON/S175/157(?)	ARC40017
(%) 081/81018/208800	48C40C18
COMMON/S ND/IND (6)	ARC40019
C SAVE CALLING PROGGAM CONTROLS	ARC40020
	ARC40021
	ARC40022
	ARC40023
	4RC40024
	ARC40025
	ARC40026
011=12) 251	ARC40027
\$1000£	APC40028
	4FC40029
	ARC40030
	1500234V
	ARC40032
	APC40033
NOTE 11 255	0400
NODE (2) = 5%.	ARC40035

DO 40 Nat 10	24003
	04003
30 [EN-(1) 251-315E [13104]	ARC40038
Ž	24003
ISS (TOWN) BIPNIE	04004
1814 NE. 11 GO 10 20	04004
NOWE (3) #27	24004
800 (4) 300 N	50050
GO TO 40	24004
18 (W. ME. 10) 60 TO 30	24004
400 (1) a 3 a	40040
NOOF (4) = 37	40040
00 10 40	40040
NOOE (3) EMOOF (2) +3	04004
1 • (1) 3000 (7) 500W	C4005
	24005
20 50 50 50	20070
1-2-1-01M91=00V1	04005
100F=MCDE (1) @?	C4005
[SS([ADD-1)=[00F-]	C4 n 0 S
155(1400)=1007	24005
NOOE (1) = NOOF (4)	C4005
	C4005
NOOE (1) 300N	C4005
NODE (2) =53	C4006
00 110 W=11.20	C4008
ionidate.	C4006
1	04006
STATE CHARGES	C4006
THIS WE NOT 1 50 TO 70	90070
1100E (3) = 26	04006
75 (4) 377	C400 6
50 TC 90	24006
18 (N .ME. 20) 60 TO AD	C4006
MODE (3) = 39	C4007
k(CDE (4) ≈38	C4007

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RRRRRRRRRRRRRRRRRRRRRRRRRRRRRRRRRRRRRR	XXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXX	7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7	ARC40097 ARC40098 ARC40100 ARC40102 ARC40102 ARC40103 ARC40103
GO TO 90 NODE (3) =NODE (2) -3 NODE (4) =NODE (1) +3 CONTINUE DO 100 I=1,4 IADD=IPNTR+I*2-1 IDOF=NODE (I) *2	1 1 m 0 2	ISS(IDWMY)=IPNTR IF(N .NE. 21) GO TO 120 NODE(3)=25 NODE(4)=26 GO TO 140 O IF(N .NE. 30) GO TO 130 NODE(3)=40 NODE(4)=39	0 NODE(3)=NODE(2)-3 NODE(4)=NODE(1)-3 CONTINUE DO 150 I=1+4 IAOD=IPNTR+I*2-1 IOOF=NODE(7)*2 ISS(IADD-1)=IDOF-1 0 ISS(IADD)=IOOF NODE(1)=NODE(3)

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αc	C4033
Z *	C4011
	C4011
F(N .NE. 31) 60 TO 151	C4033
	C4011
(0)E(4)=25	54011
0 10 162	C4011
F(N .NE. 40) 60 TO 1615	C4033
100E (3) =41	C4011
000 (4) = 40	C4011
30 10 162	C4012
-(2)	21093
100E (4) =N0DE (1) -3	C4612
	C&012
0 163 1=1,4	C4012
•	54012
4	C4012
	C4015
Ç	C4012
~	C4012
•	C4013
2F 9	C4013
ENTS	C 4013
IRRINNER	C 33
012 I + 21 + 21 + 21 + 21 + 21 + 21 + 21	C4013
S=C05(DTHT)	C4013
SHOTE COTET	C4013
R PING ELEMENT:	64013
:00904(1)=81	C4013
:00PD4 (4) =PO	C4013
÷	C4014
COGRD4 (8) =RO*SS	ARC40141
1+0	C4014
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ARC40145
                            4RC40146
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                                                                                                      SAME
CALL QUAD4 (COORD4.THK.TEMP4.C.O.ND4.ANGLE4.ELG. ELK .8 .1.KW)
                                                                                                     SIMILAR GEOMETRY AND HAVE
                                                                                                                                                                                                                                                                                                                                                                                                                                                 RETURN CALLING PROGRAM CONTROLS TO THEIR ORIGINAL STARAGE
                                                                                                     MID RING & OUTER RING ELEMENTS ARE OF
                                                                                                                                                                                                                                                                                                                                             ASALTY (NM] . R.ELK.ELQ.RSS. (SS)
                                                                                                                                                                                                                                                                                                                               ASMLTV (NI + & + ELK + ELQ + RSS + ISS)
                                                                                                                                                                                                                                                                                                                                                           ASMLTV (NM2.8.ELK.ELD.RSS.1SS)
                                                                                                                                                                                                                                                                                                                                                                          ASMLTV (NO .R.ELK.ELO.RSS.1SS)
                                                                                                                                                                                                                                                                                                                                                                                                                                  CALL STACON (ISIGN+NID+RSS+ISS)
                                                                                                                                                                                                                                                                                                                TRANS (THETA FLK1 + ELK+ 8)
                                                                                                                                 ROTATE ELEMENTS AROUND APC
                                                                                      ELK1 (J+I) = ELK1 (I+J)
                                                                                                                                               THETA=THETA! -- DTHT
                                                                                                                                                                                                                                     THE TA=THE TA+DTHT
                                                                                                                                                                                                                                                                                                                                                                                                     STATIC CONDENSATION
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        IBEGIN(I)=IBG(I)
                                                                                                                    STIFFNESS MATOICES
                                                                                                                                                                                                                                                                                                                                                                                                                                                                (SIZE(1)=15Z(1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                              (S1ZE(2)=1S7(2)
                                                                        ELK1(I.J)=FLK
                                                                                                                                                                                                                        DO 200 I=1.10
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           SIZE (3) =NID
                            00 170 1=1.8
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            00 300 I=1.6
                                            DO 170 J=1.1
                                                                                                                                                                                                                                                                   NAI = NAI+1
                                                                                                                                                                                                                                                                                  NMO=NMO+1
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               0=7
                                                                                     170
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186(1)=1SAVE2(1) 182(1)=1SAVE3(1) 182(1)=1SAVE1(1) 152(2)=1SAVE1(2) RETURN END

RANS(THETA.ELKSQ.ELKV.IDOF) ***********************************	50 (ØF•2	TRANDO23 TRANDO24 TDOF TPANDO25 TRANDO25 TRANDO26 TRANDO27 TRANDO27 TRANDO27 TRANDO27 TRANDO27 TRANDO29 TRANDO30 TRANDO31 TRANDO31 TRANDO31
SUBROUTINE TRANS (THETA.EL) ***********************************	MENT APPLI 10N ELKSO(=1.100F =0.0	CS=COS (THETA SS=SIN (THETA T (1,1) = CS T (1,2) = SS T (2,2) = CS T (2,1) = -SS DO 10 T=2,1 ITM2= T-2 DO 10 T=2,1	10 T(ITM2+I.ITM2+J)= T(I.J) L=0 DO 20 I=1.IDOF DO 20 J=1.I L=L+1 ELKV(L)=0.0 DO 20 K=1.IDOF DO 20 LE=1.IDOF RETURN

VSJZE+ RING0000 +*********************************	N N N N N N N N N N N N N N N N N N N	EOODNIA EOODNIA
UTINE RING(RINNER.THK.THTCRK.NCRK.Al.A2.INDCTR.S.C.NSJZES) ************************************	PINGODO STRUCTURES RESEARCH LABORATORY STRUCTURES RESEARCH LABORATORY STRUCTURES RESEARCH LABORATORY APPLICATIONS TO USAF STRUCTURAL INTEGRITY PROBLEMS INGODO APPLICATIONS TO USAF STRUCTURAL INTEGRITY PROBLEMS APPLICATIONS TO USAF STRUCTURAL (3+3) *C (3+3	/20*0/ /10,4,6,25,24,48,47,18,16,8,2,4,6,22,12,18,16,14 0,10,16,14,71,9*20/
R.THK.THTCRK.NCRK.Al.AZ.IN ***********************************	75 MASSACHUSETTS INSTITUTE OF STRUCTURES RESEARCH LABORATORY ************************************	(4,48,47,18,16,8,2 1,9#20/
STINE S) RESERVE	(C) 1975 MASSACHUSETTS C AND STRUCTURES RESEA MENT APPLICATIONS TO UI ION RCRKTP (2) • ICASE (2) ELZ (32) • NOTASM (20) • NOC ELX (36) • ELQ (8) • ISAVE I NDRNG1 (29) • NDRNG2 (28) ION RARC (4504) • IARC (45) ION EK (171) • RCR (2•18) LENCE (RARC (1) • IARC (1)) /SIZE / ISZ (2) /SEGIN/IAG (6) /SIZE / ISZ (2) /SEGIN/IAG (6) /SIZE / ISZ (2) /SEGIN/IAG (6) /MILPRM/SMU•ETA /KI/RCR (2•2•18) /RI/RCR (2•2•18) /RI/RCR (2•2•18) /RADIUS/RNODE (5) 2/18*0•0/•PI/3•141593/ ODEL1/47•18•12•49•18•16 5•25•22•20•4•6•20•8•2•	NOTASM/20#0/ NDCRK1/10+4+6+25+24+48 +2+4-20+10+16+14+71+9#
SUBROUT RESS ISS) COMMENTINE R COF A 2 DIMENS COF ANOTHER F	COPYRIGHT (C) 197 AEROELASTIC AND S S=+***********************************	DATA NO DATA ND

	A NDCRK2/	RING0036
	DATA NDRNG1/3	PING0038
	,64,63,62,61,1,3,5,37/	PING0039
	DATA NDRNG2/26,27,28,29,30,31,32,33,34,35,17,15,13,59,	PING0040
	858+57+56+55+54,53+52+51+50+49+2+4+6+25/	RING0041
C 54	VE CALLING PRO	RING0042
	00 101 1=1.6	RING0043
	ISAVE2(I)=196(I)	PING0044
101	ISAVE3(I)=IEND(I)	RING0045
	00 103 I=1.2	8 I NG0046
103	ISAVE1(I)=ISZ(I)	RING0047
	RCRKTP(1)=RINNER+A1	RING0048
	RCRKTP(2)=RINNER+A2	PING0049
	DTHT=PI/12.0	RING0050
	RHODE (1) =RINNER	RING0051
	DO 10 I=1.4	PINGU052
10	RNODE(I+1)=RNODE(I)*(1,0,0,0THT)	FING0053
	R0=RN00E(5)	RING0054
	NET=20	RING0055
	NOT=144	RINGUUS6
	152(1)=20	RING0057
	152(2)=144	RING0058
	DELTA=(RNODE(5)+RNODE(4))/2.0	RINGU059
	RNODE (5) =RNODE (4)	RIMG0060
	RNODE (4) = DEL TA	RINGU061
		91NG0062
	GT. DELTA) GC TO 2	PING0063
	E0.	PING0064
		RINGU065
20	IF (RCPKTP(I) .GT. RNODE(J) .AND. RCRKTP(I) .LE. RNODE(J+1)) ICASE	SE (PINGO066
		PINGU067
9	60 TO 40	RING0068
0 4	CONTINUE	EING0070
•	RNODE (4) =RNODE (5)	PING0071

THE STATE OF THE S

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2 ING0100
0 ING0101
                                                                           RING0075
                                                RING0074
                                                                                                      RING0076
                                                                                                                           RING0077
                                                                                                                                                     WRITE(KW.5000)RINNER, THK, NCRK, THTCRK, A1, A2, INDCTR, (RCRKTP(I), I=1,2RING0078
                                                                                                                                                                                                        9000 FORMAT(1H1.60x,10HENTRY RING,//,23H SUBROUTINE INPUT DATA:,/,17H RRING0080 RADIUS OF HOLE =,E12.5,/,19H THICKNESS OF RING=,E12.5,/,18H NUMBER RING0081
                                                                                                                                                                                                                                                                                                                                         INDICARING0085
                                                                                                                                                                                                                                                                                                                                                               #TOR=1 : D.O.F.S AROUND HOLE ARE REMOVED),///,23H SUBROUTINE STATISRING0086
                                                                                                                                                                                                                                                                                                                                                                                                                                                 RING0089
                                                                                                                                                                                                                                                                                                                                                                                                                                                                     FORMAT (35H INNER RADII OF CONCENTRIC RINGS : $/.34x.EI2.5./.34x.EIRING0090 R2.5./34x.EI2.5./.34x.FI2.5./.22H OUTER RADIUS OF PING=.EI2.5./.34x.FIP.5./.62H OUTER RADIUS OF PING=.EI2.5./.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    9019 FORMAT (714 NO. OF INTERNAL D.O.F.S TO BE CONDENSED OUT OF HING STIPING0095
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  PING0098
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         91NG0099
   RING0072
                                                                                                                                                                                                                                                                                  *CRACK NO. 2 IS 180 DEGREES OPPOSITE 1,/, 20H CRACK NO. 1 LFNGTH=, EIRING 1083
                                                                                                                                                                                                                                                                                                             CKACK NO. 2 LFNGTH=+E12.5.//+24H CONDENSATION INDICATOR=RING0084
                                                                                                                                                                                                                                                                                                                                                                                                                     RING0088
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            31NG0092
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             76009NI
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 96009NI &
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      FING0102
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  PING0103
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            9 I NG 0 1 04
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     PING0105
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              AING0106
                                                                                                                                                                                                                                                                                                                                                                                          R CRACK NO. 1 = . ERING0087
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    E6009NI a
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        76005NI a
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       RINGUI07
                                                                                                                                                                                                                                                            (RADIANS) = • E12 • 5 • 42H
                                                                                                                                                                                                                                                                                                                                        (INDICATOP=0 : 0.0.F.S AROUND HOLE REMAIN :
                                                                                                                                                                                                                                                                                                                                                                                          #TICS: . / / . 52H RADIUS DIMENSION OF CRACK TIPS:
                                                                                                                                                                                                                                                            GOF CRACKS=*13*/*32H ANGLE OF CRACK NO. 1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  FORMAT (26H CASE REFERENCE NUMBERS : +215)
                                                                                                                                                                                                                                                                                                                                                                                                                   R CRACK NO. 2=, £12.5)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     CALL SETUP ("SI7E, 14, 296, RSS, ISS)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       Walte (h#+9002) (ICASE (I) . I=1+2)
                                                                                                                                                                                                                                                                                                                                                                                                                                          WRITE(184.5001)(RNODE(1).1=1.5)
                                                   GO TO 105
                                                                                                                               60 TO 9331
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              ESTABLISH ASSFMBLY LIST
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           WRITE (FALLES) P. IDSS
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              AFFINESS MATOIX =+15)
                                                   .EQ. 1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    SS(IMASTR)=IPNTA
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 DOF = NDPNG) (I) +2
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          2-2+I+dINdI=304)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          SS(IADD)=100F-1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           | PNTR=IMAST0+NFT
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     SS(IADD+1)=IDOF
                                                                                                                             .Eu. KW)
                                                                           NIDSS=48-NCPK+2
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     MASTREIEND (4)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         IMASTR=185(4)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               NO 50 1=1.28
RNO0E (5) =R0
                                                   IF (INDCTR
                                                                                                                                                                                                                                                                                                                                                                                                                   #12.5,19H
                          96=SS0IN
                                                                                                    CONTINUE
                                                                                                                                                                                                                                                                                                             #2.5.22H
                                                                                                                                                                                                                                                                                                                                        A.13,99H
                                                                                                                           IF (KT1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       9331
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  4005
                                                                                                                                                                                                                                                                                                                                                                                                                                                                       9001
                                                                                                    105
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IPNTR=IPNTR+56 ISS(IMASTR+1)=IPNTR DO 60 I=1+28 IACD=IPNTR+1+2+2	NG01 NG01 NG01
2(I)*2 IDOF-1)=IDOF	ING011 ING011 ING011
.3.4).N	1 NG0 1 1 1 NG0 1 1 1 NG0 1 1 1
,	1NG011 1NG012 1NG012
2 1 1	INGO 12 INGO 12 INGO 12
21.	ING012
+) =NP4	1 NGO 1 3 1 NGO 1 2 1 NGO 1 3
=9 2) 60 TO 22	TNG013 TNG013 TNG013
5 × 70N= 7	ING013 ING013 ING013
2	INGO 13
3 (1=12+13 N+4 SM (NP4) =NP4 SM (N) =N	ING014 ING014 ING014 ING014
	ING014

£ 0.4	241001KG
31 N=5.6	RING0145
	91001d
NOTASM (NPC) =NPC	4109NIa
NOTAS#(N) = N	97100NIa
60 70 5	64109N1d
no 33 v=13.14	0109N1a
カ・スリナロス	BINGUISI
	PING0152
NOTASM (N) AN	P1 NG0 153
GO 10 S	PI460154
	55109N1&
11	95109N18
%00EL1(14)=12	25109NI&
11	RINGOISE
Ħ	PING0159
11	RING0160
	RING0161
60 70 3	PING0162
	PING0163
NOVEL2(1*1=11	PING0164
	RINGUI65
	PING0166
ti	PINGUI67
	@ING0168
	PING0169
-	PING0170
_	PING0171
	RING0172
4	EL105N1a
•	P1NG0174
	51109NIa
~	91100N18
•	FINGULT
	FINGU178
55118A513+	PING0179

	00 00 1#1.46	RING0180
		DINCOLD
		TOTODAL A
(28 T 0 9 N I 2
٥ د	ISS(IADD*I) #155(IADD) *!	BI09NI6
	DO 100 N×10+20	# ING0 184
		PING0185
	ISS(IMASTR+V-1)=IDNTP	PING0186
	00 100 121.9	PING0187
	[A0D=1PNTQ+(1-1)+2	PING0188
	IF (N .EQ. 20) 60 TO 90	PING0189
	[SS(]ADD) = NDCPK1([.[CASF(])) + 2-1	6019
	ISS(1ADD+1)=1SS(1ADD)+1	D I NG0 191
	60 101	RING0192
Ü	0 ISS(1a00) = NOCPK2(1,1CASF(2)) *2-1	6019
	[SS(1An0+1)=[SS(1An0)+]	6019
100	CONTINUE	6109NIa
	[F(KT] ,EQ, KW) GO TO 1235	PING0196
	ERITE (9105N19
7006	FORMATIZEM ELEMENTS NOT ASSEMBLED: 4/2015)	9 1 NG 0 1 98
	WRITE (xx+4003)(15S(1)+1x1x4STQ+LMASTR)	96109NI9
6000	FORMAT (22H MASTER ASSEMBLY LIST: . / . 10H POINTERS: . 2015 . / . 32K	ELEMENPING0200
_	## 0.0.F.St ELEMENTS 1-141./.15(1H0.1615./)./.49H ELEMENT P.	DING0201
•	BELEMENT 0.0.F.St ELEMENT 19-201./.2(1H0.1815./))	DING0202
1235	CONTINUE	RINGUS03
	CALL OPKINS	PING0204
ST 3	SEMBLE ELEMENTS	FING0205
	THETA#THTCOX+DI+DTHT	PING0206
	CALL ARC4 (RINNEG. THE TA.DTHT.C.THK.ELK.RARC. IARC. IS2SS. IBEGSS.BARC) RING0207	1PING0207
	00 120 N#1+2	PINGUS08
120	SMSUP	PING0209
	O.	PING0210
	SAMS (PING0211
	-	
	Desin.a	# I NG0513
	IF (N .EQ. NOTASM(N)) GO TO 125	PING0214
	ALL ASMLTV	91209N19

CONTINUE	PINGUS16
EG. NOTASMINP411 GO TO	91NG0217
4.8.ELKV.FL.0.RSS.I	PING0218
このとするとは	61209N1a
	02209N1d
CALL TRANSCIEFTA.FUX.FUXV.B)	FINGUSSI
00 140 NE7.10	RING0222
	RING0223
SE(N)) 60 TO 135	P1NG0224
8 * 5 T 4 * 6 T 5 * 8	PING0225
	PING0226
IFIND4 "FD. NOTASMIND4:1 GO TO 140	61NG0227
4.4.FLKV.FLO.RSS	PING0228
COMTINISE	PING0229
DO 160 WEIG.20	PING0230
	PING0231
1F(N.FQ. NOTASM(N)) GO TO 156	PING0232
CAKSO COORDINATES	PING0233
CS1 = COS = THE TA - DTIT	PING0234
SS1=SIN(THFTA-DTHT)	p I NG0235
CS2*COS (THFTA)	PINGC 536
25.24.51.2 (177.14.)	F1NG0237
CS3*COS(THFT&+DTAT)	p1NG0238
S93#512 (TMETA+DTMT)	6E209N1a
HINGCRATO (NAIR) COSS	01209NI 0
1 • 5:52	PING0241
RO * BNOOF (10 ASE (NA 1 A) • 2)	27209NIB
C008D (1) #C52+80	PING0243
Ua+€55+1€100000	PING0244
00 150 1*1.3	24208NIa
1.5.1.2	05×1
40 x 4 NODE (10 SE (NA 1 A) + 3 - 1)	PINGUS41
C0080(J) *80*C53	さい
CQQBQ (7+1) #PQ+553	ING054
	ING02
PORTNOOF (ICASE (NAIA) + I + I)	PING0251

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PING0253
                           P1%60254
                                        PIEG0255
                                                      PING0256
                                                                                              # ING0259
                                                                                                                                                    PING0253
                                                                                                                                                                 PING0264
                                                                                                                                                                              91NG0265
                                                                                                                                                                                            PING0266
                                                                                                                                                                                                                      RING0268
                                                                                                                                                                                                                                   ₽1 №GC269
                                                                                                                                                                                                                                                 PING0270
                                                                                                                                                                                                                                                                           9 INGUS12
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                                                                                                                                                                                                                                                                                                                                                                          PING0279
                                                                                                                                                                                                                                                                                                                                                                                      PING0280
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                                                                                                                                                                                                                                                                                                                                                                                                                                                                       PINGUSBA
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RING0252
                                                                   PING0257
                                                                                 RING0258
                                                                                                            FING0260
                                                                                                                                       PING0262
                                                                                                                                                                                                       PING0267
                                                                                                                                                                                                                                                                                                       DING0274
                                                                                                                                                                                                                                                                                                                                                            #ING0278
                                                                                                                         PING0261
                                                                                                                                                                                                                                                               PING0271
                                                                                               PCRKSO12.5MU.ETA.XT.YT. COORD.EK.BCK)
                                                                                                                                                  CALL ASMLTVIN-18-FK+E0-R55-155-
                                                                                                                                                                                                                                                                                                                                 #1255(J) .ME. 5.0) GO TO 190
                                                                                                                                                                                                                                                                                                                                                                                                                              CALL STACOMITANIDSS.RSS.155)
                                                                                                                                                                                                                                                                                                                    24155 (186(2) + 10 (46-1) + 101AG
                                                                                                                                                                                                                                                 ERMINE CONSTRAINED D.O.F.S
                                                                                                                                                                                                                                                                                                                                                                          -1-10146)=0.0
                                                                                                                                       BCRK (NM18+1+J) #8CR (1+J)
                            ROSENDDE (ICASE (NAIR))
                                                                    (b ) G80003=(11) G8000
                                                                                COURD (12) = COURD (10)
                                                                                                                                                                                                                      BCRK (NM18-1.4) = 0.0
                                                                                                                                                                                                                                                                                                                                                                                                   CALL &COM (R55-155)
             COORD (J+1) #40+451
                                                       COORD (10) #RO+552
                                                                                                                                                                                                                                                                                                                                                                                                                                                                       BEGSS (1) *146 (1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    BG(1) #184VF2(1)
                                          20000 (4) #RO+CS2
183-08*(1)080000
                                                                                                                                                                                                                                    SPICING COLUMN
                                                                                                                                                                                                                                                                                         20 190 1×1 0×1 00
                                                                                                                                                                                                                                                                                                      ISTAGE TOTAGe !
                                                                                                                         DO 155 J#1,18
                                                                                                                                                                                                          00 157 Jel-18
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                                                                                                           5-1-1 551 00
                                                                                                                                                                                            00 157 1x1.2
                                                                                                                                                                                                                                                                                                                                                                                                                                            ROFFRODE (8)
                                                                                                                                                                                                                                                                                                                                                                          632 (196 (5)
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                                                                                                CALL
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               150
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195	
	DØ 195 TE1.2
	15755(1) #147/1) PING0289
196	
	15255(1) #Wanco
	15 (X1) .EQ. XX1 GO 10 101
	#914F(X#.1241)
1234	FORTATION AND AND AND AND AND AND AND AND AND AN
101	RETURN FILES
200	
0009	FORMAT (14MIC) TO THE STATE OF
,	REENTED OF HOLF AND TO TOTALTY THE THE TELL STATE MEASURED FROM PINGAZOR
_	SOLVE TARE COORES OF THE TEST TRACES ORACK LENGTE ALLONED BYPINGOZOG
_	BING BING! SUBSTITUTE OF SELESTINGS EXECUTION TERMINATED IN SUBSOUTRINGS300
	STOP
	END PINGO302
	E0E03016

APPENDIX D

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PANOORS
                                                                                                      LPAN0006
                                                                                                                                                                                LPAN0008
                                                                                                                                                                                                           (6E10.3,15) LPAN0009
                                                                                                                                                                                                                                                                                                                 PANOGIE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      PANDORY
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             DIMENSION RFF (10000), IFF (10000), REAL (8000), INTGR (R000), RRNG (12000) LPAN0023
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    PAN0032
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      PAN0034
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               PANOGUE
                            .....INPUT DATA FOR PROBLEM #3...........
                                                                                                                                                                                                                                    (2E10.3.2IS) LPAN0010
                                                                                                                                                                                                                                                                                          (315) LPAN0012
                                                                                                                                                                                                                                                                                                                                           PAN0014
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                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        LPAN0024
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                                                                                                                                                                                                                                                               (2E10.3) PANO011
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         PAN0031
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           PANCOZI
                                                                                                                                                                                                                                                                                                                                                                                                                     IDFFSET = OFFSET INDICATOR; A(1) = LENGTH OF CRACK ONE; A(2) = LENGTH OF CRACK TWO: IPOS(1) = INITIAL POSITION OF CRACK ONE;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  BANGLE (2,2) + A (2) + I POS (2) + I SZFF (3) + I BGFF (6) + I SAVE (6) + ELQ (18) + RK (3)
                                                                                                                                                                                   FORMAT FOR EACH CARD
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       QUIVALENCE (RFF(1) + IFF(1)) + (REAL(1) + INTGR(1)) + (IBEGIN(1) + ICOM)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    PRINTS
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        8.IRNG(12000) +S(3+3) +C(3+3) +IREGIN(6) +IEND(6) +ISZ(7) +ISZSS(3) +
                                                                                                                               FINITE ELEMENT APPLICATIONS TO USAF STRUCTURAL INTEGRITY PROBLEMS
(LEFT SIDE STIFFENED
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    OPTIONAL
                                                                                                                                                                                                                                                                                                                                                                                                                                                                         E = YOUNGS MODULUS$
                                                  COPYRIGHT (C) 1975 MASSACHUSETTS INSTITUTE OF TECHNOLOGY
                                                                                                                                                                                                                                                                                                                                                                  STFFCT = STIFF'NESS FACTOR;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  GNU = POISSONS RATIOIKTI = PRINT CONTRÔL FOR FEABL
                                                                                                                                                                                                                                                                                                                                           PLATE: LENGTH = LENGTH OF PLATE;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           = PRINT CONTROL FOR OPTIONAL FARFLD PRINTING!
                                                                                                                                                                                                           WIDTH.LENGTH.THK.STFFCT.PRESS.RI. JOFFST
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      = PRINT CONTROL FOR OPTIONAL RING PRINTING;
                                                                                                                                                                                                                                                                                                                                                                                           RI = RADIUS OF HOLES
                                                                             AEROELASTIC AND STRUCTURES RESEARCH LABORATORY
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 COMMON/BEGIN/ICON. IKOUNT, ILNZ, IMASTR, IQ, IK
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         COMMON/END/LCGN.LKOUNT.LENZ.LMASTR.LO.LK
                                                                                                                                                                                                                                                                                                                                                                                                                                                                       IPOS(2) = FINAL POSITION OF CRACK ONE;
 TEST MAIN - CONTRACT 81739 PROBLEM 3
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    COMMON/SIZESS/NETSS.NDTSS.NIDSS
                                                                                                                                                                                                                                      A(1), A(2), IPOS(1), IPOS(2)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               COMMON/IO/KW.KW.KP.KTI.KT2.KT3
                                                                                                                                                                                   VAHIABLES IN SET
                                                                                                                                                                                                                                                                                                                                                                                             PRESS = FARFIELD LOADING:
                                                                                                                                                                                                                                                                                                                                                                  = THICKNESS OF PLATF
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 COMMON/KI/BCRK (2.2.2.18)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      COMMON/MILPHM/SMU.FTA
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               COMMON/BEGSS/IAGSS(6)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      INTEGER CNODE, PRNTSV
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          COMMON/SIZE/NET+ND1
                                                                                                                                                                                                                                                                                          KT1.KT2.KT3
                                                                                                                                                                                                                                                                                                                                            WIDTH # WIDTH OF
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            PEAL LENGTH
                                                                                                                                                                                                                                                                 E . GNU
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1919年,1918年,1918年,1918年,1918年,1918年,1918年,1918年,1918年,1918年,1918年,1918年,1918年,1918年,1918年,1918年,1918年

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PAN0038
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                                                                              PAN0040
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                                                                                                                                                        PANOCAS
                                                                                                                                                                                                                                      PANDO46
                                                                                                                                                                                                                                                                  PAN0047
                                                                                                                                                                                                                                                                                           PANOO4A
                                                                                                                                                                                                                                                                                                                     PAN0049
                                                                                                                                                                                                                                                                                                                                                                                                                                                                             PANDOSS
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          FORMATITHI.58X.14HCONTPACT 81739.//57X.13HPROBLEM NO. 3.///.55X.19LPAN0058
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     SIDE STIFFENED.//.60x.11H INPUT DATA:///.16H PLATE GEOMETRY: LPAN0059
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     MHICKNESS=+E12.5./.24H PLATE STIFFENER FACTOR=+F8.3./.25H FAR FIELDLPAN0061 CLOADING (PSI)=+E12.5./.16H RADIUS OF HOLE=+E12.5./.23H HOLE OFFSELPAN0062
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    PANOO64
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 LPANDO65
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         LPAN0066
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 6001 FORMATILLH CRACK NO. >13-17H : CRACK LENGTH=,E12,5,/,18x,23HINIT1LPAN0070
                                                                                                                                                                                    PANDO44
                                                                                                                                                                                                               PANCOAS
                                                                                                                                                                                                                                                                                                                                                PAN0050
                                                                                                                                                                                                                                                                                                                                                                                                 PANOOSS
                                                                                                                                                                                                                                                                                                                                                                                                                              PANOONA
                                                                                                                                                                                                                                                                                                                                                                                                                                                       PANOUSA
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          PANOOSÓ
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         OT INDICATOR=.13.274(#6, HOLE REMAINS CENTERED) .//,12H CRACK DATA: . [PANGO63
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    PANOG67
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 PAN0068
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     LPAN0072
                                                                                                                                                                                                                                                                                                                                                                           PANGOS
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                PANCOST
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            CRACK POSITION=+13+1M(+F8+3+9H DEGREES)+/+20x+21HFINAL CPACK POLPANOOT
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               8.//.i3H PLATE WIDTH=,E12.5./.14H PLATE LENGTH=,E12.5./.17H PLATE
                                                  PI/3.14?593/.5/1.0.3#0.0.1.0.4#0.0/.C/1.0.3#0.0.1.0.4#0.0/
# (15ND (1) . LCON) . (152 (1) . NET) . (152SS (1) . NETSS) . (RANG (1) . 1RNG (1))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                HRITE(KW.6000) WICHW-LEWSTM.INK.STFFCT.PRESS.RI.IOFFST
                                                                                                                                                                                                           READIKR. 5000) WIDTH. LENGTH. THK. STFFCT. PRESS. RI. 10FFST
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       WRITE(KW.6001) I.A(I).(IPOS(J).ANGLE(I.J).J=1.2)
                         DATA NSZFF/10000/.NSZRNG/12000/.NSZMN/8000/
                                                                                                                                                                                                                                                                   READ(KK+5001) A(1).A(2).IPOS(1).IPOS(2)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     #SITION=.13.1H(.F8.3.9H DEGREES)./)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   0.0) NCRK=NCRK+1
                                                                                                                                                                                                                                                                                                                                                                                                                                                  ANGLE (1,2) = (IPOS(2)-1)+15.0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         ANGLE (2,2) = ANGLE (1,2)+180,0
                                                                                                                                                                                                                                                                                                                                                                                                                           ANGLE (1,1) = (IPOS(1)-1)+15,0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                             ANGLE (2,1) = ANGLE (1,1) + 180.0
                                                                                                                                                                                                                                                                                                                                                                         READ (KR. 5003) KT1.KT2.KT3
                                                                                                                                                                                                                                                                                                                   READ (KR. 5002) E. GNU
                                                                                                                                                                                                                                                                                           FORMAT (2E10.3.215)
                                                                                                                                                                                                                                      FORMAT (GE10,3.15)
                                                                                                                                                        SGRIPI=SORT (PI)
                                                                                                                                 OTHE TA=P1/12.0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            DO 15 I=1.NCR#
                                                                                                                                                                                                                                                                                                                                              FORMAT (2E10.3)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   IF ( A (1) .6T.
                                                                                                                                                                                                                                                                                                                                                                                               FORMAT (315)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         DO 10 I=1,2
                                                                                                                                                                                     INPUT DATA:
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       BALEFT
                                                    DATA
                                                                               不玩用几
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              E AL
                                                                                                                                                                                                                                                                                                                                                5005
                                                                                                                                                                                                                                        500r
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               6000
                                                                                                                                                                                                                                                                                             5001
                                                                                                                                                                                                                                                                                                                                                                                                   5003
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           Ś
```

E(KW.6002) E.GNU AT(21HOMATERIAL PROPERTIES:.//.20H YOUNGS MODULUS (E)=.E12.5./ POISSONS RATIO=.F12.5.///) TE S&C MATRICES:	073
(1) = GNU $(3) = (1 < 0 - GNU) / 2 \cdot 0$	079
.1)=-6NU .3)=(1.0+6NU)*2.0	0 % C
=E/(2.0*	080
= (3.0=6NU)/(1.0+6NU) = E/(1.0=6NU+6NU)	280
20 I=1.	400
J)=S(I+J)/E	986
(C+I)S=(I	081
1) HC(II+1) # @NC	900
DETERMINE NUM	060
HEWIOTH/(4.0*RI)	160
THAT NELW IS EVEN VALUED:	260
5LW/2	E60
7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7	4000
IDIA/NELY	960
IO=W/RI	160
INE STIFFENER THICKNESS:	860
STEINKHINK+SIFFCI+WIDIH+IHK/W C CFNIFR NODF WFFFRENCF (INDII FOR SUBBOLIINF CAONF):	2000
CNODE=NELW/2+1	207
IMIT=2	102
F(IOFFST .EG.) LIMIT=NELW	€ .
HOLE WILL INITIALLY BE PLACED IN CENTER OF PLATE. IF	7 (1) (1) (1)
QUAL TO 0 THE HOLE CENTER WILL BE MOVED TO THE RIGHT IN INCREMENTS	304
A AS TAK AS I	108

LPANO109 LPANO1109 ILPANO1112 LPANO1113 ILPANO1114		1000N	~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~	n a a a a a a a a a a a a a a a a a a a	LPAN0137 LPAN0138 LPAN0139 LPAN0140 LPAN0141 LPAN0142 LPAN0143 LPAN0143
3 T L L			I ALDUNE SARA		
SMU.ETA SEQ OF ELEMEN E12.5./.30H H EFERENCE=.14.			S CRODE SO		(CHESIRE CAT)
C PRINT OUT PROGRAM STATISTICS TO NATE: IF(KT1 .EQ. KW) GO TO 30 WRITE(KW+6003) NELW+W+RATIO+CNODE+STFTHK+SMU+ETA 6003 FORMAT(20H0PROGRAM STATISTICS:+//+33H NUMBER OF ELEMENTS ACROSS GDTH=+14+/+27H QUADRILATERAL DIMENSION W=+E12+S+/+30H HOLE ELEMEN GDTH=+14+/+27H QUADRILATERAL DIMENSION W=+E12+S+/+30H HOLE ELEMEN GDTH=+14+/+27H QUADRILATERAL DIMENSION W=+E12+S+/+21H STIF GANER THICKNESS=+E12+S+/+21H MATERIAL PARAMETERS:+/+5H SMU=+E12+ GANER THICKNESS=+E12+S+/+21H MATERIAL PARAMETERS:+/+5H SMU=+E12+ GANER THICKNESS=+E12+S+/+10H C MATERIAL PARAMETERS:+/+5H SMU=+E12+S+/+10H C MATERIAL PARAMETERS:+/+5H SMU=+E12+S+/++10H C MATERIAL PARAMETERS:+/++5H C MATERIAL PARAMETERS:+/-+++++++++++++++++++++++++++++++++++	D • I = 1 • 3)	1) + [=] + 3)	D SUBSTRUCTURE (CHESIRE CAT): LPANO1 LPANO1 LPANO1 TA) ** 4 * RI LPANO1 LPANO1 LPANO1 LPANO1 LPANO1 LPANO1	(ga)	L.INTGR) SUBSTRUCTURE (
STATISTICS TO GO TO 30 NELW+W+RATIO+C RAM STATISTICS UADRILATERAL D =+F8.3+/+23H C	(S(I+J)+J=I+3	RIX:) (C(I•J),J=l•3	BSTRUCTURE (C *4*RI	SZMN, RFAL, INT) M: •1•IPNTR•REAL T: E FAR FIELO S
OUT PROGRAM S KT1 .EQ. KW) TE(KW+6003) N MAT(20H0PROGR =.14./.27H QU ENSION RATIO= THICKNESS=.E	TE(KW*6004) (MAT(1H *3E12*	MAT (10H0C MAT TE (KW+5004) (TINUE	FAR FIELD SU TINUE TSV=KT1 =KT2 (I.0+OTHETA)* CTR=0	ZFF & RFF + 1FF + NC = 1PRN TSV 35 I = 1 + 3 FF (I) = 1 SZSS (I	IBGFF(I)=IBGSS(I) I UP CRACK PROBLEM: NET=2 NDT=96+2*NCRK*146 IPNTR=2*NCRK*146 CALL SETUP(NSZMN*1*IPNTR*REAL*INTGR) I UP ASSEMBLY LIST:
C D INTERPRETATION OF THE COURT COUR	#RI 6004 FOR	6005 FOR WRI 30 CON	C OBTAIN 32 CON PRN FTI RTI RO= IND	8 .NS JEO JEO JEO 85 152	36 IBGF C SET UP OF SET UP OF SET UP CALL

	IPNTR=IMASTR+2	LPAN0145
	INTGR(IMASTR)=IPNTR	LPAN0146
	00 40 I=1•48	LPAN0147
		LPANO 140
0*		4
CEL	EMENT NO. 2 IS THE CHACKED RING	15
	+1)=[6	LPANO151
45	IPNTR=INTGR(IMASTR+1;	15
	DO 50 1#49*NDT	S
	INTGR(IPNTR)=I	51
20	IPNTR=IPNTR+1	LPANOISS
	J=(++JLOC)+2+]	15
	IF (JLOC .GE. 21) J=(JLOC-20)*2-1	LPAN0157
		LPAN0158
	INTGR(IPNTR)=I	LPAN0159
9	IPNTR=IPNTR+1	LPAN0160
		LPAN0161
	IF (JLOC .Eq. 21) 60 TO 75	LPAN0162
	DO 70 I=1,0	LPAM0163
	INTGR(IPNTR)=I	LPANO164
	IPNTR=IPNTR+1	LPAN0165
75	CONTINUE	LPAN0166
	IF (KT) .EQ. KW) GO TO 80	LPAN0167
	J=IMASTR+1	•
		LPAN0169
9009	ZHOMASTER ASSEMBLY LIST: , / , 59H PUINTER FOR FAR FIELD	~
	GRUCTURED ELEMENT (CHESIRE CAT)=,15,7,26H POINTER FOR CRACKED RING	~
-	6.150/j	
		- P
	MRITE(KM.6007) (INTGR.(T).IBJ.IPNTR)	F PANOL 75
2009	¥	PANOLT
_	1615./.444.1615)	17
	FNIKE FNIK+1	-
	LHIPRIK+VU+NCKK#Z HDITF(KH*KACK) (INTOCI), IHIDNID, 1)	L L PANG L
	2000185141	4 > 2

N'REAL'INTGR) LD SUBSTRUCTURE: F(I) *AFF'IFF'REAL'INTGR) *ABLE CHACKED RING ELEMENT: 1)*DTHETA *THK.THTCRK,NCKK,A(I)'A(2)'INUCTR'S.C.NSZRNG,RRNG, *THK.THTCRK,NCKK,A(I)'A(2)'INUCTR'S.C.NSZRNG,RRNG, *THK.THTCRK,NCKK,A(I)'A(2)'INUCTR'S.C.NSZRNG,RRNG, **INOTHETOR DISPLACEMENTS: **RNG,IRNG,REAL'INTGR') **INOTHETOR DISPLACEMENTS: **RNG,IRNG,REAL'INTGR') **INOTHETOR DISPLACEMENTS: **I	
I) IE CHACKED RING ELEMENT: *DIHEIA K.THICRK,NCKK,A(i).A(2).INUCTR.S.C.NSZRNG.RRNG. RNG.IRNG.REAL.INTGR) *REAL.INTGR) *REAL.INTGR) *GO IV IZO (I) (I) (I) (I) (I) (I)	LPANO183
I) IE CHACKED RING ELEMENT: *DTHE TA *DTHE TA RNG* IRNG* REAL* IN TGR) RNG* IRNG* REAL* IN TGR) G INTERIOR DISPLACEMENTS: NG* IRNG* REAL* INTGR) G O TO 120 (I) (I) (I) (I) (I)	LPAN0185
FF. IFF. REAL. INTGR) LE CHACKED RING ELEMENT: *DTHE TA *DTHE TA RNG. IRNG. REAL. INTGR) G INTERIOR DISPLACEMENTS: G INTERIOR DISPLACEMENTS: G OTO 120 (1) (1) (1) (1) (1)	LPAN0186
I) FF.IFF, REAL. INTGR) LE CHACKED RING ELEMENT: *DTHETA *DTHETA K.THTCRK, NCRK, A(I) .A(2) .INUCTR.S.C.NSZRNG, RRNG, RNG. IRNG. REAL. INTGR) G INTERIOR DISPLACEMENTS: NG. IRNG. REAL. INTGR) G OTO 120 (1) (1) (1) (1)	LPAN0187
FF.IFF.REAL.INTGR) LE CRACKED RING ELEMENT: *DTHE TA *DTHE TA RNG.IRNG.REAL.INTGR) *REAL.INTGR) G INTERIOR DISPLACEMENTS: NG.IRNG.REAL.INTGR) (1) (1) (1)	LPAN0188
LE CHACKED RING ELEMENT: *DTHE TA *DTHE TA K. THTCRK, NCHK, A(1), A(2), INDCTR, S.C.NSZRNG,RRNG, RNG, IRNG, REAL, INTGR) G INTERIOR DISPLACEMENTS: NG, IRNG, REAL, INTGR) G INTERIOR DISPLACEMENTS: (I) (I) (I) (I)	LPAN0189
*DTHE TA K. THTCRK, NCKK, A(i).A(2).INUCTR.S.C.NSZRNG.RRNG. RNG.IRNG.REAL.INTGR) REAL.INTGR) G INTERIOR DISPLACEMENTS: NG.IRNG.REAL.INTGR) G O TO 120 (I) (I) (I) (I)	
K.THTCRK,NCKK,A(!),A(2),INDCTR,S.C,NSZRNG,RRNG, RNG,IRNG,REAL,INTGR) REAL,INTGR) G INTERIOR DISPLACEMENTS: NG,IRNG,REAL,INTGR) G OTO 120 (1) (1) (1)	6
PRNTSV=KI1 KT1=KT3 CALL RING(RI.THK.THTCRK.NCRK,A(i).A(2).INUCTR.S.C.NSZRNG.RRNG. FIRNG. KT1=PRNTSV CALL ASMSUB(2.RRNG.IRNG.REAL.INTGR) AIN SOLUTION: AIN SOLUTION: AIN CACKED RING INTERIOR DISPLACEMENTS: CALL SIMULQ(GNU.REAL.INTGR) CALL SIMULQ(GNU.REAL.INTGR) I=1 CALL SIMULQ(GNU.REAL.INTGR) CALL GBACK(2.RRNG.IRNG.REAL.INTGR) IF(NCRK.EU. 0) GO TO 120	19
KT1=KT3 CALL RING(RI,THK,THTCRK,NCRK,A(i),A(2),INUCTR,S,C,NSZRNG,RRNG,PIRNG) FIRNG) KT1=PRNTSV CALL ASMSUB(2,RRNG,IRNG,REAL,INTGR) AIN SOLUTION: I=1 CALL FACT(I,REAL,INTGR) CALL SIMULD(GNU,REAL,INTGR) TAIN CRACKED RING INTERIOR DISPLACEMENTS: CALL QBACK(2,RRNG,IRNG,REAL,INTGR) IF(NCRK,EU,0) GO TO 120 TAIN KI ANU KII: WRITE(KW,6012) FORMATHING) DO 90 I=1,6 ISAVE(I)=18EGIN(I) INEGIN(I)=18EGSS(I) THTCKK=THTCRK*180,0/PI DO 110 I=1,NCKK	LPAN0193
CALL RING(RI,THK,THTCRK,NCMK,A(i),A(2),INUCTR,S.C.NSZRNG,RRNG, PIRNG) KTI=PRNTSV CALL ASMSUB(2,RRNG,IRNG,REAL,INTGR) AIN SOLUTION: 1=1 CALL SIMULG(GNU,REAL,INTGR) CALL SIMULG(GNU,REAL,INTGR) CALL GBACK(2,RRNG,IRNG,REAL,INTGR) TAIN CRACKED RING INTERIOR DISPLACEMENTS: CALL QBACK(2,RRNG,IRNG,REAL,INTGR) IF (NCRK, &Cu., 0) GO TO 120 TAIN KI AND KII: WRITE (KW,6012) FORMAT(1H%) DO 90 I=1,6 ISAVE(I)=IBEGIN(I) IBEGIN(I)=IBESS(I) THTCKK=THTCRK*180,0/PI	O.
FIRNG) KTI=PRNTSV CALL ASMSUB(2.RRNG.IRNG.REAL.INTGR) AIN SOLUTION: 1=1 CALL FACT(I.REAL.INTGR) CALL SIMULQ(GNU.REAL.INTGR) TAIN CRACKED RING INTERIOR DISPLACEMENTS: CALL QBACK(2.RRNG.IRNG.REAL.INTGR) IF (NCRK .Eu. 0) GO TO 120 IF (NCK .eu. 0) GO TO 120	LPAN0195
KTI=PRNTSV CALL ASMSUB(2.RRNG.IRNG.REAL.INTGR) AIN SOLUTION: 1=1 CALL FACT(I.REAL.INTGR) CALL SIMULQ(GNU.REAL.INTGR) TAIN CRACKED RING INTERIOR DISPLACEMENTS: CALL QBACK(2.RRNG.IRNG.REAL.INTGR) IF (NCRK .Eu. 0) GO TO 120 IF (NCK .Eu. 0) GO TO 120 ISAVE(I)=IBEGIN(I) IBEGIN(I)=IBGSS(I) IHTCKK=THTCRK*180.0/PI DO 110 I=1,NCFK	LPAN0196
CALL ASMSUB(2.RRNG.IRNG.REAL.INTGR) AIN SOLUTION: 1=1 CALL FACT(I.REAL.INTGR) CALL SIMULO(GNU.REAL.INTGR) TAIN CRACKED RING INTERIOR DISPLACEMENTS: CALL QBACK(2.RRNG.IRNG.REAL.INTGR) IF (NCRK .Eu. 0) GO TO 120 IF (NCRK .Eu. 0) GO TO 120 TAIN KI AND KII: WRITE(KW.6012) FORMAT-(1H40) DO 90 I=1.6 ISAVE(I)=IBEGIN(I) IBEGIN(I)=IBGSS(I) THTCKK=THTCRK*180.0/PI DO 110 I=1.NCFK	-
AIN SOLUTION: 1=1 CALL FACT(I•REAL•INTGR) CALL SIMULD(GNU•REAL•INTGR) TAIN CRACKED RING INTERIOR DISPLACEMENTS: CALL QBACK(2•RRNG•IRNG•REAL•INTGR) IF (NCRK •Eu. 0) GO TO 120 TAIN KI AND KII: WRITE (KW•6012) FORMAT-(1H0) DO 90 I=1•6 ISAVE(I)=IBEGIN(I) IBEGIN(I)=IBGSS(I) THTCKK=THTCRK*160.0/PI DO 110 I=1•NCFK	LPANO198
<pre>1=1 CALL FACT(I,REAL,INTGR) CALL SIMULQ(GNU,REAL,INTGR) TAIN CRACKED RING INTERIOR DISPLACEMENTS: CALL QBACK(2,RNG,IRAG,REAL,INTGR) IF (NCR .E. 0) GO TO 120 IF (NCR .E. 0) GO TO 120 IF (NCR .E. 0) GO TO 120 IF (NW,6012) FORMAT(1HΦ) DO 90 I=1,6 ISAVE(I)=IBEGIN(I) IBEGIN(I)=IBGSS(I) THTCKK=THTCRK*180.0/PI DO 110 I=1,NCFK</pre>	PAN0199
CALL FACT(I, REAL, INTGR) CALL SIMULQ(GNU, REAL, INTGR) TAIN CRACKED RING INTERIOR DISPLACEMENTS: CALL QBACK(2, RRNG, IRNG, REAL, INTGR) IF (NCRK .e. 0) 60 TO 120 TAIN KI AND KII: WRITE (KW, 6012) FORMAT*(1H0) DO 90 I=1,6 ISAVE(I)=IBEGIN(I) IBEGIN(I)=IBGSS(I) THTCKR=THTCRK*160,0/PI DO 110 I=1,NCFK	PAN0200
CALL SIMULD (GNU-REAL,INTGR) TAIN CRACKED RING INTERIOR DISPLACEMENTS: CALL QBACK (2-RRNG-IRNG-REAL,INTGR) IF (NCRK -Eu. 0) GO TO 120 IF (NCRK -Eu. 0) GO TO 120 TAIN KI AND KII: WRITE (KW-6012) FORMAT-(1H0) DO 90 I=1.6 ISAVE (I) = IBEGIN(I) IBEGIN(I) = IBGSS(I) THTCKK=THTCRK*160.0/PI DO 110 I=1.NCFK	PANGZOI
TAIN CRACKED RING INTERIOR DISPLACEMENTS: CALL QBACK(2.RRNG.IRNG.REAL.INTGR) IF (NCRK .Eu. 0) GO TO 120 IF (NCRK .Eu. 0) GO TO 120 TAIN KI ANÚ KII: WRITE (KW.6012) FORMAT-(1H0) DO 90 I=1.6 ISAVE (I) = IBEGIN(I) IBEGIN(I) = IBGSS(I) THTCKK=THTCRK*180.0/PI DO 110 I=1.NCFK	PAN0202
CALL QBACK(2.RRNG.IRNG.REAL.INTGR) IF (NCRK .Eu. 0) GO TO 120 IAIN KI ANU KII: WRITE(KW.6012) FORMAT-(1H0) DO 90 I=1.6 ISAVE(I)=IBEGIN(I) IBEGIN(I)=IBGSS(I) THTCKK=THTCRK*180.0/PI DO 110 I=1.NCFK	LPAN0203
IF (NCRK .EU. 0) GO TO 120 TAIN KI AND KII: WRITE (KW.6012) FORMAT(1H0) DO 90 I=1.6 ISAVE(I)=IBEGIN(I) IBEGIN(I)=IBGSS(I) THICKK=THICRK*180.0/PI DO 110 I=1.NCFK	LPAN0204
TAIN KI AND KII: WRITE(KW.6012) FORMAT-(1H0) DO 90 I=1.6 ISAVE(I)=IBEGIN(I) IBEGIN(I)=IBGSS(I) THTCKK=THTCRK*180.0/PI DO 110 I=1.NCFK	LPANG205
WRITE(KW.6012) FORMAT-(1H0) DO 90 I=1.6 ISAVE(I)=IBEGIN(I) IBEGIN(I)=IBGSS(I) THTCKK=THTCRK*180.0/PI DO 110 I=1.NCFK	LPAN0206
FORMAT(1H0) DO 90 I=1.6 ISAVE(I)=IBEGIN(I) IBEGIN(I)=IBGSS(I) THTCKK=THTCRK*180.0/PI DO 110 I=1.NCKK	LPAN0207
GIN(I) GSS(I) K*180.0/PI CŘK	LPAN0208
GIN(I) GSS(I) K*180.0/PI	LPAN0209
GSS(I) K*180.0/PI Cřk	_
K*150.0/PI CKK	LPAN0211
以不	
	LPAN0213
L XTRACT(I+16+18+ELU+RRNG+IRNG)	LPAN0214
	PNO PNO
KK:J)=0.0=	PANOZIE

LPANO217 LPANO218 LPANO218 LPANO220 LPANO221 LPANO223 KIILPANO223	LPAN0225 LPAN0225 LPAN0226 LPAN0228 LPAN0228 LPAN0226	LPAN0232 LPAN0233 LPAN0234 LPAN0235 LPAN0235 LPAN0236 LPAN0236 LPAN0240 LPAN0241
KI=•E12.5.8H) 130) 130 ;X•134HOLE OFFSET
•J=1•2) GLE=•FB•3•8H	10 45	O TO 130 •AND• IOFFST •EQ• 1) GO TO 130 •AND• IOFFST •EQ• -1) GO TO 130 INCREMENT HOLE POSITION•//•54X•13HHOLE
K=1.	=TMTCRK+180.0 CMACK POSITION: LOC+1 I=1.6 (I)=ISAVE(I) CLE. IPOS(2) GO HOLE POSITION:	.Eu. 0) G .GE. LIMIT .LE. LIMIT ST+# DE+10FFST SO11) E 11.53x,24H
DO 100 100 RK(J)=RK DO 105 J 105 RK(J)=RK RK(Z)=AB WRITE(NM	110 THTCRK= C INCREMENT 120 JLUC=JL DO 125 125 IBEGIN(IF (JLOC C INCREMENT	IF (IOFFST IF (CNODE IF (CNODE CNODE = CNOTE WRITE (KM**) GOIL FORMAT(IH) GO TO 32 130 CONTINUE STOP

	SUBROUTINE 1 116 / MITCH AND MATHY STATEM OF A STATEM	
٠	「ハル・アンドリングのアンドリングのアンドリングでは、アンドリング	***LUGL0001
	SUBROUTINE LUG GENERATES A PECTANGULAR REGION WHICH IS USED BY Subroutines farein, sri ann nri	LUGLADOZ
٠	TOT TOT TOTAL SERVICE をおおおおとのできない 日本のでは、「「「「「「」」「「」」「「」」「」「」」「」「」「」「」「」「」「」「」「	F000 T90 T***
	TECHNOLOGY	LUGLOOOS
•	SIMUCIUMEN MESTARCH LABORATORY	LUGL0006
CFI	APPLICATIONS TO USAF STRUCTURAL INTEGRITY PROBLEMS	**LUGL0007 **LUGL0008
	SIDE STIF	LUGLOGO9
	ΥĒ	LUGL0010 LUGL0011
	INTEGER ELNO	LUGLOO12
	COMMON/IO/KP®KP®KTI KTV®KTS	LUGLOOI3
	COMMON/SIZE/NET.NDT	
	COMMON/BEGIW/IBEGIN(6)	1 UGL 0016
	COMMON/END/IEND(6)	LUGLOOI7
	COMMON STREES AND TEST OF THE	LUGL0018
	, ,	LUGL0019
		LUGLOOZO
	00 5 1=1.12	LUGL0021
S	C00PD(I)=0.0	
	W=WIOTH/NELW	1.061.0023
	AR#5.0	LUG-0025
	NELL=LENGTH/(W*AR)+1	LUGL0026
		LUGL0027
		LUGL0028
		LUGL0029
		LUGL0030
	ALCOSENDI-AFRON	LUGL0031
		LUGL0032
	AD#: /1	LUGL0033
		LUGL0034
		LUGL0035

600	COORD(2)=L COORD(10)=W LMASTR=NDW*? LMASTR=NDW*? IF (KT1 .EQ. KW) GO TO 10 WRITE(KW.6000)WIDTH.LENGTH.THK.STFTHK.NELW FORMAT(1H1.60×.9HENTRY LUG.//.23H SUBROUTINE INPUT DATA:.//.11H FORMAT(1H1.60×.9HENTRY LUG.//.23H SUBROUTINE INPUT DATA:.//.11H FORMAT(1H1.60×.9HENTRY LUG.LENGTH=.E12.5./.15H LUG THICKNESS=.E12. EQ. WIDTH=.E12.5./.12H LUG LENGTH=.E12.5.30H (LEFT SIDE STIFFENED R25H LUG STIFFENER THICKNESS=.F12.5.30H (LEFT SIDE STIFFENED R25H LUG STIFFENENTS ACROSS WIDTH=.13./.) WRITE(KW.500.11)NELL.NDW.NDL.NGT.NDT.NIDSS.(COORD(1).1=1.12).AR
100	FORMATICZHOSUBROUTINE LUG STATISTICS: // 37H NUMBER OF ELEMENTS ALLUGIERON LUG LENGTH= 13./ 39H NUMBER OF NODES ALONG WINTH= 13./ 30H NUMLUGIERONG LUG LENGTH= 13./ 39H NUMLUGIERONG LUG LENGTH= 13./ 39H NUMBER OF NODES ALONG LENGTH= 13./ 53H TOTAL NUMBER ELEMENTS= 13./ 39H NUMLUGIEROF NODES ALONG LENGTH= 13./ 53H NUMBER OF N.O.F.S TO RE CONDENSEDLUGIENT GOUT GLOBAL STIFFNESS MATFIX= 13./ 27H ELEMENT COORDINATES: 12FR.31UGIEN/ 22H ELEMENT ASPECT RATIO= , FR.3) CALL SETUP(NSTZE.LMASTR.IMASTR.RASTP, RSS, ISS) ELNO=
20	ISS(IMASTP+ELNO) = IPNTP

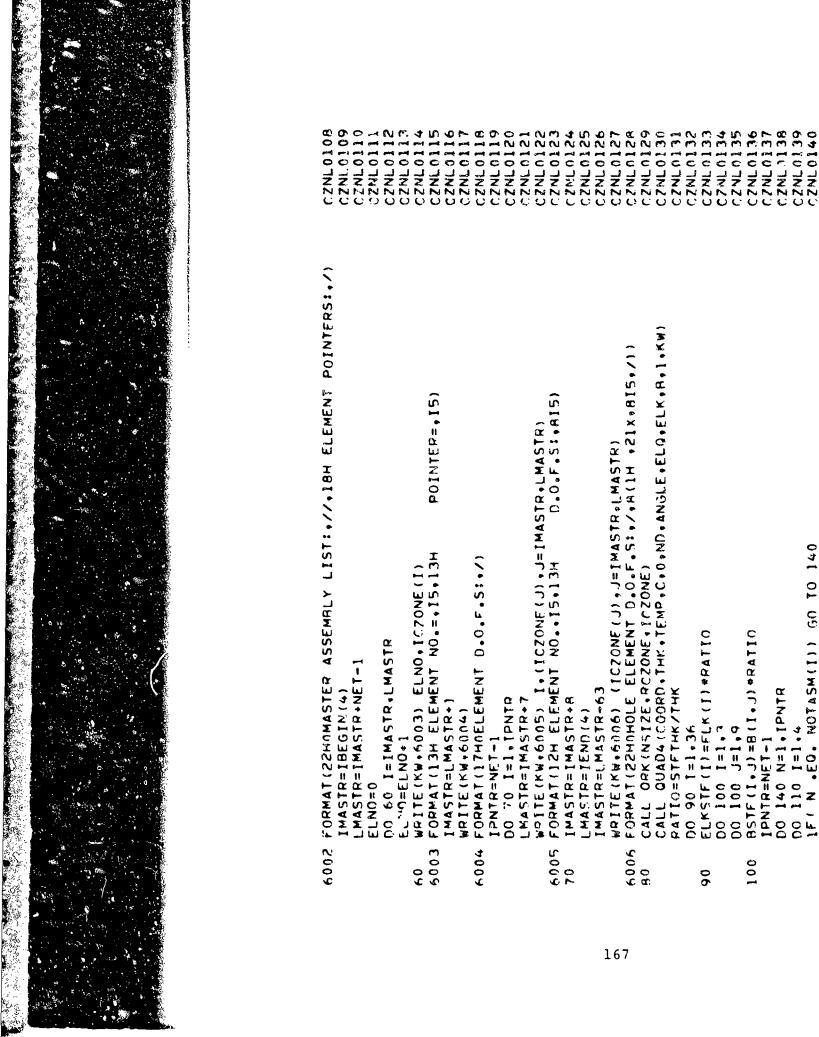
	ISS(IPNT# 07) = ISS(IPNTR+6) + 1 IPNTR = IPNTR - 8	LUGL0072 LUGL0073
2	IMASTP=18EGIN(4) +NFT	LUGL0075
	LMASTP=[MASTR+NFLW+R	LUGL0076
	INODE1=NDT-2+hinu+1	LUGL0077
	LNODE1=1	111610078
	DO 35 I=INONE1+NDT	LUGL0079
	DO 34 IT=IMASTR-LMASTR	LUGL0080
	IF (ISS(II) .En. LNODE1) ISS(II)=I	LUGL0081
	CONTINUE	LUGL0082
35	LN00E1=LN00E1+1	LUGL0083
	1F(KT] .EG. KW) GO TO 40	LUGL0084
	WPITE(***・ハ・・・)	LUGL0085
4002	FOPMAT (2240MASTER ASSEMBLY LIST: . // . 184 ELEMENT POINTERS: . /)	LUGL0086
		LUGLOOB7
	[#ASTD= MASTR+NET-]	LUGL0088
	FLNO=0	LUGLOAR9
	ng 40 I=IMASTP.LMASTR	100C 0000
	ELNO=FLNO+1	LUGL0091
07	BRITE (****) 3) FLNO.ISS(I)	TOGL0092
C	FORMAT (13H ELEMENT NO. = 15,13H POINTER=,15)	LUGL0093
	IMASTP=[MASTR+]	LUGL0094
	1217E (************************************	TrieP0095
4004	FORMAT (17 MOELEMENT 0.0.F.S:./)	10GL¢096
	Di 20 1=1*rE1	LUGL0097
	LMASTR=1MASTR+7	1116L0098
	KRITE(<***)::::/I. (ISS(J).J=IMASTR.LMASTR)	10GL0099
000	FORMAT (1	LUGL0100
5	IMASTR IMASTR.R	LUSL0101
0	CALL ORK (NSTZE+RSS+1SS)	LUGL0102
	CALL GUAD4 (COOPD, THK, TEMP, C, 0, ND, ANGLE, ELQ, ELK, B, 1, KW)	LUGLOIO3
	ARHSTF TIK/TIK	LUGL0104
	00 70 [=1.36	LUGL0105
70	FLKSTF(I) #FLK(I) • AR	LUGL0106

•	00 BG J=1.9	LUG. 0108
£	85TF(1.J) 18(1.J) *AR	2
	NELWHI ZNELW-1	LUGL0110
	ELN0=0	LUGL0111
	DO 100 IROW=1.WELL	LUGL0112
	DO 90 IMERETINECEM	LUGL0113
	ELMO=ELMO+1	
06	CALL ASMLTV(ELNO.8.ELK.ELG.RSS.ISS)	LUGL0115
	€[ND=ELNO+]	LUGL0116
100	CALL ASMLTV(ELNO.8.ELKSTF.ELQ.PSS.15S)	LUGL0117
	LMASTDEND#02	LUGL0118
	IMASTO=18EGIN(5)-1	LUGL0119
	00 110 1=1.1 MASTP	LUGL0120
	12(1)551	LUGL0121
110	PSS(1#AST#+1) = 0.0	LUGL0122
	CALL BCON(RSS,1SS)	LUGL0123
115	in the second	LUGL0124
	CALL STACON (I.NIDSS.RSS.ISS)	LUGL0125
	00 120 1=1.5	LUGL0126
120	1865S(1) #1REGIN(1)	LUGL0127
	NETISSEART.	LUGL0128
	₩ 0₹55≖₩0₹	LUGL0129
	IF(KT] .FO. KW) GO TO 130	LUGL0130
	WATTE (* **60.06)	LUGL0131
6006	FORMAT (1H0.60x.8MEXIT LUG.//)	Ē
130	ONTINUE	
		E .
	END	LUGL0135

•	INE CZO	
	. 4. 8. 8. 8. 8. 8. 8. 8. 8. 8. 8. 8. 8. 8.	000 JNZU+
S. S. D. S. D. S. C. S.	SURROUTINE CZONF GENERATES THE CENTRAL STRIP THAT CONTAINS THE HOLF FOR USE IN THE FARFIELD MESH GENERATED BY SUBROUTINE FARFLD	CZNL0004
		•
	HT (C) 1975 MASSACH	-
•	PEREARCH LAGOPATORY	CZNL000
1	FIRENAL ADDITIONS TO USER STRUCTURAL INTERNAL PRODE	100 NZU
	(1) -040LE (1) -1HOLE (1)	CZNCOOL
	12) .EI D(R) .NO.	CZNLOOI
	:	
	COMMON AND AND AND AND AND AND AND AND AND AN	
	COMMON/SIZE/NOT NOT	
	できることでは、1910年に、1910年に、19	
	COMMON/S1755/15	CZNI 0019
	COMMON/86655/19655161	CZNL0020
	COMMON/STASS/A(3.9), 8STF(3.9)	CZNL0021
	OBTE TEMP/4.0.0/	CZNL0022
	C1-1=1 5 00	CZNL0023
ď	C0000 (1) 20°0	CZNL0024
	# CHAZZINO THE	CZNLAA25
		CZNL0026
	コア・ しょうじり ・うしゅ ボールはんりゃ かんりつれ ・つしゅ ちじま ニーロン トロース 子供 にかまってものの こうかい アンカのじがっぱんり	CZWL 0027
4008	INTERUPT INITIATED BY SURPOUTINE CZONF .	2001825 *C28L008
•	/// 34H CENTER NODE REFERENCE PARAMETER # 14,35H IS OUT OF	RACZNL 0030
	E OF E WINTH (MELW) / . 44H CNODE MUST BE GREATER THAN I AND LF	ZNL003
	S	*CZNL0032
	2100	CZNL0033
3	AFT to 1 + 2 + aff to 1	CZNL0034
	NOT=20(30NOW-24)	CZNL0035

000		CZNL0039 CZNL0046 CZNL0064 CZN
, 6001 10	WRITE(KW*6001) NOW.RIDGS.(MOTASM(1).Ex1.4).([ELSTF(1).F=1.2).(COOPCZNLOOSGRO!1).]=1.12) CORNATIONALIZOPHOSUMMOUNTINE CYONE STATISTICS:.//.JOH NUMBER OF NODES ACPCZNLOOSGROSS WIDTHE.12./.TSM GUMMOER OF SMIDTHE.12./.TSM GUMOSM OF SMICRARL O.O.F.S TO RE CONDENSED OUTCZNLOOSGROSS WIDTHE.12./.TSM GUMOSS MATHIXE.14./.JOH ELEMENTS NOT TO RE ASSEMBLEDCZNLOOSGROSS./.28H ELEMENT COOMDINATECZNLOOSGROSS.12FA.J) CALL SFILD.WS1ZE.2.LMASTA.HCZONE.16/20ME)	OPCZNL 0056 CZNL 0056 CPCZNL 0056 UTCZNL 0056 TECZNL 0056 TECZNL 0060
•	FINDERSTREIBECINICI INDSENDA: I DO 30 IDDW: I P IF (IPOW .EG. 2) INDOE: I LNOOE: INDOE: WODE IONTHE WASTO-NET-FLNOOB ICZONE (IMASTO-NET-FLNOOB FLNOOE: NOO: I	CZNL.0065 CZNL.0065 CZNL.0065 CZNL.0065 CZNL.0065 CZNL.0065 CZNL.0065

	1C20NE (1PM10+1) #1•2	CZNL007
	ICZONE (IPNTA) × ICZONE (IPNTA+1) +1	CZNL007
	1070NF (19NTD+2) =1070NF (19NTD+1) +1	CZNLO07
00	1020MF (10MTB+1) x1020MF (10MT9+2)+1	C2NL007
	LNODE ENDIA	CZNL007
	IF (190 a .go.) LHOOE = 1 a AD *	CZNL007
	00 30 1=1.4FLW	C2NL0078
	2.20% (1.00mm - 3.00mm) (1.20mm) (1.20mm) (1.20mm)	C2NL007
	ننا خ	C2NL008
	1020NE 118NIA + 1 016,20NF (18NIA + 6) - 2	CZNL008
	VF (1 PMT 2 . 6.) .	CZNL008;
	は の これ の こ	CZNL008
30	1-300m1=300m1	CZNL008
	1005 (1) = (1 + 2 + 40 + 40 + 40 + 40 + 40 + 40 + 40	CZNL008
	100% (2) #C500£ -1	CZML008
	100F(3) = CNOOF - 1 + NOW	CZNL 008
	1005 (4) #64008 •40*	CZNLOOB
·	100F(5) #CMM9F•1•*0#	CZNLOOB
	1.300%0=(4)3001	CZNL 009
	100F (7) = CNODE + 1 + 2 + 10 =	CZNL009
	(00F(A) ±CN00E • > • 404	CZNL009
	IDATOR IMAGID - NET - 1 5 - NFL W	CZNI 009
	1020MF (IMASTR-11-11-11-11-11-11-11-11-11-11-11-11-11	CZNL 009
	(*300℃=1	CZNL 009
	\$* In I 07 Cu	CZNL009
	1070NE (IPATE+1200E) = 100F(1) • 2	.600 TN Z 3
	ICZONE (FPNTA-INODE-1) = ICZONE (IPNTA-INODE) -1	CZNL009
0 7	12/10E = 12/00E • 2	CZNLA09
	PMTR= PMTR+16	CZM 010
	1400E=2•(3•NO#•1)-1	CZML019]
	1,400£ = 1,400 € • 4.7	CZNL0102
	30 nm3-300N1=1 05 00	CZNL010;
	ICZÓNE (IPMID) = I	CZNL0104
53	paramipara.	CZNL0109
	IF(KY) .FQ. KW) GO TO AO	CZNL0106
	MOTIFICAN GOODS)	CZNC0107



C2NL-142

130

.EO. IELSTF(1)) 60 TO

DO 120 I=1.2 IF (N .EO. I

CONTINUE

116

~ZWL0141

120	CONTINUE	C2NL0164
	CALL ASMLTV(N. 8. ELK. ELO, RCZONE, ICZUNE)	CZNL0145
	Ç	
6.)	CALL ASMLTV(N&R.ELKSTF.ELO, RCZONE, ICZONE)	C2NL0147
140	1.1	ESTO TNZ J
	(=1,	CZNL0149
150	0 0 =	CZNL0150
	=2.	
	02=	CZNL0152
	-00	CZNL0153
	U	C2NL0154
	F	CZNL n 155
		CZNL0156
	CALL HOLEL (COORD.THK.S.RI.RHOLE.IHOLE.BHOLE)	CZNL0157
	KTIHIMASTR	CZNL0158
	CALL ASMSUB (NET, RHOLE, 140LE, RCZONE, 1CZONE)	651u7W20
	1020NE(1) #CNODE#2	CZML0160
	ICZONE (2) = ICZONE (1) = 1	C27L0161
	IMASTREBEGIN(S)-1	CZML0162
	00 160 Iz1.2	CZNL0163
	J=IMASTR+IC2ONF(I)	CZNI.0164
160	PC20NE(J)=0.0	CZNL0165
	CALL BCON (PC20NF , IC20NE)	CZNL0166
		CZNL0167
	00	CZNL0168
	#	CZNL0169
170	===	CZML0170
	ñ	C214L0171
	Ş	CZNLO172
	VIDS	CZNTU113
	E0	CZNL0174
	XRITE(KW+6007)	CZNLA125
6007	FORMAT (1H0.	CZNL0176
αC)	CONTINUE	CZNLO133
	RETURN	CZNL0178
		02101420

SUBPOUTINE FARFLD (WIDTH.LENGTH.NELW.THK.STFTHK.C.S.CNODE.FI.PRESS.FFDL.0000 FFDLNOGA FFDL 0019 DIMENSION (3.3).S(3.3).48S(1).15S(1).PWORK(1).IWORK(1),RHOLE(2097FFDL0012 FFDL0013 FFDL 0015 FFDL0017 FFDL 0019 FFD10024 FFDL0025 FFDL0026 FFULCO2A FFDL0029 FFDL0030 FFDL 0032 FFOL 0033 FF.01.034 FFDL:0003 かに いい しい ふる FFDL0016 FFDL0018 FFD1 0020 FFDL 0022 ドドひしゃりとろ FFDL0027 FFDL0031 FFDL0011 FFDLOO21 WPITE (KW.6000) WIOTH-LENGTH-NELW-THK.SIFTHK,CNODE-RI-PPESS-INDCTR THAT IS CFNTEDED IN THE VERTICAL DIRECTION 4).IHOLE (2097).ISAVF1(2).ISAVE2(6).ISAVE3(6).IFGS5C(6).ISZSSC(3). (& SURSTRUCTURE) AND IS EITHER CENTERED OR DEF-CENTERED IN THE HOPIZONTAL DIRECTION C FINITE ELEMENT APPLICATIONS TO USAF STRUCTURAL INTEGRITY PROBLEMS (RHOLE (1) + I HOLE (1)) + (IS7SS(1) + NETSS) + (IS7(1) + NET) CODYRIGHT (C) 1975 MASSACHUSETTS INSTITUTE OF TECHNOLOGY SUAROUTINE FARFLO GENERATES A FINITE ELEMENT MODEL. Of a plate with one hole. That is centered in the v AEPOELASTIC AND STRUCTURES PESEARCH LABORATORY BINDCIR. WSIZE . RSS . ISS . NSZWRK . RWORK . I WORK) MIDANENIDSSEPANDE COMMON/S12ESS/NETSS+N0TSS+N10SS COMMON/10/KP+KB+KP+KF1+KF0+KF3 IF (KT1 .EQ. KW) GO TO 10 ##IDTH/2.n-(CNODE-1)*# COMMON/9EGIN/19EGIN(6) COMMON/REGSS/18655(6) LEFT SIDE STIFFENED ONLY COMMON/SIZE/NET NOT LAGTH=LENGTH/2.0-W COMMON/END/1END(A) REAL LENGTH. LNGTH LMASTP=12*NOW+51 (2) 25I • (8) SSZSI® IF (INDCTR .EO. INTEGER CNODE MOLHBANDA+CH NIDSSHNDI-4A W-WIDTH/NEL'S ACON = NOON EDUIVALENCE とうとしてににて・1

,这种是一种,我们是一种,我们也是一种,我们也是一种,我们也是一种,我们也是一种,我们也是一种,我们也是一种,我们也是一种,我们也是一种,我们也是一种,我们也是

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DATA.//.13FFDL 0036
                                                                                                                                                                    FFDL063
                                                                                                                                                                                                               FORMAT (23HASUBROUTINE STATISTICS: . / / . 12H LUG LENGTH= . E12, 5. / . 1 3HHOFFDLAA45
                                                                                                                                                                                                                                                                FFDL.0047
                                                                                                                                                                                                                                                                                                              FFDL n049
                                                                                                                                                                                                                                                                                                                                                                                                                                                        FFDL0055
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    FFDL 0059
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               FFDL0065
                        ** PLATE WINTH=.E12.5./.14H PLATF LENGTH=.E12.5./.33H NUMBFR OF ELEFFOLOG37
                                               SMENTS ACROSS WIDTH=,15,7,17H PLATE THICKNESS=,E12,5,7,21H STIFFENEFFDL0038
                                                                    BR THICKNESS=+F12.5./.334 HOLE CENTFR YNDF RFFFRFNCE CODE=.15./.27HFFDL0039
                                                                                             A HOLE ELEMENT INPUT RANTUS=+E12.5+/+26H APPLIED TENSION PRESSURE=+FFOLNO40
                                                                                                                                         PCHESIPE CAT PROBLEM: 1.39x.73H INDICATOR=11PLATE WITH FNU NODES ANFFOLOG42
                                                                                                                                                                                                                                      D.O.F.S TO RE CONDENSED FFDL 0046
                                                                                                                                                                                                                                                                                       FFDL0048
                                                                                                                                                                                                                                                                                                                                    FFDL0050
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                                                                                                                                                                                                                                                                                                                                                                                                         FFDL0053
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                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 FFOLA363
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         FFDL0064
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       FFDL n 0 66
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                                                                                                                   (INDICATOP=0 $FFDL 0041
                                                                                                                                                                                                                                                                                                                                                          FF DL 0051
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     FFDL0061
 INPLI
FARFLD.///.22H SUBROUTINE
                                                                                                                   GE12.5./.314 STATIC CONDFNSATION INDICATOR=.14.374
                                                                                                                                                                                                                                       RLE OFFSET=+F12.5./.75H NUMBER OF INTERNAL
                                                                                                                                                                 WED WITH HOLE-NO LOADS OR 3.C. APPLIED))
WRITE(KW.5001) LNGTH.F.VIDS
                                                                                                                                                                                                                                                           GOUT OF GLOPAL STIFFNESS MATRIX= 15.//)
                                                                                                                                                                                                                                                                                    SETUP (NSIZE + NCON+LMASTR+RSS+ISS)
                                                                                                                                                                                                                                                                                                                                                                                                                                                       F( N .EQ. ?) IDOF1=(2*NDW+1) #2-1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                            N .EQ. 2) 150F2=(NDM+1)*2-1
                                                                                                                                                                                                                                                                                                                                                                                                        PNTR=IMASTR+NET+(N-1)+4#ND#
FORMAT (1H1.59x.12HENTRY
                                                                                                                                                                                                                                                                                                                                                                                                                             SS(IMASTR+N-1)=IPNTR
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            DO 20 I=INOF1.LMASTP
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          00 40 1=INOF1.LMASTR
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     MASTP=IDOF 1+2+NNW-1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  MASTR=IDOF2+2*NDW-1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         0 30 I=IDOF2+LMAST
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             SS(IMASTR+2)=IPNTR
                                                                                                                                                                                                                                                                                                                                                          JOF2=2+(3+40+1)-1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             DOF2=(ND#+1)+2-1
                                                                                                                                                                                                                                                                                                         MASTP=IBEGIN(4)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           PATR=IPNTR+1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        PATRE IPNTD+1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  SS(IPNTR)=J
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              SS([PNTR)=]
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  MASTR-NOW+2
                                                                                                                                                                                                                                                                                                                                                                                 0 30 N=1.2
                                                                                                                                                                                                                                                                                                                                   00F1=1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       00F1=1
                                                                                                                                                                                                                                                                                       CALL
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|<u>|</u>
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FFDL0072
FFDL0073
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                                             FFDL0075
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                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              FFDL0107
                                                                                                                                       FFDL 0081
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 CALL LUGIWIDTH.LNGTM.NELW.THK.STFTHK.C.NSZWPK.RWORK.IWORK)
                                                                                                                                                                                                     FORMAT(22HOMASTER ASSEMBLY LIST:•/+10H POINTERS:•~15)
                                                                                                                                                                                                                                                                               FORMAT (13HO).UG ELEMENT .12,9H 0.0.F.S:./)
                                                                                                                                                                                      (155(I), I=100F1, 100F2)
                                                                                                                                                                                                                                                                                               WRITE (KW+6004) (155(1).[=100F1+100F2)
                                                                                                                                                                                                                                                                                                                                                                                         WPITE(KW+6004) (ISS(I)+I=IDOF1+IDOF2)
                                                                                                                                                                                                                                                                                                                                                                          FORMAT (23H0CZONE ELEMENT D.O.F.S:./)
                                                                                                                                                                                                                                  IDOF1=IREGIN(4) +NET+(N-1) *4*NDW
                                                                                                                                         G0 T0 An
                                                                                                                                                                                                                                                                                                                                                                                                         CALL ORK (NSTZE+RSS+TSS)
                DO 50 I=IDOF2.LMASTR
                                                                                           00 60 I=100F1,100F2
                                                                                                                                                                                                                                                 IDOF2=IDOF1+4*NDW-1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    SAVEZ(I) = IBEGIN(I)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   SAVE3(1)=IEND(1)
                                                                                                                                                                                                                                                                 MPITE(KW.6003) N
                                                                                                                                                                                                                                                                                                              FORMAT(1H .2016)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 ISZ(I)=ISAVF1(I)
                                                                                                                                                                                                                                                                                                                                                                                                                                                       ISAVE1(1)=ISZ(1)
                                                                                                                                       FIRTI .EG. KW)
                                                                                                                                                      JOE 1=19EGIN(4)
                                                                                                                                                                                     #RITE (K#+6902)
                                                                           100F2=100F1+47
                                                                                                                                                                                                                                                                                                                                                           WRITE (KW+6005)
                                                                                                                                                                       100F2=100F1+2
                                                                                                                                                                                                                                                                                                                            100F1=In0F2+1
                                                                                                                                                                                                                                                                                                                                            [DOF 2= IEND (4)
                                                              DOF 1 = 8 + NUV + 1
                                                                                                                         PNTR=IPNTR+1
                                                PNTR-IPN'R+1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 51=1 011 00
                                                                                                                                                                                                                                                                                                                                                                                                                                                                      00 100 I=1.4
 MASTR=4+NDW
                              SS(IPNTR)=[
                                                                                                          SS(IPNTR)=I
                                                                                                                                                                                                                    DO 70 N=1.2
                                                                                                                                                                                                                                                                                                                                                                                                                       SSOIN=ASGIN
                                                                                                                                                                                                                                                                                                                                                                                                                                       5.1=1 00 00
                                                                                                                                                                                                                                                                                                              6,00%
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FFDL0135
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                                                                                      FFDL0114
                                                                                                                                                             FFDL0119
                                                                                                                                                                                                                        FFDL.0123
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FFOL 0108
             FFDL0109
                            FFDL0110
                                                         FFDLO112
                                                                        FFDL 0113
                                                                                                     FFDL0115
                                                                                                                   FFOLO116
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                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               FFDL0141
                                            FFDL 9111
                                                                                                                                                                                            FFDL0121
                                                                                                                                                CALL CZONE (WIDTH, NELW, THK, STFTHK, C, S, CNODE, RI, NSZWRK, RWORK, IWORK,
                                                                                                                                                                                                                                                                                                                                 IF (INDCTO .EO. 0) GO TO 190
PLATE WITH END NODES AND HOLE-NO B.C. OR APPLIED LOADS
                                                            CALL ASMSUB (N. RWORK, IWORK, RSS. ISS)
                                                                                                                                                                                                                                                                                                     CALL ASMSUB(3,RWORK, [WORK,RSS,ISS)
                                                                                                                                                                                                                                                                                                                                                                              STACON (I .NIDSS.RSS.ISS)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  DC 200 I=100F1, IDOF2,2
                                                                                                                                                                                                                             IBEGIN(I)=ISAVE2(I)
                 REGIN(I)=ISAVE2(I)
                                                                                                                      (SAVE2(I)=IBEGIN(I)
                                                                                                                                                                                                                                                         [B655C(I)=IB65S(I)
                                                                                                                                                                                                                                                                                        182886(1)=18288(1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     MASTR=18EGIN(5)-1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               RSS (LMASTR+T) =0.0
                                                                                                                                                                                                                                            (END(I)=ISAVE3(I)
                                                                                                                                                                                                                                                                                                                                                                                                                                         100F1=(2*ND#+1)*2
                                 IEND(I)=ISAVE3(I)
                                                                                                                                     [SAVE3(I)=IEND(I)
                                                                                                                                                                                                                                                                                                                                                                                                           CHESIRE CAT PROBLEM
                                                                                                                                                                                               [SZ(I)=ISAVE1(I)
                                                                                          ISAVE1(I)=ISZ(I)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 ISS(IMASTR)=I
                                                                                                                                                                                                              00 170 I=1.6
                                                                                                                                                                                                                                                                         DO 180 I=1.3
                                                                                                          30 150 I=1.6
                                                                                                                                                                                  DO 160 I=1.2
                                                50 130 N=1.2
                                                                            00 140 1=1.2
                                                                                                                                                                   RHOLE . IHOLE)
                                                                                                                                                                                                                                                                                                                     WIDSS=WIDSV
                                                                                                                                                                                                                                                                                                                                                                                                                                                        100F2=6*NDW
                                                                                                                                                                                                                                                                                                                                                                                CALL STAC(
60 TO 229
                                                                                                                                                                                                                                                                                                                                                                                                                                                                       MASTR-1
                                                                                                                                                                                                                                                                                                                                                                                                                           APPLY 9.C.
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200	ASTR=IMAST	FFDL0144
	100F1=(2*NDH+1+NDH/2)+2-1	FFDL0145
	S(IMASTP)=	FFDL0146
	RSS(LMASTP+100F1)=0.0	FFDL1147
	IOOF1=6*NDW+2	FF0L0148
	OF 2=8*N	FFDL0149
	1 1 1 1	FFDL0150
	DO 210 I=INOF1.100F2.2	FFDL0151
	RSS (LMAST	FFDL0152
210	RSS (LMASTR+1+2) =PS	FF0L0153
C ADD	IN ADDITE	FF01.0154
	(STF THK-THK)	FFDL 0155
	S(LMASTP+JD0F2+2	FF0L0156
	SILMASTO+150F2	FF01.0157
	LI BCON (PSS+1SS)	FF0L0158
		FF0L0159
	CALL STACON (1.NIDSS. RSS. ISS)	FF0L0160
220	00 221 1=1.2	FFDL0161
2) 2SI=(I) SSZ	FF01.0162
	15255(3)=NInS\$	FF0L0163
	00 252 1=1.6	FFD1.0164
255	5SS (I) = 1BE(FFOLUIGS
	¥	FFOL 0166
	ITE (KW.6006	FFDL0167
9009	L	01010
ሞን	CONTINUF	FF0L0169
	RETURN	DL 017
	ENIO	FFDL0171